

# Cognition

## The presence of irrelevant alternatives paradoxically increases confidence in perceptual decisions

--Manuscript Draft--

<b>Manuscript Number:</b>	COGNIT-D-22-00442R2
<b>Article Type:</b>	Full Length Article
<b>Section/Category:</b>	
<b>Keywords:</b>	confidence; perceptual decision making; multiple alternatives; bayesian confidence hypothesis; computational modeling
<b>Corresponding Author:</b>	Nicolás Comay ARGENTINA
<b>First Author:</b>	Nicolás Comay
<b>Order of Authors:</b>	Nicolás Comay Gabriel Della Bella Pedro Lamberti Mariano Sigman Guillermo Solovey Pablo Barttfeld
<b>Abstract:</b>	<p>Confidence in perceptual decisions is thought to reflect the probability of being correct. According to this view, confidence should be unaffected or minimally reduced by the presence of irrelevant alternatives. To test this prediction, we designed five experiments. In Experiment 1, participants had to identify the largest geometrical shape among two or three alternatives. In the three-alternative condition, one of the shapes was much smaller than the other two, being a clearly incorrect option. Counter-intuitively, confidence was higher when the irrelevant alternative was present, evidencing that confidence construction is more complex than previously thought. Four computational models were tested, only one of them accounting for the results. This model predicts that confidence increases monotonically with the number of irrelevant alternatives, a prediction we tested in Experiment 2. In Experiment 3, we evaluated whether this effect replicated in a categorical task, but we did not find supporting evidence. Experiments 4 and 5 allowed us to discard stimuli presentation time as a factor driving the effect. Our findings suggest that confidence models cannot ignore the effect of multiple, possibly irrelevant alternatives to build a thorough understanding of confidence.</p>
<b>Suggested Reviewers:</b>	<p>Dobromir Rahnev rahnev@psych.gatech.edu Dr. Rahnev is an expert in computational models of confidence and metacognition. Is one of the leaders of the "visual metacognition goals" initiative that, among other things, encourages the use of multi-alternative tasks to study confidence judgments.</p> <p>Ariel Zylberberg ariel.zylberberg@gmail.com Dr. Zylberberg is an expert in computational models of decision making and confidence. We discuss several of his models and work in our paper.</p> <p>Megan Peters megan.peters@uci.edu Dr. Peters is an expert on computational models of confidence and metacognition. Some of her work and models are discussed in our paper.</p> <p>Brian Odegaard bodegaard@ufl.edu Dr. Odegaard is an expert in behavioral experiments and computational models of perceptual decision making and confidence.</p> <p>Paul Windschitl paul-windschitl@uiowa.edu Dr. Windschitl is an expert in decision making under uncertainty. He is the first author</p>





January 6<sup>th</sup>, 2023

Dear Cognition Editor:

We are pleased to send you the revised version of the manuscript entitled “The presence of irrelevant alternatives paradoxically increases confidence in perceptual decisions” for consideration in Cognition.

In this revised manuscript, we responded to the suggestions of reviewer 2. Text has been modified accordingly, and we also added a new figure for clarity (Fig 3b).

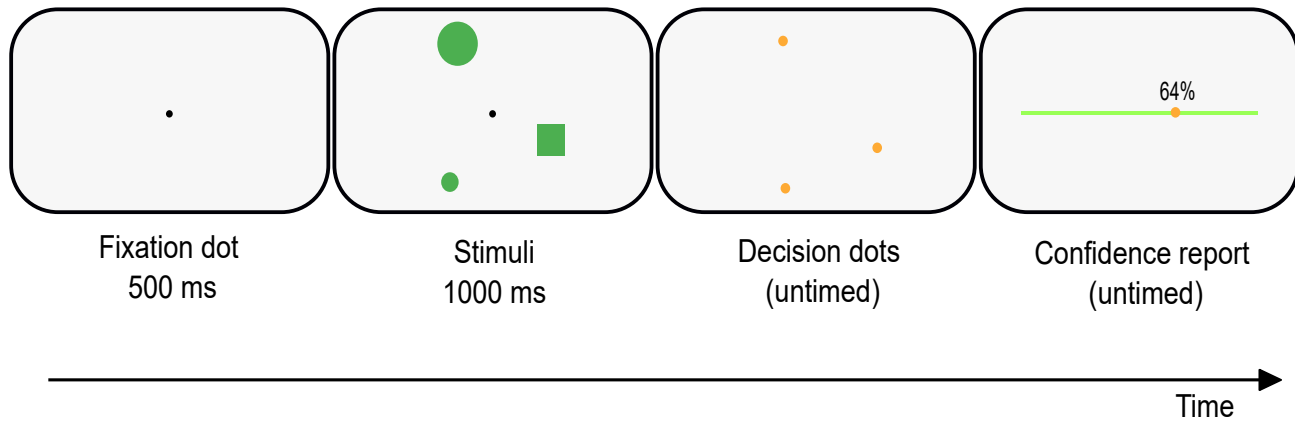
To guarantee replicability, we have made our data, scripts and experiments publicly available at [https://github.com/nicolascomay/confidence\\_dud](https://github.com/nicolascomay/confidence_dud).

Thank you for considering our manuscript.

Cordially yours,

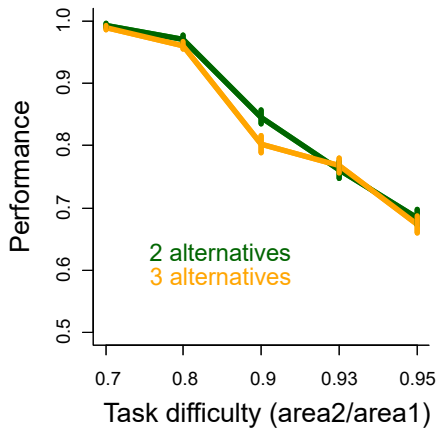
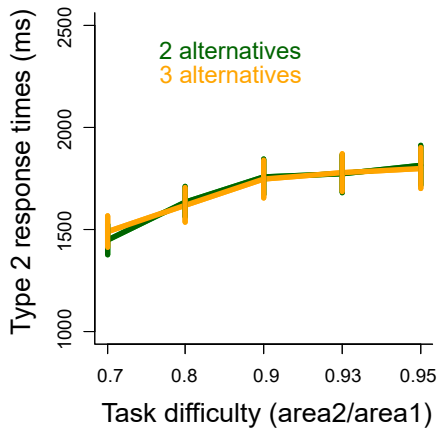
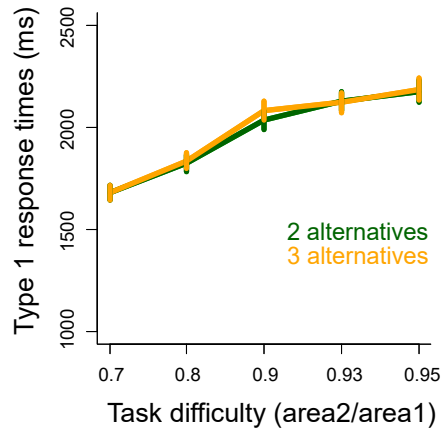
A handwritten signature in blue ink, appearing to read "Pablo Barttfeld", with a stylized flourish underneath.

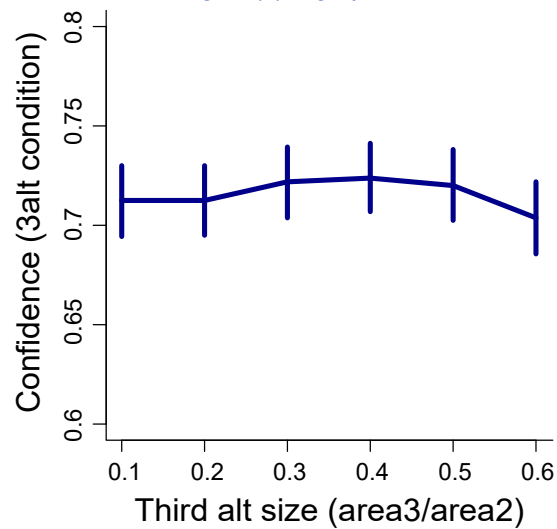
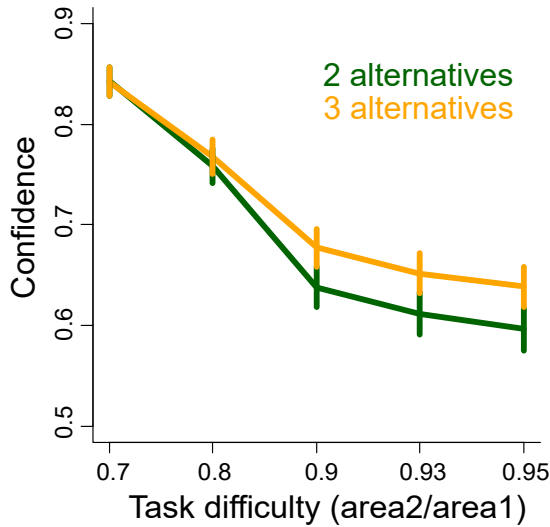
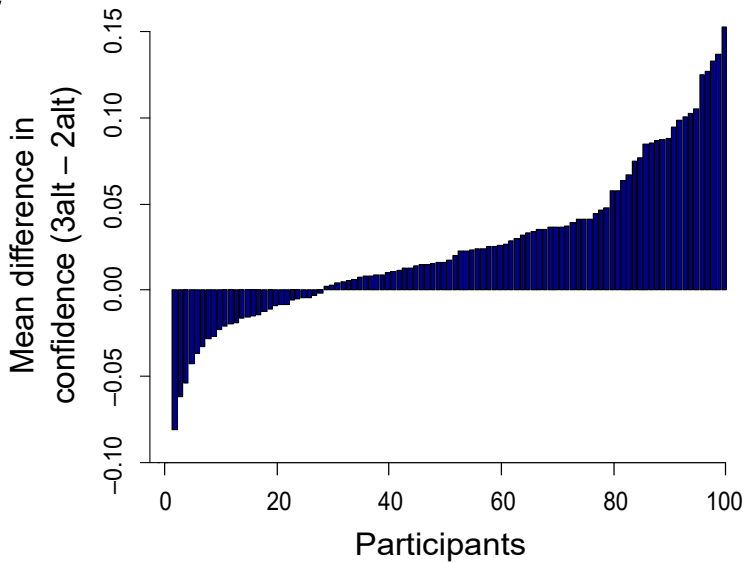
Dr. Pablo Barttfeld  
Instituto de Investigaciones Psicológicas  
Universidad Nacional de Córdoba, Argentina  
Consejo Nacional de Investigaciones Científicas y Técnicas, Argentina  
Email: pablob@conicet.gov.ar  
Phone: +54 9 3541 522967  
Ciudad de Córdoba, Córdoba, Argentina.

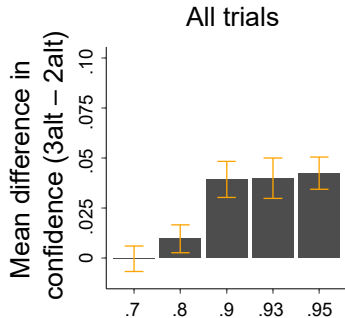
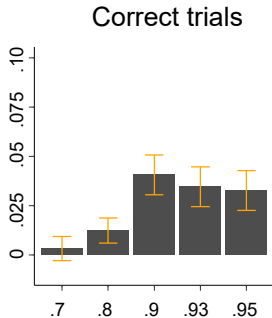
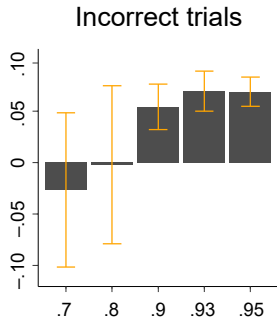


Figure(s)

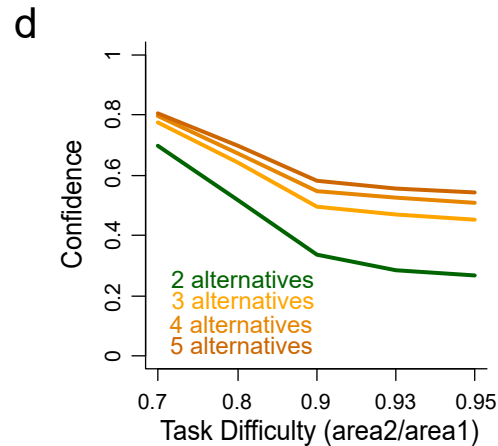
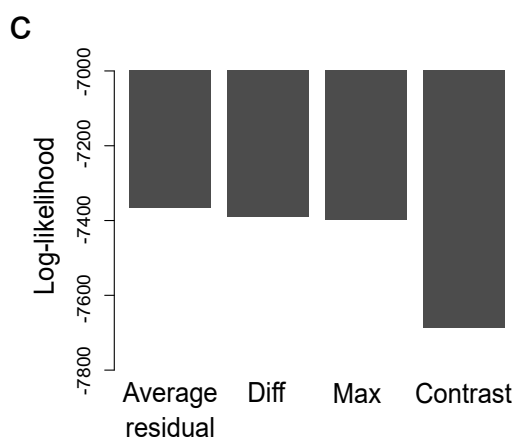
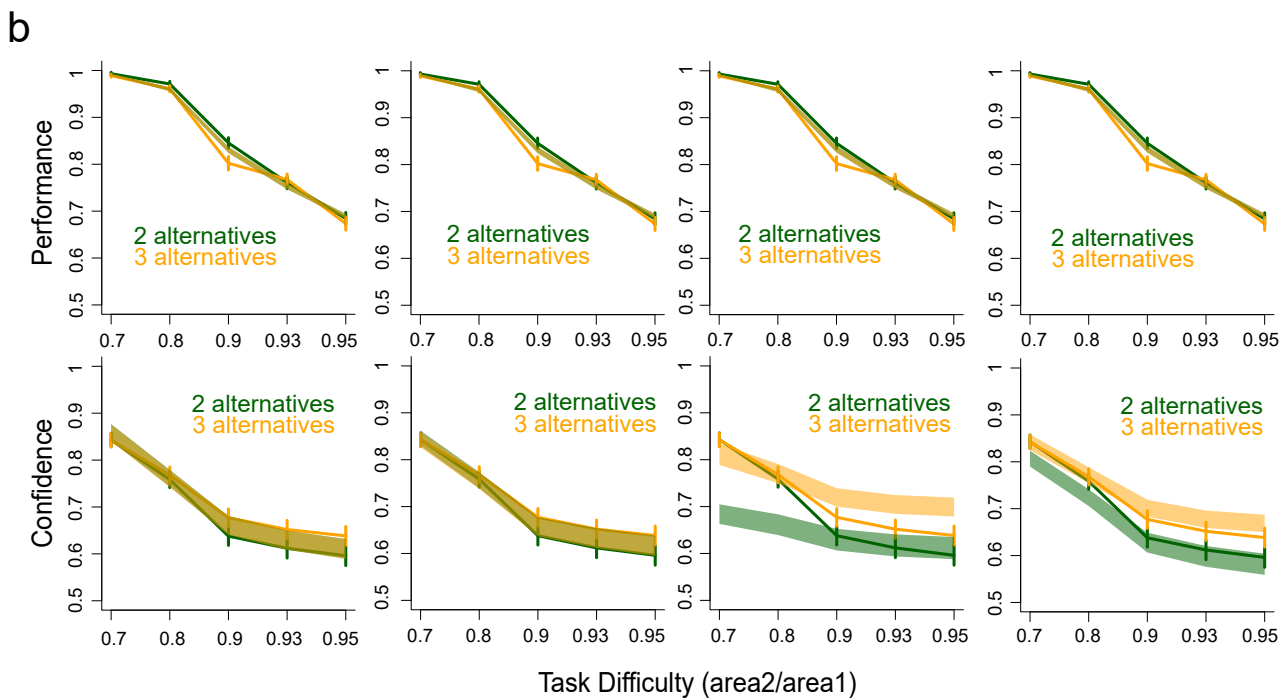
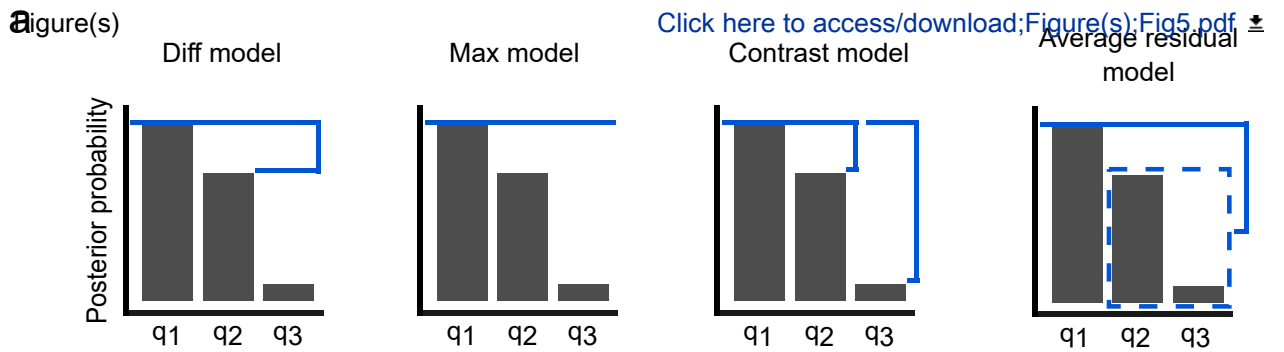
[Click here to access/download;Figure\(s\);Fig2.pdf](#)



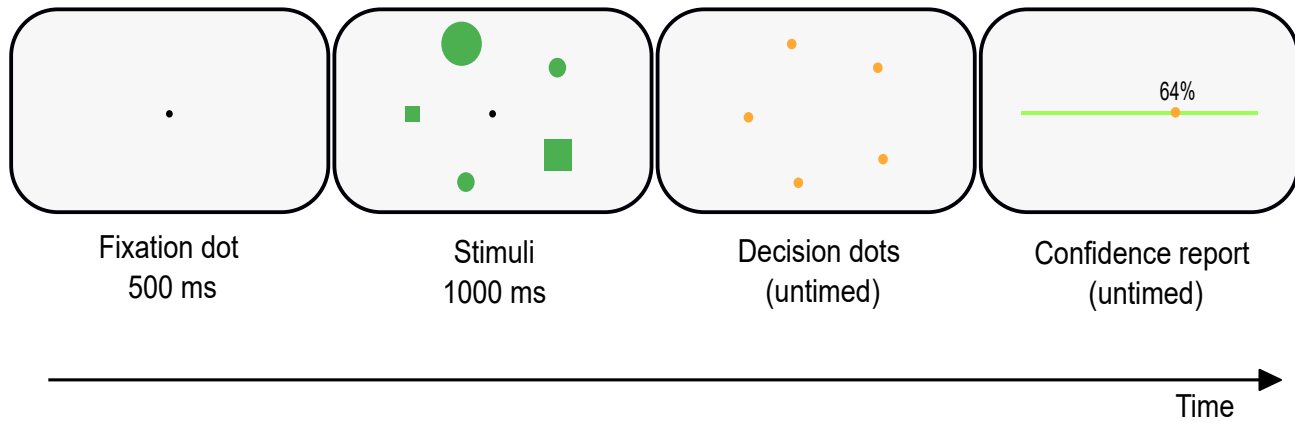
**c**

**a****b****c**

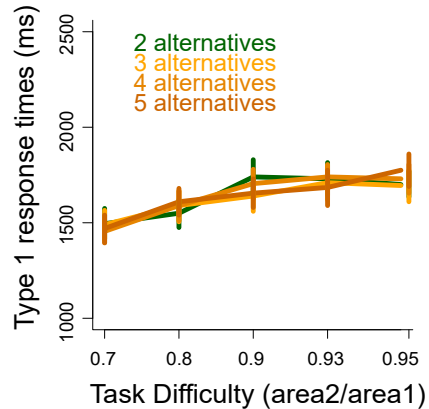
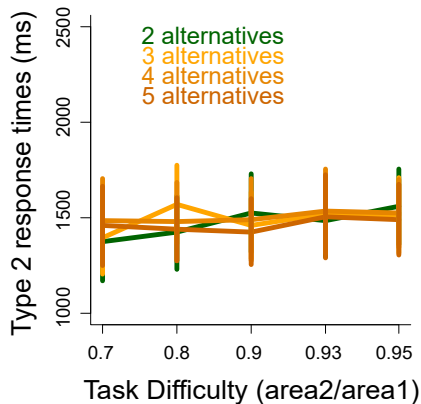
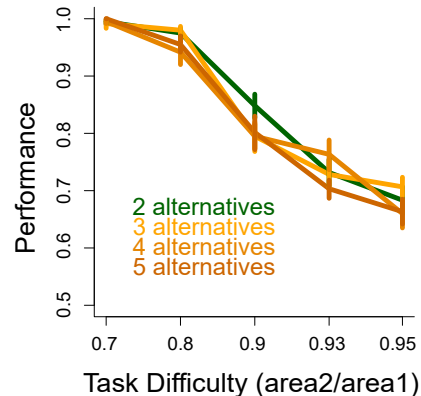
Task difficulty (area2/area1)

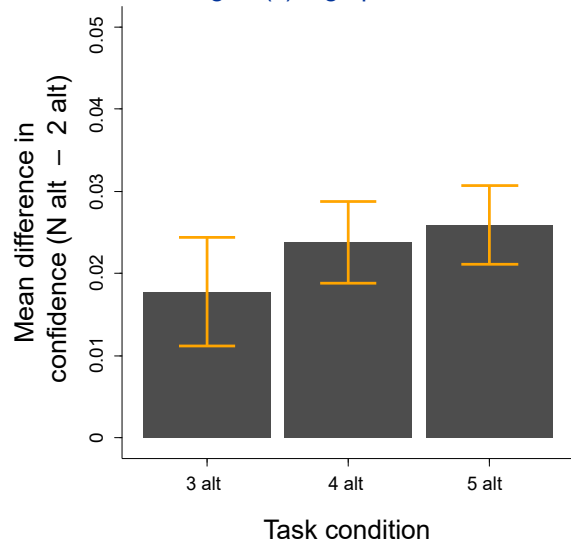
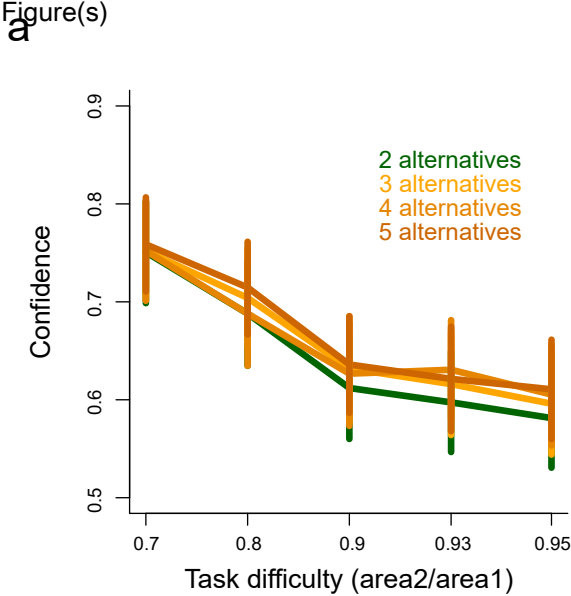




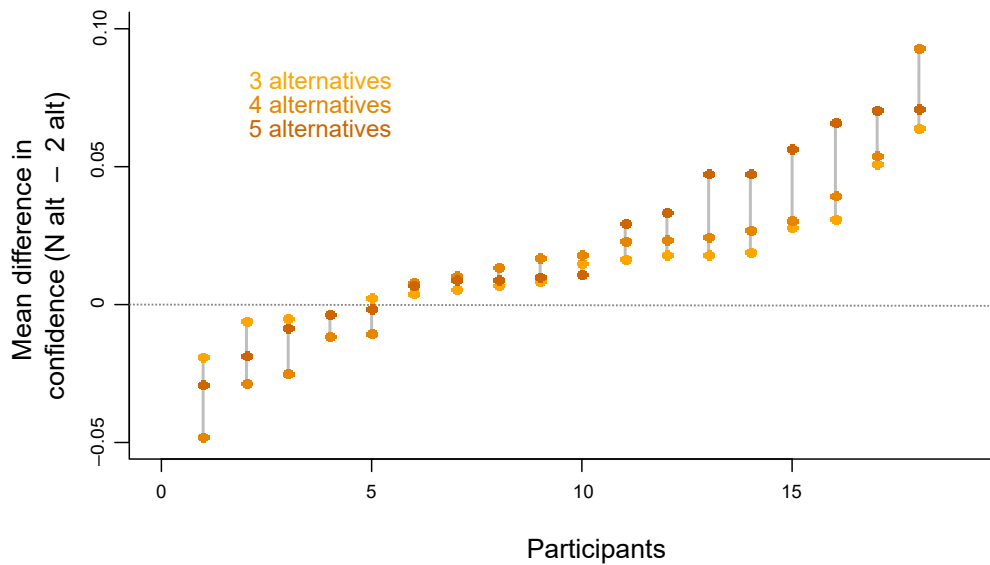


Figure(s)

**b**[Click here to access/download;Figure\(s\);Fig7.pdf](#)**c**

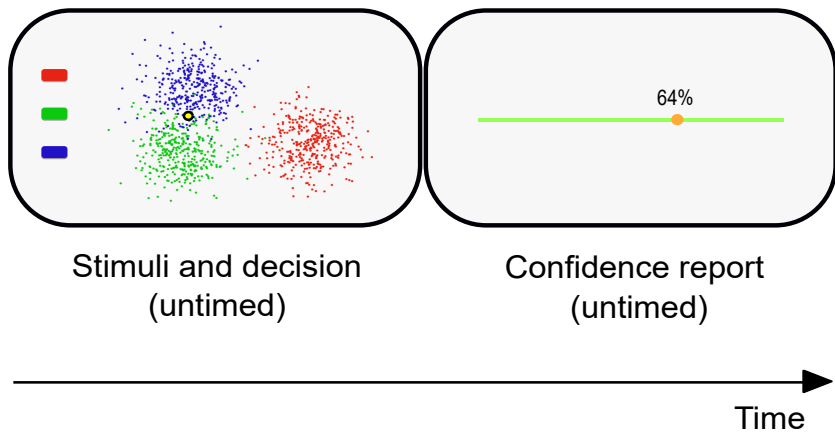


**c**

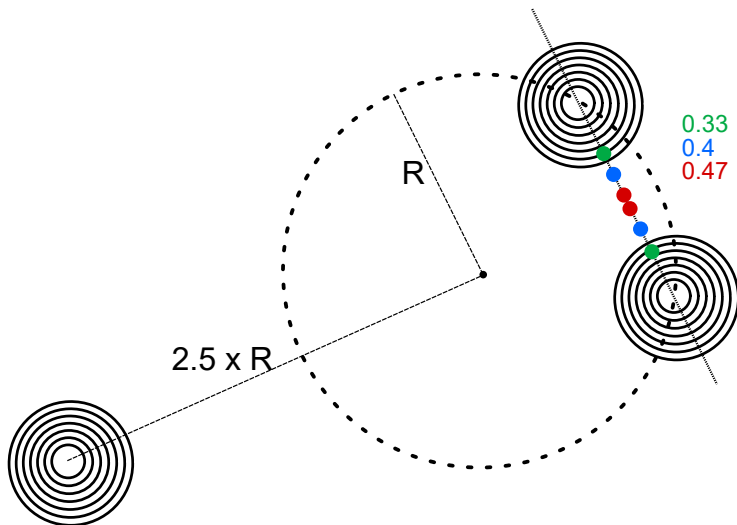




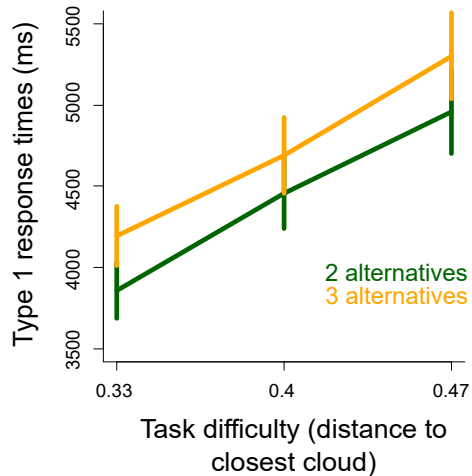
a



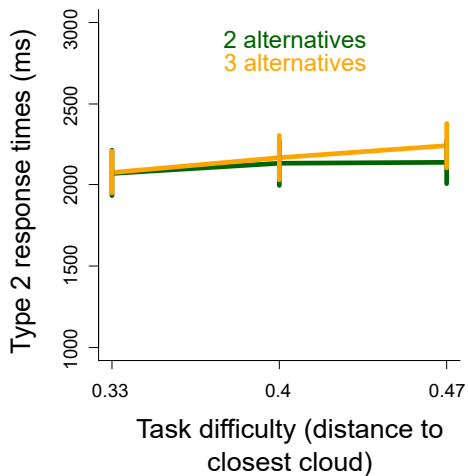
b



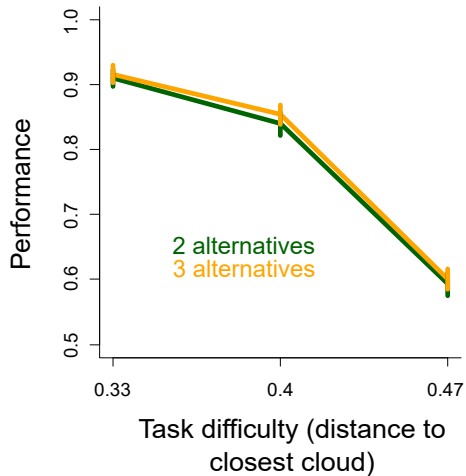
**a**



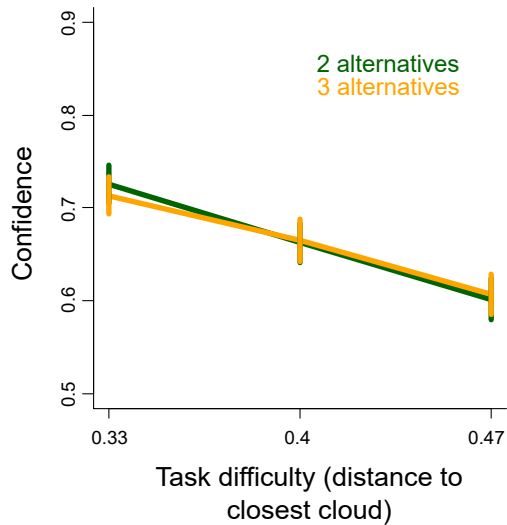
**b**



**c**

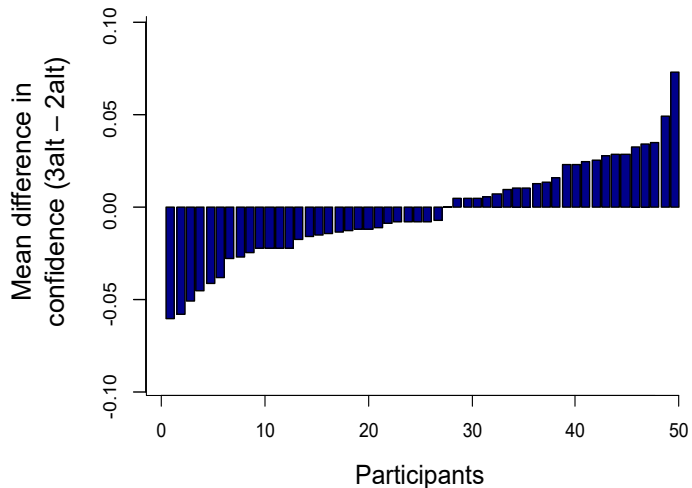


Figure(s)



b

[Click here to access/download;Figure\(s\);Fig11.pdf](#)

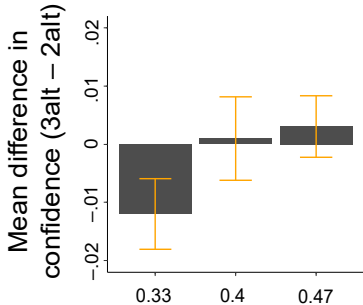


**b**

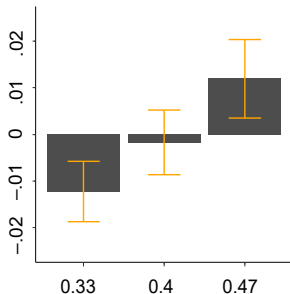
[Click here to access/download;Figure\(s\);Fig12.pdf](#)



All trials

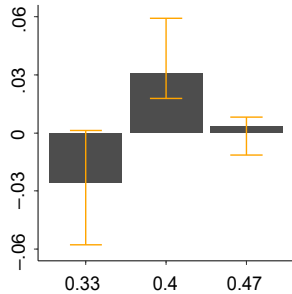


Correct trials



**c**

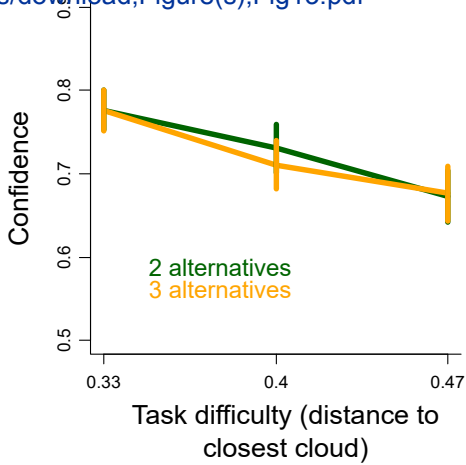
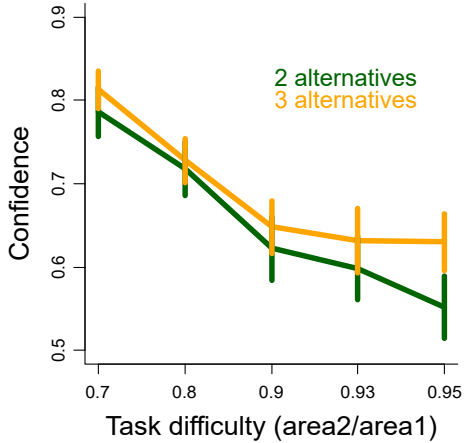
Incorrect trials



Task difficulty (distance to closest cloud)

Figure(s)

[Click here to access/download;Figure\(s\);Fig13.pdf](#)





Irrelevant alternatives can increase confidence in perceptual decisions

Confidence deviates from the Bayesian confidence hypothesis in multialternative tasks

A new Bayesian model of confidence that accounts for the effect is proposed

## The presence of irrelevant alternatives paradoxically increases confidence in perceptual decisions

Nicolás A. Comay<sup>a+</sup>, Gabriel Della Bella<sup>a</sup>, Pedro Lamberti<sup>b</sup>, Mariano Sigman<sup>c,d</sup>,  
Guillermo Solovey<sup>e\*</sup>, Pablo Barttfeld<sup>a\*</sup>

a- Cognitive Science Group. Instituto de Investigaciones Psicológicas (IIPsi), CONICET-UNC, Facultad de Psicología, Universidad Nacional de Córdoba, Boulevard de la Reforma esquina Enfermera Gordillo, CP 5000. Córdoba, Argentina  
[nicocomay@gmail.com](mailto:nicocomay@gmail.com)

b- Facultad de Matemática, Astronomía, Física y Computación, Universidad Nacional de Córdoba, Córdoba, Argentina.

c- Laboratorio de Neurociencia, Universidad Torcuato Di Tella, Buenos Aires, Argentina.

d- Facultad de Lenguas y Educación, Universidad Nebrija, Madrid, Spain.

e- Instituto de Cálculo, Facultad de Ciencias Exactas y Naturales, UBA-CONICET, Buenos Aires, Argentina

+ *corresponding author*

\* *last authors*

## Abstract

Confidence in perceptual decisions is thought to reflect the probability of being correct. According to this view, confidence should be unaffected or minimally reduced by the presence of irrelevant alternatives. To test this prediction, we designed five experiments. In Experiment 1, participants had to identify the largest geometrical shape among two or three alternatives. In the three-alternative condition, one of the shapes was much smaller than the other two, being a clearly incorrect option. Counter-intuitively, confidence was higher when the irrelevant alternative was present, evidencing that confidence construction is more complex than previously thought. Four computational models were tested, only one of them accounting for the results. This model predicts that confidence increases monotonically with the number of irrelevant alternatives, a prediction [we tested](#) in Experiment 2. In Experiment 3, we evaluated whether this effect replicated in a categorical task, but we did not find supporting evidence. Experiments 4 and 5 allowed us to discard stimuli presentation time as a factor driving the effect. Our findings suggest that confidence models cannot ignore the effect of multiple, possibly irrelevant alternatives to build a thorough understanding of confidence.

*Keywords: confidence, perceptual decision making, multiple alternatives, bayesian confidence hypothesis, computational modeling, open data*

## 1. Introduction

We constantly make decisions under uncertainty, accompanied by a feeling of confidence—a belief or a subjective feeling that our own thoughts, knowledge, performance, percepts or decisions are correct (Grimaldi et al., 2015; Mamassian, 2016; Meyniel et al., 2015). To be useful in our everyday activities, confidence has to reflect the true likelihood of being correct (Ais et al., 2016). However, this correspondence is not perfect, and several biases have been described in the literature (Rahnev & Denison, 2018), including overconfidence in difficult tasks and underconfidence in easy tasks (Baranski & Petrusic, 1994; Gigerenzer et al., 1991), a mismatch between confidence and accuracy on individual trials (Maniscalco & Lau, 2012), and overconfidence due to misperception of stimulus variability (Zylberberg et al., 2014). However, despite these findings, the dominant view of the field is that confidence reflects the probability that the decision is correct. This definition is known as the Bayesian confidence hypothesis (BCH) (H.-H. Li & Ma, 2020; Meyniel et al., 2015; Sanders et al., 2016) and is inline with the classical assumption—known as independence of irrelevant alternatives (Luce, 1979)—that the subjective value of a stimulus is only dependent on the stimulus properties.

The Bayesian confidence hypothesis is based mostly on 2-alternative forced choice tasks (2AFC), because they allow for a relatively easy and straightforward computational modeling of confidence (Rahnev, 2020) using diverse approaches, such as signal detection theory (Fleming & Lau, 2014), accumulation of evidence (Pleskac & Busemeyer, 2010; Ratcliff & Starns, 2013) and Bayesian modeling (Drugowitsch et al., 2014; Galvin et al., 2003; Kepecs & Mainen, 2012; Mamassian, 2016; Pouget et al., 2016). However, while methodologically useful, 2AFC tasks are a large oversimplification of the decision-making process, often implying more than two (or an undefined number of) options (H.-H. Li & Ma, 2020; Niwa & Ditterich, 2008; Rahnev, 2020). Including a larger number of alternatives may not only reveal that the methodological tools developed for 2AFC tasks are insufficient, but also that the proposed mechanisms are wrong (H.-H. Li & Ma, 2020). Specifically, the context in which we make decisions might alter our subjective interpretation of the facts (Ariely & Wallsten, 1995; Northoff & Mushiake, 2020). One example is the attraction effect (Huber et al., 1982): when deciding between two alternatives (the focal options), the addition of a third one—similar to one of the focal alternatives regarding one attribute but inferior in another attribute—may increase the probability for choosing that focal option. Critically, this kind of context phenomena has been shown to play a role both in conceptual and perceptual processes (Trueblood et al., 2013), so they are thought to be a fundamental part in our decision processes. Moreover, it has recently been proposed that the allocation of attention—modulated by the stimuli location (Winter & Peters, 2021)—might also give rise to context influence on decision-

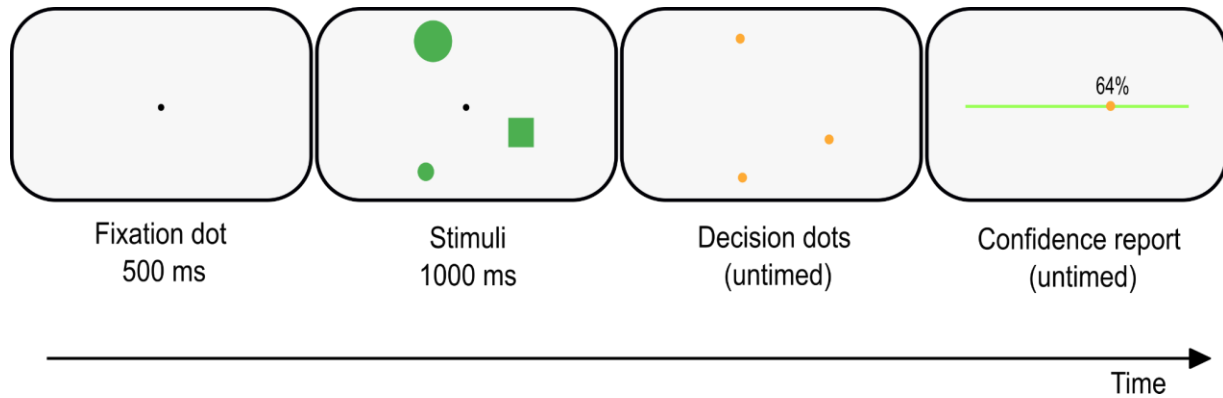
making. Nevertheless, partly due to the prevalence of 2AFC tasks paradigms, the impact of these effects on confidence remains unknown.

Building on these ideas we explored whether a phenomenon already described in the literature for likelihood judgments (Windschitl & Chambers, 2004), line-up identifications (Charman et al., 2011) and associative memory (Hanczakowski et al., 2014) takes place in multi-alternative perceptual decision-making. This effect is defined as “*the tendency to become more confident that a chosen response option is correct if it is surrounded by implausible response options*” (Charman et al., 2011, p. 479) and it is called the “dud-alternative effect”. Bayesian models of confidence predict that confidence should remain virtually invariant when adding irrelevant alternatives, because these hardly affect the probability of being correct. Moreover, they practically do not affect the difference between the posterior probabilities that the two best options are correct, a recently proposed computation for confidence in multi-alternative tasks (H.-H. Li & Ma, 2020). On the other hand, the dud-alternative effect found in non-perceptual tasks predicts that confidence should paradoxically increase.

We investigated the influence of irrelevant alternatives on confidence in three perceptual decision making tasks. In contrast to other decision making processes, perceptual decision making tasks are mainly based on incoming sensory information. In Experiment 1 we studied the effect of a third, irrelevant stimulus on confidence and contrasted our data with predictions from four computational models. In Experiment 2 we replicated the results from Experiment 1 and, based on the models’ simulations, extended them up to three irrelevant stimuli. In Experiment 3 we explored how stimuli-dependent our results are, using a task recently introduced to study confidence in a three alternative decision making context (H.-H. Li & Ma, 2020). In Experiments 4 and 5, we tested whether the differences found in the two previous paradigms are due to differences in the stimuli exposure duration.

## **2. Experiment 1**

We designed a size discrimination task to evaluate the effect of the presence of a third, weak alternative (i.e. dud alternative) in confidence (Fig. 1). This task allowed us to manipulate the subjective value of the alternatives, making them more or less eligible only by varying their relative size.



**Fig. 1.** Size discrimination task. Participants had to decide which was the largest shape. The size of the stimuli varied in every trial, and the relative size of the two largest shapes controlled the difficulty (established in 5 levels). Half of the trials had 2 alternatives and the other half had 3 alternatives, making up a total of 120 trials. The third alternative was very small when present, and varied in size (see Methods). After choosing the largest shape, participants had to report how confident they felt about their decision on a scale from 0% (not confident at all) to 100% (completely confident).

## 2.1 Materials & methods

The task was programmed in JavaScript using the library jQuery. It ran on a JATOS (Lange et al., 2015) server. The experiment could be run on mobile devices or desktop computers.

### 2.1.1 Participants

101 participants took part in Experiment 1 (63% females; mean age = 29.46, sd = 8.83). The study was approved by the ethical committee of the Institute of Psychological Research (IIPsi - CONICET - Córdoba, Argentina). Participants should read and accept an informed consent prior to the experiment. All participants reported no psychiatric, illegal drug consumption or neurological history. Instructions were written on screen prior to the experiment. Thirty four % of the sample performed the experiment on a mobile device, whereas the rest performed it on a computer.

### 2.1.2 Experimental design

The experiment consisted of a decision making task where participants had to decide which of two or three geometric shapes was the largest. It had 120 trials, 60 with two alternatives and 60 with three alternatives. The shapes were circles and squares, and the two largest shapes were always a circle and a square (to make the comparison harder). On half of the trials a circle was the correct option, and on the other half a square. The third alternative, when present, was randomly a square or a circle, and it was much smaller than the other 2 shapes in order to make it easily discarded (in fact, it was only chosen on 7 out of 11751 trials). The size of the largest shape was sampled from a normal

distribution with a mean value that depended on screen size (7500px<sup>2</sup> for a screen with a width size  $\geq 600$ px; 6500px<sup>2</sup> for a screen with a width size  $< 600$ px and  $\geq 400$ ; 5500px<sup>2</sup> for a screen with a width size  $< 400$ px) and a standard deviation of one fourth of the mean value. The second largest shape area was set to the 0.7, 0.8, 0.9, 0.93 or 0.95 of the area of the stimulus 1, and the third alternative' area (if present), was set to the 0.1, 0.2, 0.3, 0.4, 0.5 or 0.6 of the area of the stimulus 2. Consequently, there were 60 trials with 2 alternatives (of which there were 12 trials per each size of the second largest alternative) and 60 trials with 3 alternatives (of which there were 2 trials for each combination of size of the third and second largest alternative) (Table 1). Stimuli were randomly displayed in 3 equispaced positions (120 degrees) located in a circular array of a radius that varied with the screen size. The stimuli-array was randomly rotated so the positions changed across trials. Shapes were shown for 1 s, and the participants could respond by clicking the chosen shape or, once disappeared, by clicking a small circular dot marking the position. After that, participants had to report their confidence level on the decision on a scale from 0% (not confident at all) to 100% (completely confident). Participants had to move a dot that was initially hidden (until they moved the cursor) and appeared in the cursor's position. [Specifically, in the confidence instructions we stated \(in spanish in the actual experiment\): "Once you have picked the shape that you think is the largest you will have to report your degree of confidence in that choice, that is, how sure you are that you picked the correct option" \[...\] "the scale goes from 0% \(COMPLETELY UNSURE, that implies that you don't have confidence at all in your decision of which was the largest shape\) to 100% \(COMPLETELY SURE, that implies that you are fully confident about your decision of which was the largest shape\). YOU CAN USE INTERMEDIATE VALUES, the idea is that you report your confidence in your choice in the most precise way possible". On the first 3 trials we included, on the top of the screen, the question "How sure are you?"](#).

Table 1. Task structure.

Third alternative size (area3/area2)	Second alternative size (area2/area1)				
	0.7	0.8	0.9	0.93	0.95
Absent	12 trials	12 trials	12 trials	12 trials	12 trials
0.1	2 trials	2 trials	2 trials	2 trials	2 trials
0.2	2 trials	2 trials	2 trials	2 trials	2 trials
0.3	2 trials	2 trials	2 trials	2 trials	2 trials
0.4	2 trials	2 trials	2 trials	2 trials	2 trials
0.5	2 trials	2 trials	2 trials	2 trials	2 trials

0.6	2 trials	2 trials	2 trials	2 trials	2 trials
-----	----------	----------	----------	----------	----------

### 2.1.3 Data analysis

We excluded 2 participants from subsequent analysis due to low overall performance (8 and 66% overall accuracy; the median performance for the sample was 85% with an interquartile range (Q3-Q1) of 6.7%). The definitive sample consisted of 99 participants. Our sample size was based on a pilot study with 20 participants in which we observed our main findings. We excluded trials with response times (RT) shorter than 200 ms and larger than 10 s. [These exclusion criteria were not pre-registered, but including the discarded data does not modify the results.](#) We conducted repeated measures ANOVAs and Tukey HSD post hoc tests (both with the software Statistica). Our predefined p-value for statistical significance was 0.05. We defined task difficulty as the ratio between the area of the two largest shapes. The ANOVA for incorrect trials was done with the highest levels of difficulty (0.9, 0.93, 0.95) because there were not enough incorrect trials in easier conditions (0.7 and 0.8).

## 2.2 Results

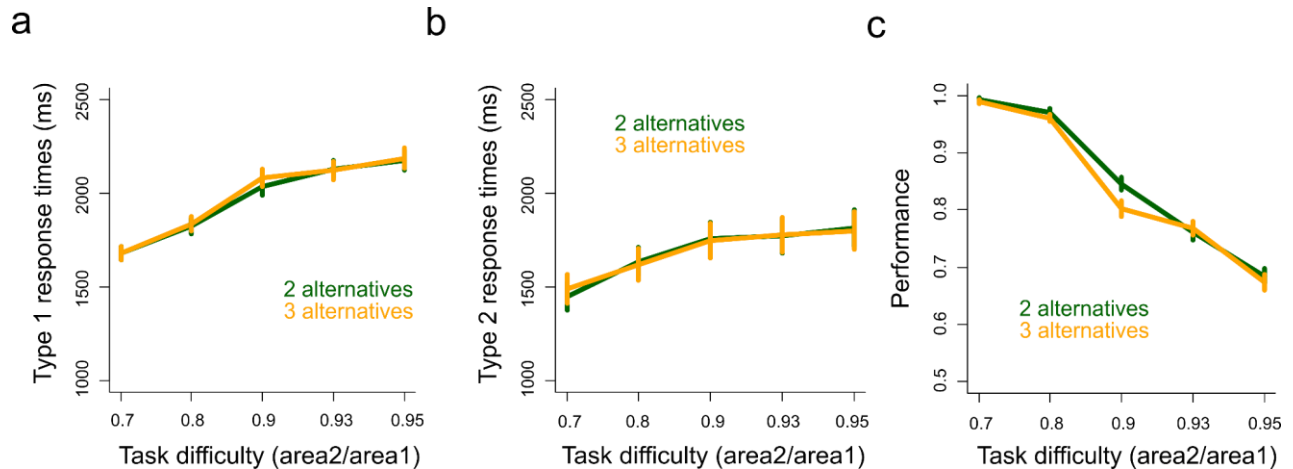
### 2.2.1 Response times

Task difficulty had a significant impact on the response times of both the [decisions](#) and the confidence reports. Higher difficulty was associated with larger RT ( $F_{4, 392} = 130.95, p < 0.000001, \eta_p^2 = 0.57$  - [decisions](#) - Fig. 2a;  $F_{4, 392} = 19.36, p < 0.000001, \eta_p^2 = 0.16$  - [confidence reports](#) - Fig. 2b). The presence of a dud alternative in half of the trials did not affect RT in none of the tasks ( $F_{1, 98} = 0.79, p = 0.37, \eta_p^2 = 0.008$  - [decisions](#) - Fig. 2a;  $F_{1, 98} = 0.002, p = 0.96, \eta_p^2 = 0.00002$  - [confidence reports](#) - Fig. 2b).

### 2.2.2 Performance

Participants' performance, as expected, decreased as task difficulty increased irrespective of the number of alternatives ( $F_{4, 392} = 374.31, p < 0.000001, \eta_p^2 = 0.79$ ) (Fig. 2c). We found a marginally significant effect of the inclusion of the third alternative on performance, restricted to the middle difficulty ( $F_{1, 98} = 4.04, p = 0.047, \eta_p^2 = 0.03$ ) (Fig. 2c). We didn't find a significant interaction between the number of alternatives and the task difficulty ( $F_{4, 392} = 1.79, p = 0.12, \eta_p^2 = 0.017$ ) (Fig. 2c).



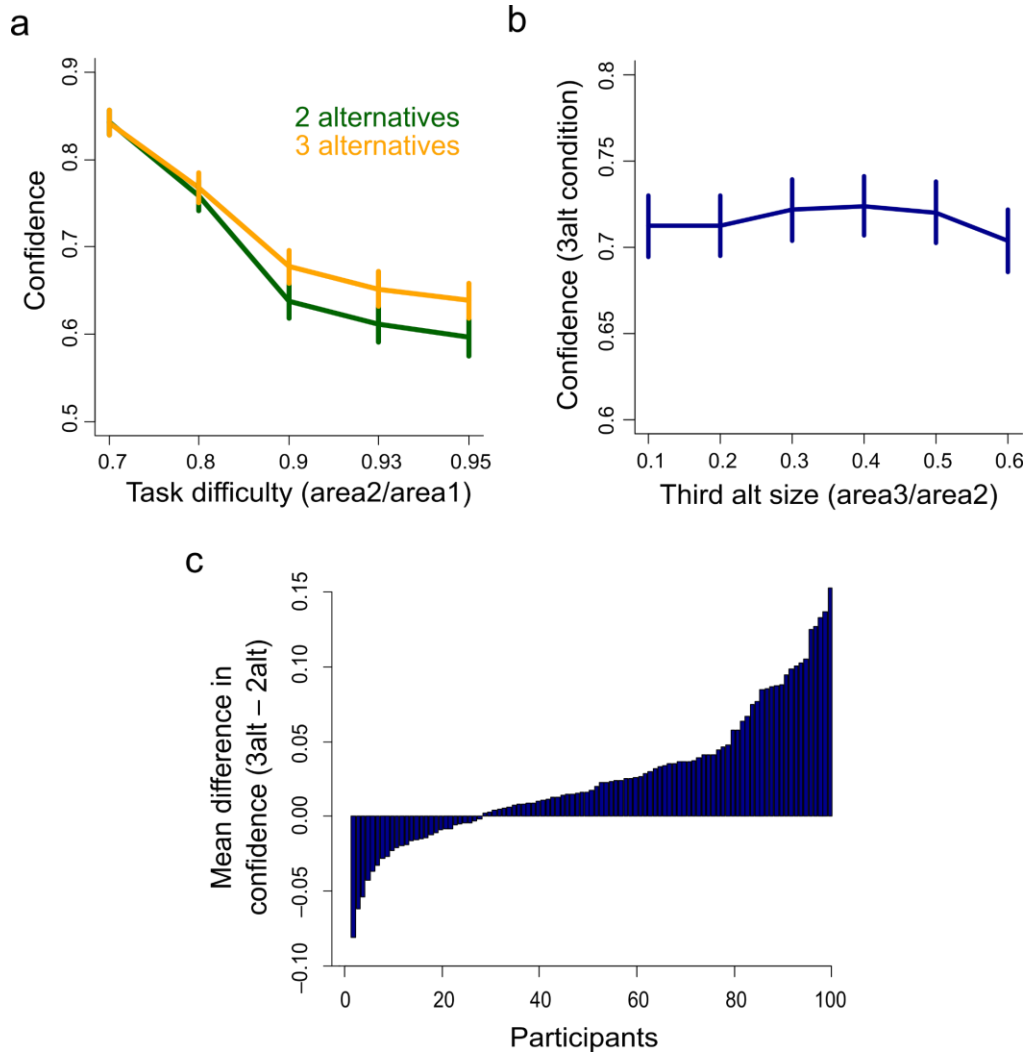


**Fig. 2.** The dud alternative did not have an effect on response times neither in (a) the decision task nor in (b) the confidence report. (c) The dud alternative only decreased task performance in difficulty 0.9. In all figures vertical bars refer to s.e.m. and “area2” and “area1” refer to the area of the second largest shape and the largest shape, respectively.

We also analyzed whether the shape of the third alternative had any effect on the decisions (i.e, a context effect regarding “square” and “circle” choices). In other words, we tested whether a squared (circled) third alternative made subjects more likely to choose a square (circle) as the largest figure. For trials where the chosen shape was a square, we found an interaction between the 2-alternative condition and the presence of the squared third alternative ( $F_{4, 392} = 3.66, p = 0.006, \eta_p^2 = 0.04$ ). When comparing between 2 or 3-alternative conditions on the same level of difficulty, a Tukey HSD post-hoc test showed a significant difference only on the highest level of difficulty ( $p = 0.02$ ). This means that participants were more likely to choose a square when the dud-alternative was also a square on that particular difficulty level. With respect to trials where the chosen shape was a circle, we again found an interaction between the 2-alternative condition and the presence of a circular third alternative ( $F_{4, 392} = 2.72, p = 0.03, \eta_p^2 = 0.03$ ). However, a Tukey HSD post-hoc test showed no significant difference between the same difficulty conditions (i.e. participants were not more likely to choose a circle if the third alternative was a circle).

### 2.2.3 Confidence

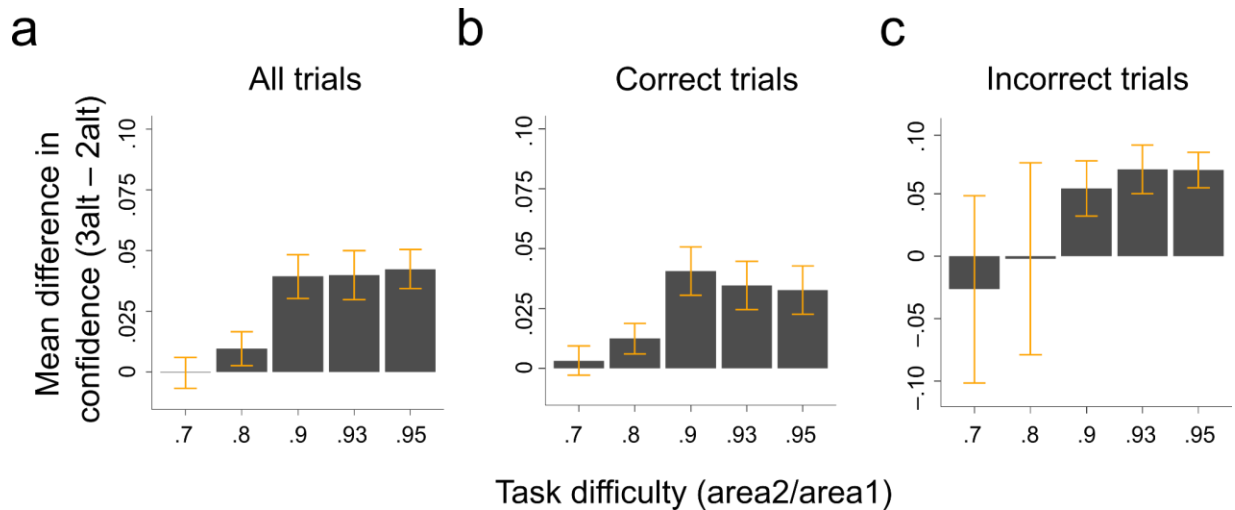
Confidence, just like performance and as expected, decreased with increasing levels of task difficulty ( $F_{4, 392} = 233.47, p < 0.000001, \eta_p^2 = 0.7$ ) (Fig. 3a). Importantly, we found a significant increment of confidence in the three-alternative condition ( $F_{1, 98} = 33.25, p < 0.000001, \eta_p^2 = 0.25$ ) (Fig. 3a and 3b). Overall, 72 out of the 99 participants had an increased confidence in the three-alternative condition (Fig. 3c) as compared with the two-alternative condition. We also found a significant interaction between the difficulty of the task and the presence of a weak alternative ( $F_{4, 392} = 6.85, p = 0.00002, \eta_p^2 = 0.06$ ) (Fig. 3a).



**Fig. 3.** (a) Confidence diminishes as a function of task difficulty but decreases less when a dud alternative is present (specifically at high levels of difficulty). (b) No effect was found regarding the size of the irrelevant alternative on confidence (i.e., confidence increased equally irrespectively of the third stimuli size). (c) Difference in confidence (2 vs 3 alternatives) per participant. Each line in (b) represents the change in confidence for each participant (considering all difficulty levels for each condition). A positive value means that confidence was higher when the dud alternative was present, whereas a negative value means that, conversely, confidence decreased in that condition.

The effect of increased confidence is present both in correct and incorrect trials ( $F_{1, 98} = 26.65$ ,  $p = 0.000001$ ,  $\eta_p^2 = 0.21$  - correct trials;  $F_{1, 61} = 22.2$ ,  $p = 0.00001$ ,  $\eta_p^2 = 0.27$  - incorrect trials) (Fig. 4). Comparing the confidence increment between correct and incorrect trials (on the 3 highest levels of difficulty) no differences were found ( $F_{1, 61} = 3.82$ ,  $p < 0.055$ ,  $\eta_p^2 = 0.06$ ). Regarding the size of the third alternative, we found a significant effect ( $F_{6, 582} = 4.73$ ,  $p = 0.0001$ ,  $\eta_p^2 = 0.05$ ). A Tukey HSD post hoc test showed that the significant differences were between the 2 alternative condition and the conditions where the size of the dud alternative was 0.07 ( $p = 0.048$ ), 0.21 ( $p = 0.0007$ ), 0.28 ( $p = 0.005$ ) and 0.35 ( $p = 0.001$ ) of the area of the largest stimulus. This means that no

differences were found across the third stimulus sizes (all differences are with respect to the 2 alternative condition). In other words, confidence increased irrespectively of the size of the dud-alternative (Fig. 3b).



**Fig. 4.** Confidence increases when the third alternative is present. All panels depict the confidence difference between 3-alternative and 2-alternative conditions. The figure shows confidence difference for (a) all trials, (b) correct trials and (c) incorrect trials. Large s.e.m. in (c) at low difficulties (difficulties 0.7 and 0.8) are due to low numbers of incorrect responses.

We did not find an effect of the shape of the third alternative on confidence. That is, when considering if the dud alternative was a circle or a square only on the 3-alternative condition, no difference was found in confidence neither for trials where the chosen shape was a circle ( $F_{1, 63} = 0.16$ ,  $p = 0.69$ ,  $\eta_p^2 = 0.003$ ) nor for trials where the chosen shape was a square ( $F_{1, 83} = 1.69$ ,  $p = 0.2$ ,  $\eta_p^2 = 0.02$ ).

## 2.3 Discussion

The results of Experiment 1 extend the “dud-alternative” effect to a perceptual decision making task: confidence level increased with the addition of a small, clearly incorrect alternative. This effect is remarkably important because it implies that confidence does not directly reflect the probability of being correct, as stated by classical views (Meyniel et al., 2015; Sanders et al., 2016), and even deviates from recent models such as the difference of the probabilities of being correct of the two best options (H.-H. Li & Ma, 2020). According to these models, the addition of irrelevant alternatives should not affect confidence (because they hardly affect the probabilities of the rest of the alternatives), and, in any case, it should decrease it. However, the opposite pattern is observed in Experiment 1.

The dud-alternative had a small effect on performance. The effect is only restricted to a middle-level difficulty, where participants’ performance only decreased minimally. So it is

likely that the task was not more difficult with the addition of the third alternative. The lack of effect in response times is consistent with this explanation, as more difficult tasks are expected to generate larger response times (Ratcliff et al., 2016). In consequence, the effect of the inclusion of the irrelevant alternative is mainly restricted to confidence.

The design of Experiment 1 allows for the possibility of testing a specific kind of “decoy effect”: the probability of choosing a geometrical shape as the largest one increases when the third alternative is of the same shape (Huber et al., 1982; Trueblood et al., 2013). However, we only found this effect for square choices, restricted to the highest level of difficulty. Moreover, this effect did not interact with the dud-alternative effect, suggesting that both are independent contextual effects.

Studies focused on the dud-alternative effect propose two main accounts for this phenomenon (Charman et al., 2011; Hanczakowski et al., 2014; Windschitl & Chambers, 2004). The first one is the “Average-residual” account: confidence reflects the difference between the evidence supporting the chosen option and the average of the evidence supporting the unchosen options (Eq. 3, see below). According to this idea, confidence increases with the addition of a dud alternative because its presence decreases the average of the evidence in favor of the unchosen options. The second proposed explanation for the dud effect is the “Contrast” account: confidence is obtained by a series of pairwise comparisons, where observers take the differences between the evidence supporting the chosen alternative and the evidence supporting each of the rest of the alternatives and sum them up (Eq. 4, see below). Confidence therefore increases with the presence of an irrelevant alternative, since there is another favorable comparison for the chosen option. We decided to formalize and test these verbal explanations in two computational models: the “Average-residual” model and the “Contrast” model. We compared these two models with the “Max” model –that states that confidence reflects the probability of being correct (Eq. 2, see below)– (H.-H. Li & Ma, 2020; Meyniel et al., 2015; Sanders et al., 2016) and the Difference model –that states that confidence reflects the difference between the probabilities of being correct of the two best alternatives (Eq. 1, see below)– (H.-H. Li & Ma, 2020).

### **3. Computational models**

In order to evaluate whether the predictions of different models of confidence could fit our empirical results of Experiment 1 —and to propose some venues for future models— we carried out simulations for 4 models: the Difference model (H.-H. Li & Ma, 2020), the Max model (H.-H. Li & Ma, 2020; Meyniel et al., 2015; Sanders et al., 2016), the Contrast model (Charman et al., 2011; Hanczakowski et al., 2014; Windschitl & Chambers, 2004)

and the Average-residual model (Charman et al., 2011; Hanczakowski et al., 2014; Windschitl & Chambers, 2004).

### 3.1 Materials & methods

#### 3.1.1 Computational modeling.

All models were developed under a Bayesian modeling approach (Ma, 2019). To set the generative model, we defined stimuli sizes as in Exp. 1. We simulated the internal responses on each trial. We assumed that observers make a noisy measurement  $x_i$  of each stimulus  $S_i$ . This measurement was modeled using a Gaussian distribution with mean on the actual value of the stimuli and standard deviation  $\sigma$ . Ideal observers compute the posterior probability that each stimuli is the largest, formally:  $p_i = p(S_i = \max(S_1, S_2, S_3) | (x_1, x_2, x_3, s))$ . As some variability in behavior is due to a “late noise” at the level of the decision variable (H.-H. Li & Ma, 2020), we assumed that observers do not maintain the exact posterior probability but a noisy version of it,  $q_i$ , modeled as a random sample of a Dirichlet distribution centered on the true posterior probabilities with a spread controlled by a parameter  $\alpha$  (H.-H. Li & Ma, 2020). We assumed participants choose the stimulus with the highest  $q(S_i | x_1, x_2, x_3, s)$ . For readability, from now on we will refer to these noisy posterior probabilities as simply the posterior probabilities.

We simulated confidence levels according to four different models (Fig. 5a). For the Difference model (Diff), confidence level is the result of the difference between the two highest posterior probabilities. In the Max model confidence level is the larger posterior probability. This model corresponds to the Bayesian Confidence hypothesis, stating that confidence reflects the probability that the decision is correct. The Contrast model and the Average-residual model are computational implementations of the two mechanisms proposed in the dud alternative literature to account for the effect (Charman et al., 2011; Windschitl & Chambers, 2004). The Contrast model states that confidence is obtained by a series of pairwise comparisons between the chosen option and the remaining. Following this, we modeled confidence by the sum of the differences between the largest posterior probability and all other posterior probabilities. The Average-residual model proposes that confidence reflects the evidence favoring the chosen option minus the average evidence of the remaining options. Therefore, we modeled confidence as the difference between the alternative with the highest posterior probability and the mean of the remaining posterior probabilities. Formally:

$$\text{Diff model: } \textit{confidence} = q_1 - q_2 \quad (\text{Eq. 1})$$

$$\text{Max model: } \textit{confidence} = q_1 \quad (\text{Eq. 2})$$

$$\text{Average-residual model: } \textit{confidence} = q_1 - \frac{(q_2 + q_3)}{2} \quad (\text{Eq. 3})$$

$$\text{Contrast Model: } \textit{confidence} = (q_1 - q_2) + (q_1 - q_3) \quad (\text{Eq. 4})$$

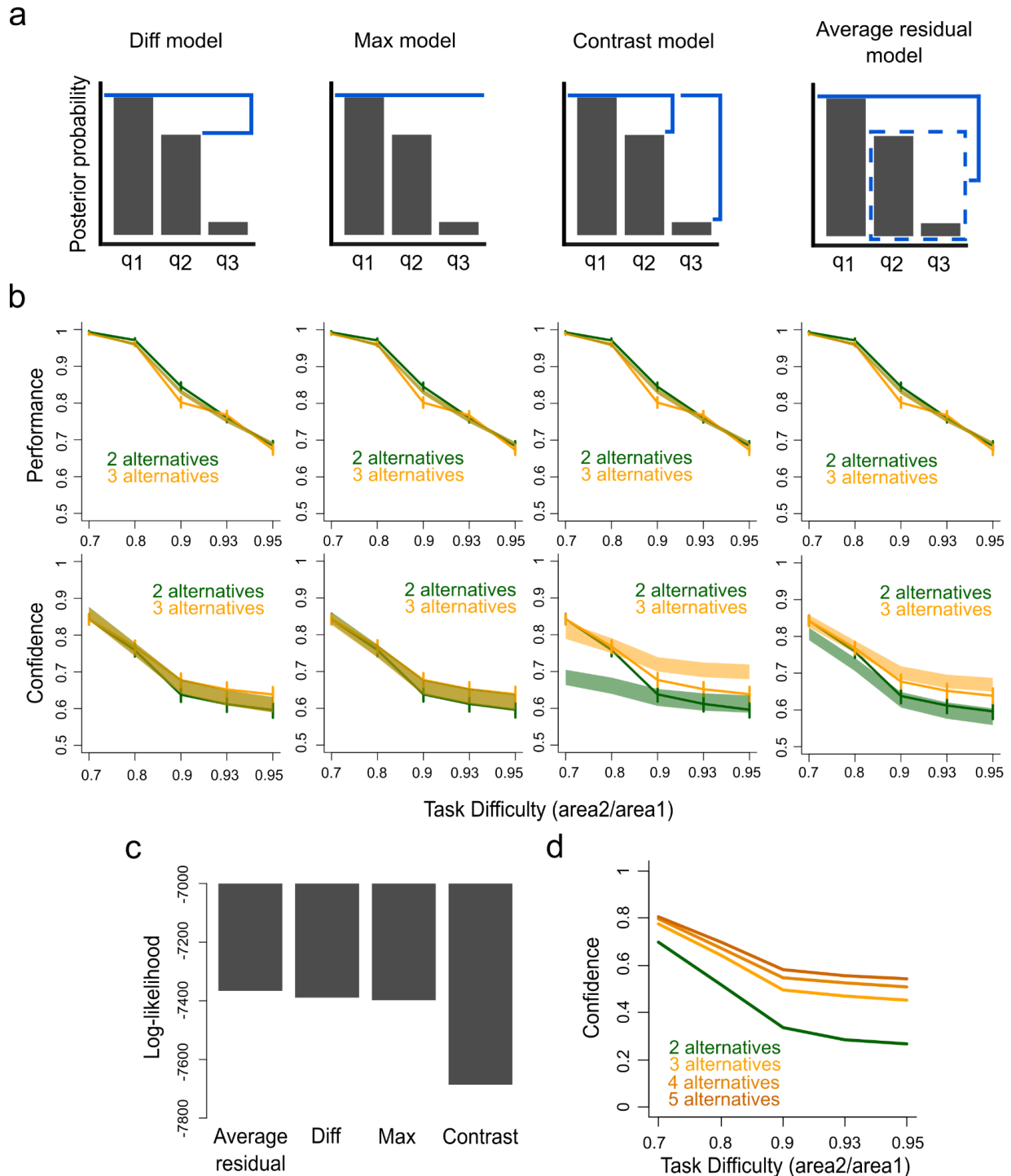
### 3.1.2 Model fitting

We fitted the models' free parameters separately for each participant's data (decisions and confidence) by maximizing the likelihood of the parameters. Formally, we maximized  $L(\theta|data) = \log p(data | \theta)$ , where  $L(\theta|data)$  is the log-likelihood of the parameters given the data,  $data$  is the decisions and the mean confidence level on each condition, and  $\theta$  the parameters ( $\sigma, \alpha, \beta_0$  and  $\beta_1$ ). The free parameters were sensory noise ( $\sigma$ ), decision noise ( $\alpha$ ) and two parameters controlling the intercept ( $\beta_0$ ) and slope ( $\beta_1$ ) of the linear transformation that maps the confidence output of the model to the confidence data of the subject (using alternative mappings does not change the computational modeling results, see Supplementary material). We first fitted  $\sigma$  and  $\alpha$  using the participant's decisions and then used these two parameters as fixed to fit confidence levels. For that, we simulated 10000 trials and calculated the proportion of trials where the model decision is equal to the decision of the participant. These numbers (one per trial) are an approximation of the data probability given the parameter values. We summed the log of these numbers, thus computing the log-likelihood of the parameters given the observed data. To find the best fitting parameter values we used the R function *optim* with the simulated annealing method to minimize the negative log-likelihood of the parameters' values given the observed data (which is equivalent to maximizing the likelihood of the parameters' values given the observed data). We then used the best  $\sigma$  and  $\alpha$  values as fixed values for fitting  $\beta_0$  and  $\beta_1$ . We simulated 100000 trials per model taking the mean confidence by 1000 trials. Confidence data was divided by 100 to transform it to the scale of 0 to 1 and then rounded to 1 decimal. We fitted the model to the mean confidence level on each condition for each participant (fitting the whole trial distribution instead of the mean level did not qualitatively change our results, see Supplementary material). To fit confidence, we ran three optimization realizations with different starting points of the parameters, and kept the best estimation. Using the resulting parameters values we simulated 100000 trials according to each model taking the mean confidence by 1000 trials and calculated their mean performance and confidence to compare these models' predictions to the participants' behavior. As all the models have the same number of free parameters we directly compared them using the summed log-likelihood across participants.

To evaluate the ability of our method to detect the true parameters for each subject, we performed parameter recovery by simulating, with the Average-residual model, the same amount of data that we had by participant (120 trials; 12 per condition) using values of  $\sigma, \alpha, \beta_0$  and  $\beta_1$  sampled from our data and then fitting models to this simulated data with the mentioned procedure. The Pearson correlation between the true parameters and the estimated parameters was 0.83 for  $\sigma$  ( $p < 0.0001$ ), 0.58 for  $\alpha$  ( $p < 0.0001$ ), 0.99 for  $\beta_0$  ( $p < 0.0001$ ) and 0.99 for  $\beta_1$  ( $p < 0.0001$ ). This suggests that our method successfully recovers the true parameters underlying each participant data.

### 3.2 Results

For both the Max model (summed log-likelihood = -7398.2) and the Diff model (summed log-likelihood = -7389) the presence of a third irrelevant option does not affect confidence (Fig. 5b). In contrast, for both the Contrast model (summed log-likelihood = -7686.03) and the Average-residual model (summed log-likelihood = -7365.97) confidence increases with the presence of an irrelevant option (Fig. 5b). However, the Contrast model shows a constant (difficulty-independent) confidence increase, whereas the Average-residual model accounts for the pattern shown in our data: the difference in confidence between three and two alternatives increases with the difficulty. Furthermore, if we extend simulations to a context with more dud alternatives, the Average-residual model predicts that confidence should increase monotonically with the number of dud alternatives (Fig. 5d).



**Fig. 5.** (a) Sketches of confidence computation for each model. In the Average residual Model, confidence is obtained by the difference between the highest posterior probability and the mean of the remaining posterior probabilities. Confidence reflects the probability of being correct in the Max Model. The Difference Model states that confidence reflects the difference between the two best posterior probabilities. Finally, in the Contrast Model confidence is the result of the sum of the differences between the highest posterior probability and each of the remaining posterior probabilities. (b) Model fits for performance (first row) and confidence (second row). Both the max model and the Diff model show that



confidence should remain invariant when a dud-alternative is added to the decision context. Conversely, the Average-residual model and the Contrast model show that confidence should be higher. However, only the Average-residual model replicates the pattern found in our experiment. Shaded regions are the standard error of the mean of model fits. (c) The log-likelihood of each model. The Average-residual model is the best fitting model regarding our data. (d) The Average-residual model predicts that confidence should increase with the number of dud alternatives, as these alternatives reduce even more the average of the remaining options.

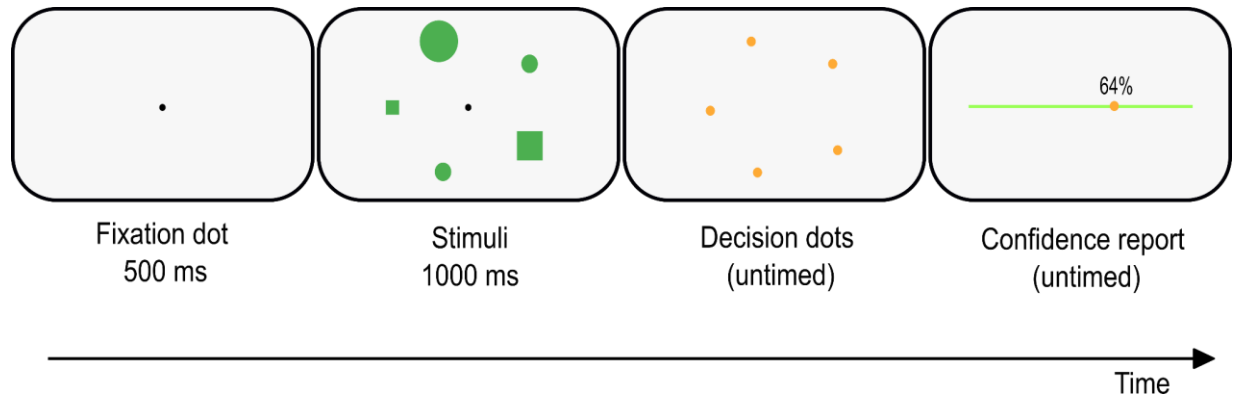
### **3.3 Discussion**

Among all tested models, both the Average-residual model and the Contrast model can recover the increment in confidence in the 3-alternative condition. However, only the Average-residual predicts a lower effect on easier trials. Contrary, both the Max model and the Diff model predict the opposite pattern: confidence remains the same when more alternatives are added into the decision context.

The Average-residual model predicts that confidence should be higher with more alternatives only when these alternatives are dud-alternatives, i.e. when the probability of these alternatives of being correct is close to zero (according to the model, if the extra alternatives are not dud-alternatives they will decrease the probability of being correct of the chosen option and then confidence will be lower than in 2-alternative case, see Supplementary Fig. 3a). This is because, with the addition of irrelevant alternatives, the probabilities of being correct of the competitive options remain the same while the average of the remaining options is lower. As a consequence, the model predicts that confidence increases monotonically with the number of dud-alternatives, since these alternatives progressively lower the average of the probabilities of being correct of the unchosen options (Supplementary Fig. 3b). We tested for this possibility in the next experiment.

## **4. Experiment 2**

The Average-residual model predicts that confidence should increase monotonically with the number of dud-alternatives, because the presence of more irrelevant alternatives decreases the average of posterior probabilities of non-chosen alternatives with a minimal effect on the posterior probabilities of the competing alternatives (Fig. 5d). In this second experiment we not only aimed to replicate the results of Experiment 1 but to see whether confidence increases with the number of dud alternatives (Fig. 6).



**Fig. 6.** Size discrimination task. Participants had to decide which one of the shapes was the largest. Stimuli size varied in every trial, and the relative sizes of the two largest shapes controlled the difficulty (established in 5 levels). There were 4 conditions: 2, 3, 4 and 5 alternatives, each one with 120 trials. After that decision, participants had to report their confidence level on a scale from 0% (not confident at all) to 100% (completely confident). Only two alternatives competed for the correct answer, the others (when present) were relatively small and easily discarded.

## 4.1 Materials & methods

As in Experiment 1, the task was programmed in JavaScript using the library jQuery and conducted online on a JATOS (Lange et al., 2015) server. Experiment 2 involved more experimental conditions and, thus, more trials. To guarantee participants' attention during the task, the experimenter made a video call and remained available for the duration of the experiment.

### 4.1.1 Participants

18 participants took part in this experiment (62% females; mean age = 27.17, sd = 4.77). The study was approved by the ethical committee of the Institute of Psychological Research (IIPsi - CONICET - Córdoba, Argentina). Participants should read and accept an informed consent prior to the realization of the experiment. All participants reported no psychiatric, illegal drug consumption or neurological history. The tasks' instructions were written on screen prior to the experiments. All participants performed the task on a computer. Each participant received a payment of roughly 4 US dollars.

### 4.1.2 Experimental design

The design of Experiment 2 was similar to that of Experiment 1 but involving a larger number of conditions: 480 trials including 120 trials of 2, 3, 4 or 5 alternatives. As in Experiment 1, only two alternatives were large enough to compete for the correct answer; the others were much smaller in order to make them easily discarded (irrelevant alternatives). In trials where the irrelevant alternatives were present, they all had the same size, and each one was randomly a square or a circle. These dud alternatives also varied

in size (as in Experiment 1). Participants had to report their confidence level in the decision in the same way as in Experiment 1.

#### 4.1.3 Data analysis

No subject was excluded from the analysis. We followed a similar analysis strategy than in Exp 1 (including the excluded trials does not modify the results). We excluded the easiest level of the task from the performance analysis because one category (the one with 5 alternatives) had perfect performance. The dissociation between correct and incorrect trials carried out in Experiment 1 was not possible because there were not enough incorrect trials.

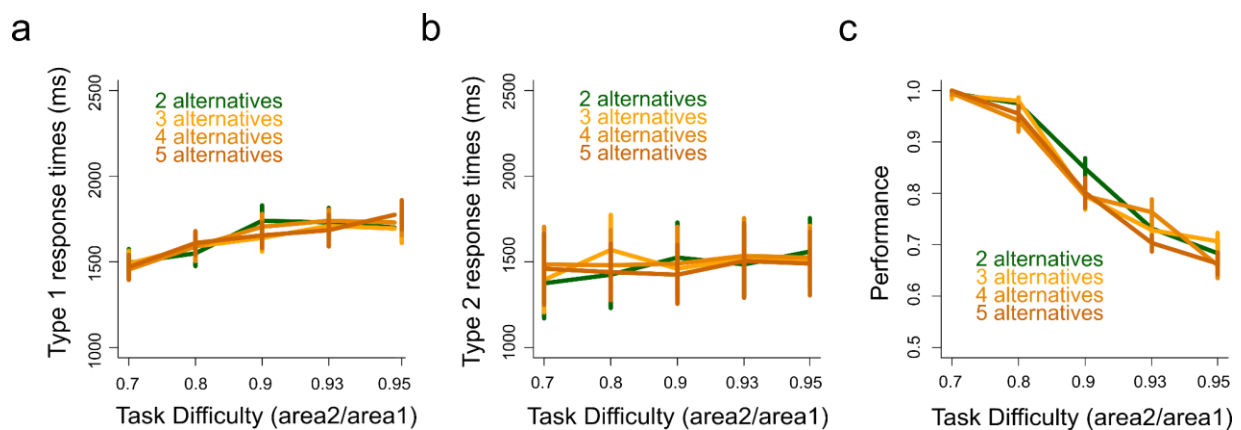
## 4.2 Results

### 4.2.1 Response times

**Decisions** RT increased with difficulty ( $F_{4, 68} = 23.47$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.58$ ) (Fig. 7a). This effect was not found in **confidence reports** RT ( $F_{4, 68} = 1.59$ ,  $p = 0.18$ ,  $\eta_p^2 = 0.08$ ) (Fig. 7b). The weak alternatives did not impact the RT on either of the tasks ( $F_{3, 51} = 0.26$ ,  $p = 0.84$ ,  $\eta_p^2 = 0.01$  - **decisions** - Fig. 7a;  $F_{3, 51} = 0.57$ ,  $p = 0.63$ ,  $\eta_p^2 = 0.03$  - **confidence report** - Fig. 7b).

### 4.2.2 Performance

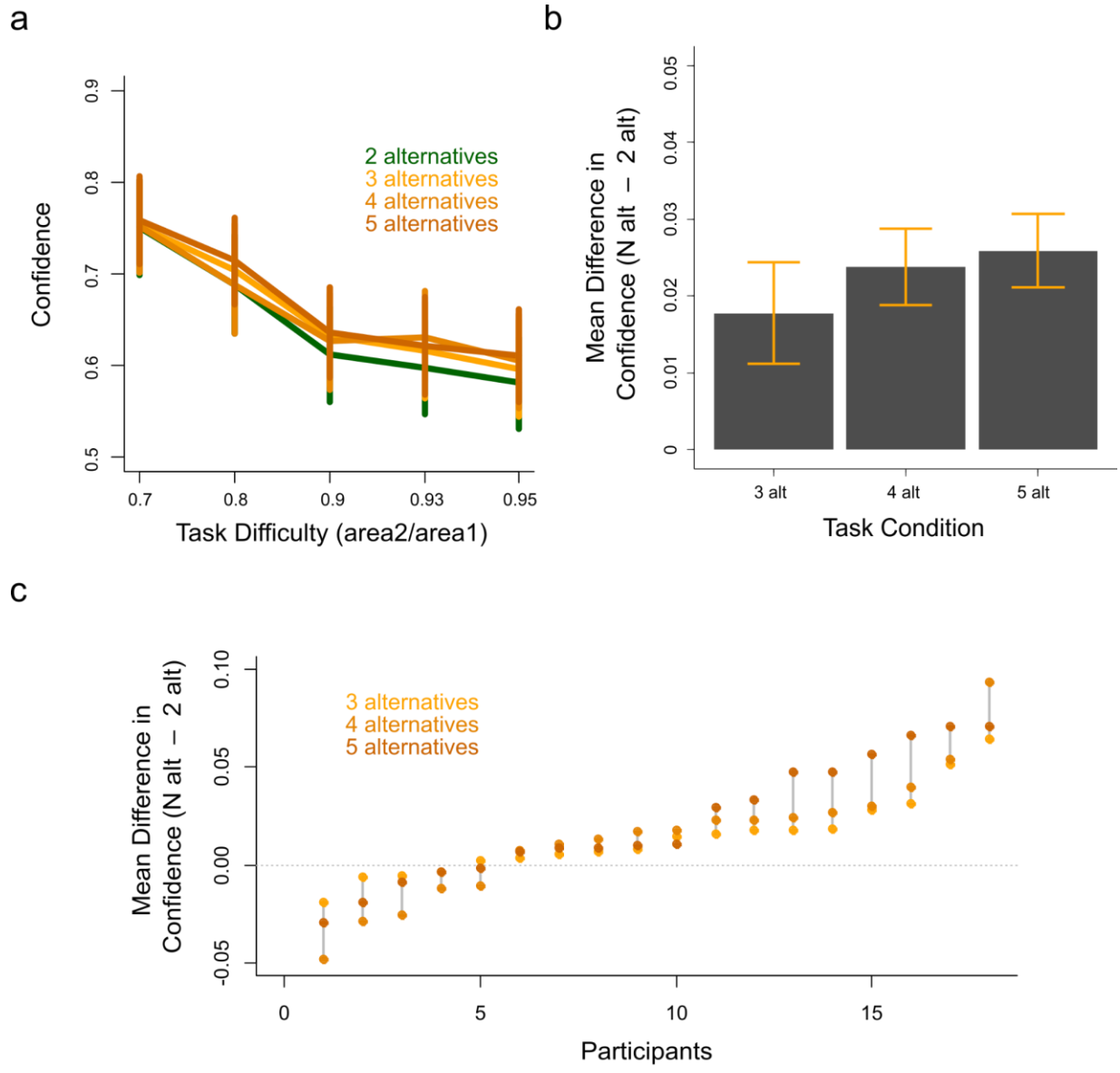
Regarding task performance, participants' accuracy decreased as the difficulty increased ( $F_{3, 51} = 90.45$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.84$ ) (Fig. 7c). Contrary, the dud alternatives did not affect participants' performance ( $F_{3, 51} = 2.62$ ,  $p = 0.06$ ,  $\eta_p^2 = 0.13$ ) (Fig. 7c).



**Fig. 7.** As in Experiment 1, dud alternatives did not have an effect in RT, neither in (a) decisions or in (b) confidence reports. (c) Performance did not vary with the addition of dud alternatives.

### 4.2.3 Confidence

Confidence level decreased with task difficulty ( $F_{4, 68} = 54.63, p < 0.000001, \eta_p^2 = 0.76$ ) (Fig. 8a). Replicating the main finding in Experiment 1 confidence increased with the presence of irrelevant alternatives ( $F_{3, 51} = 3.81, p = 0.01, \eta_p^2 = 0.18$ ) (Fig. 8a). We conducted a Tukey HSD post hoc analysis, showing that there was a significant difference between confidence with 2 and 5 alternatives ( $p = 0.008$ ). To further explore this result, we conducted ANOVAs separately for each remaining conditions (3 and 4 alternatives vs 2 alternatives). We found a significant effect on confidence for the 3-alternative condition ( $F_{1, 17} = 9.06, p = 0.007, \eta_p^2 = 0.34$ ) not detected by the post hoc test. No interaction was found on this condition ( $F_{4, 68} = 0.5, p = 0.72, \eta_p^2 = 0.03$ ). For the condition with 4 alternatives we found a marginally significant effect ( $F_{1, 17} = 3.58, p = 0.075, \eta_p^2 = 0.17$ ) and a significant interaction between the amount of alternatives and the task difficulty ( $F_{4, 68} = 2.61, p = 0.04, \eta_p^2 = 0.13$ ). We did not replicate the interaction between difficulty and the irrelevant alternatives found in Experiment 1 ( $F_{12, 204} = 1.13, p = 0.33, \eta_p^2 = 0.06$ ) (Fig. 8a). Confidence was not affected by the number of dud-alternatives ( $F_{2, 34} = 0.95, p = 0.39, \eta_p^2 = 0.05$ ) (Fig. 8a and Fig. 8b). Thirteen out of eighteen participants showed the effect of increased confidence in the dud alternative conditions (Fig. 8c). There was a significant effect of the dud alternative size on confidence ( $F_{6, 102} = 2.49, p = 0.03, \eta_p^2 = 0.13$ ).



**Fig. 8.** (a) As in Experiment 1, confidence decreased with task difficulty but increased when weak alternatives were present. (b) Confidence difference between the 3, 4 and 5 alternative conditions and 2-alternative condition considering the highest levels of difficulty (0.9, 0.93 and 0.95). (c) Average difference in confidence by condition and participant.

### 4.3 Discussion

In Experiment 2 we replicated the dud-alternative effect found in Experiment 1. However, we did not find evidence that adding more dud-alternatives influences confidence. Although this constitutes a challenge for the Average-residual model, one should keep in mind that the prediction of the model is that the increase in confidence becomes smaller with the addition of each dud alternative (because the average of the probabilities of the non-chosen options start to decrease less with each added alternative), making this

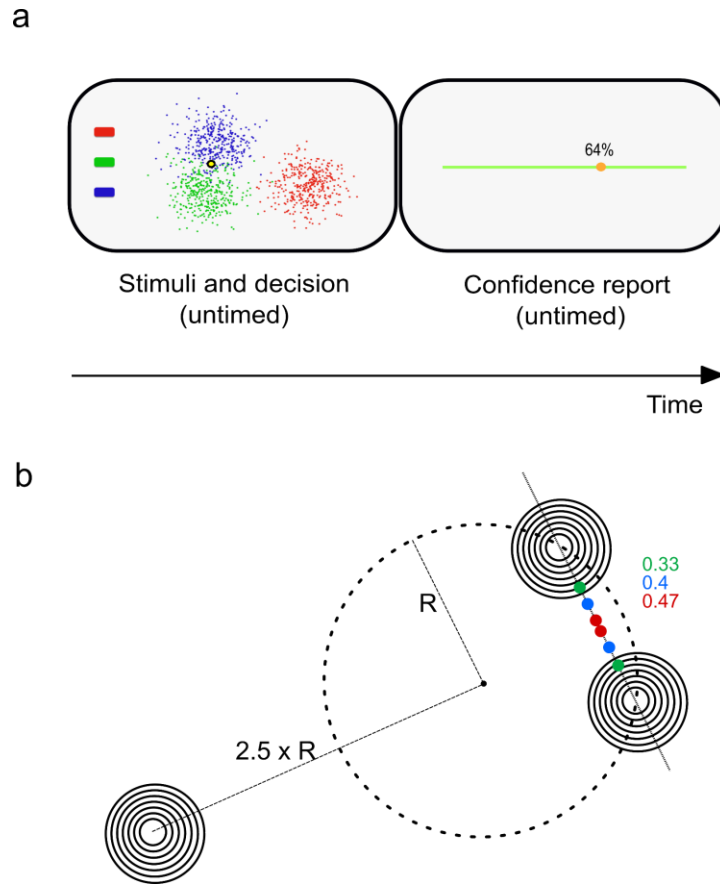
effect, if it exists, much difficult to detect. Moreover, with higher levels of sensory or decision noise the model predicts no difference between conditions. Further research is needed to evaluate if the monotonic increase in confidence actually exists and if the Average-residual model can account for its presence or absence by fitting it to participants' behavior.

Interestingly, performance was not affected by the inclusion of the dud-alternatives. This confirms the notion that these alternatives are not making the task harder (despite the small but significant effect on performance found in Experiment 1).

We extended the dud-alternative effect to a perceptual decision making task in Experiments 1 and 2. However, we wanted to test if this effect was present in a different task, the one where the Diff model was developed (H.-H. Li & Ma, 2020), to evaluate whether the predictions of the Average-residual model hold even in the context where the Diff model was the best model. Therefore, we run Experiment 3.

## **5. Experiment 3**

To evaluate whether the dud-alternative effect replicates in a different multi-alternative task, we adapted the target categorization task from Li & Ma (2020) (Fig. 9).



**Fig. 9.** Target categorization task. (a) Participants decided which cloud of dots the yellow target dot belonged to. Half of the trials had three alternatives and half two. When present, the third cloud was far from the target in order to make it ineligible, following the logic of the previous two studies (red cloud in the figure). After the decision, participants reported their confidence level on a continuous bar. (b) The underlying structure of the task (see Materials & methods).

## 5.1 Materials & methods

As the two previous experiments, the third experiment was conducted online on JATOS (Lange et al., 2015) and programmed in JavaScript using the library jQuery.

### 5.1.1 Participants

63 participants took part in this experiment (62.5% females; mean age = 30.16, sd = 12.32). The study was approved by the ethical committee of the Institute of Psychological Research (IIPsi - CONICET - Córdoba, Argentina). Participants should read and accept an informed consent prior to the realization of the experiment. All participants reported no psychiatric, illegal drug consumption or neurological history. The tasks' instructions were written on screen prior to the experiment. All participants completed the experiment on a computer.

### 5.1.2 Experimental design

The experiment consisted of a decision making task where participants had to decide which cloud of dots a target dot belonged to. It had 120 trials, 60 with two alternatives and 60 with three alternatives (i.e., two or three clouds). Dots were normally distributed in space. The mean of the distributions were set in space such that the two main clouds were closer together. More specifically, the mean of these distributions were located in a circle of radius  $R$  centered at a fixation point and separated by an angle of 120 degrees. In trials where the third cloud was present, its mean was located at a distance  $2.5 \times R$  from the fixation point and at an angle of 120 degrees from each of the mean locations of the other two clouds. Each dot cloud had 375 dots. Dot size and standard deviation of the distribution was responsively set, according to the presentation screen. The target dot was yellow with a black border. The target was located in a segment that begins and ends at the mean values of the 2 competing clouds distributions. The position of the target was parameterized by a “task difficulty” variable  $d$  that takes values from 0 to 0.5, where 0 represents one of the extremes and 0.5 represents the middle, equidistant from the mean values of the distributions. We used  $d = \{0.33, 0.4, 0.47\}$  where 0.33 is the easiest and 0.47 the most difficult condition. See Fig. 9b for a graphical reference of the task. Stimuli remained on the screen until the participant made a decision, clicking on color coded screen buttons. Participants reported their confidence level on the decision on a continuous scale, as in Experiments 1 and 2. [Similar to Experiments 1 and 2, the confidence instructions stated \(spanish in the actual experiment\): “your second task consists in reporting your degree of confidence in your choice, that is, how sure you are to have picked the correct option” \[...\] “the scale ranges from 0% \(COMPLETELY UNSURE, that implies that you don’t have confidence at all in your decision to which cloud of dots did the yellow dot belonged to\) to 100% \(COMPLETELY SURE, that implies that you are fully confident about your decision to which cloud of dots did the yellow dot belonged to\). YOU CAN USE INTERMEDIATE VALUES, the idea is that you report your confidence in your choice in the most precise way possible”.](#) On the first 3 trials we included, on the top of the screen, the question “How sure are you?”.

### 5.1.3 Data analysis

We excluded 7 participants from the analysis (3 due to low performance -our accuracy cutoff point was an accuracy of 0.6-, and 4 due to lack of variability in the confidence report (confidence level at 100% in > 90% of the trials). The final sample consisted of 52 participants (including all participants does not modify the results). We excluded trials with RT lower than 200ms both for [decisions](#) and [confidence reports](#). We excluded trials with a response time greater than 20 s instead of 10 s as in our previous tasks since RTs are larger in this task. [These exclusion criteria were not pre-registered, but including the discarded data does not modify the results.](#) We conducted repeated measures ANOVAs and Tukey HSD post hoc tests (both with the Statistica software) to estimate the impact



of the difficulty of the task and the dud alternatives in RT, performance and confidence. Our predefined p-value for statistical significance was 0.05.

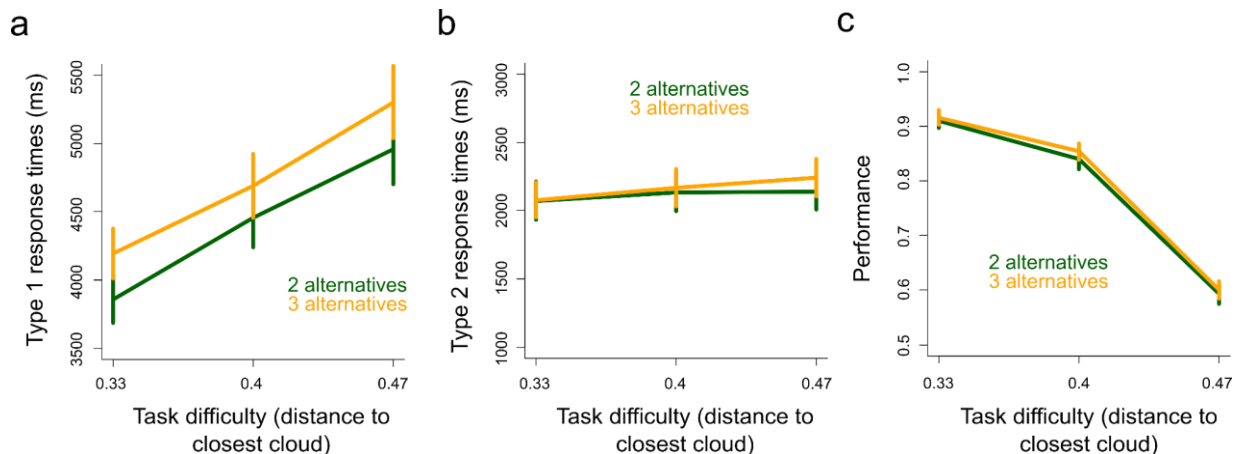
## 5.2 Results

### 5.2.1 Response times

Task difficulty had a significant effect on **decisions** RT ( $F_{2, 102} = 34.40$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.40$ ) (Fig. 11a). RT were also larger for the 3-alternative condition ( $F_{1, 51} = 14.38$ ,  $p = 0.0004$ ,  $\eta_p^2 = 0.22$ ) (Fig. 10a). No interaction was found between the number of alternatives and task difficulty ( $F_{2, 102} = 0.26$ ,  $p = 0.77$ ,  $\eta_p^2 = 0.005$ ) (Fig. 10a). Task difficulty affected **confidence reports** RT ( $F_{2, 102} = 3.63$ ,  $p = 0.03$ ,  $\eta_p^2 = 0.07$ ). The number of alternatives did not impact **confidence reports** RT ( $F_{1, 51} = 3.20$ ,  $p = 0.08$ ,  $\eta_p^2 = 0.059$ ). No interaction was found between task difficulty and the number of alternatives ( $F_{2, 102} = 1.01$ ,  $p = 0.37$ ,  $\eta_p^2 = 0.02$ ).

### 5.2.2 Performance

Performance, as expected, decreased as the task became more difficult ( $F_{2, 102} = 418.85$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.89$ ) (Fig. 10c). The presence of a third alternative did not have an effect on performance ( $F_{1, 51} = 0.78$ ,  $p = 0.38$ ,  $\eta_p^2 = 0.015$ ) (Fig. 10c).

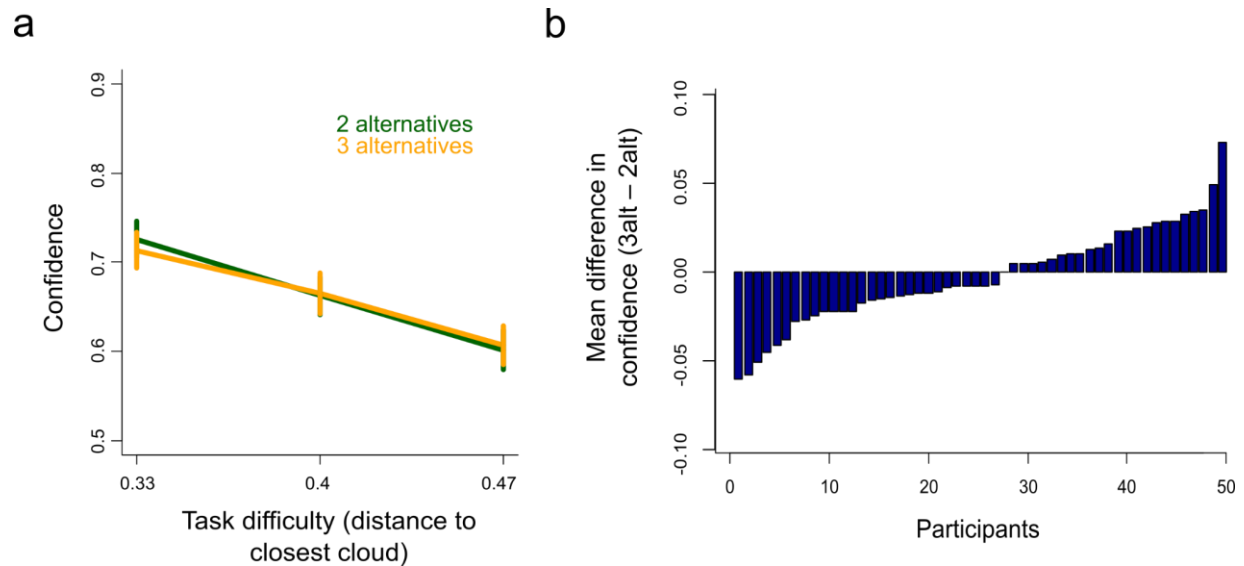


**Fig. 10.** (a) Both task difficulty and the presence of the dud alternative increased response times in the decisions. (b) Contrary to decisions, response times for the confidence report were not affected neither by task difficulty nor the amount of alternatives. (c) Performance decreased as the task difficulty increased, whereas the dud alternative did not affect it.

### 5.2.3 Confidence

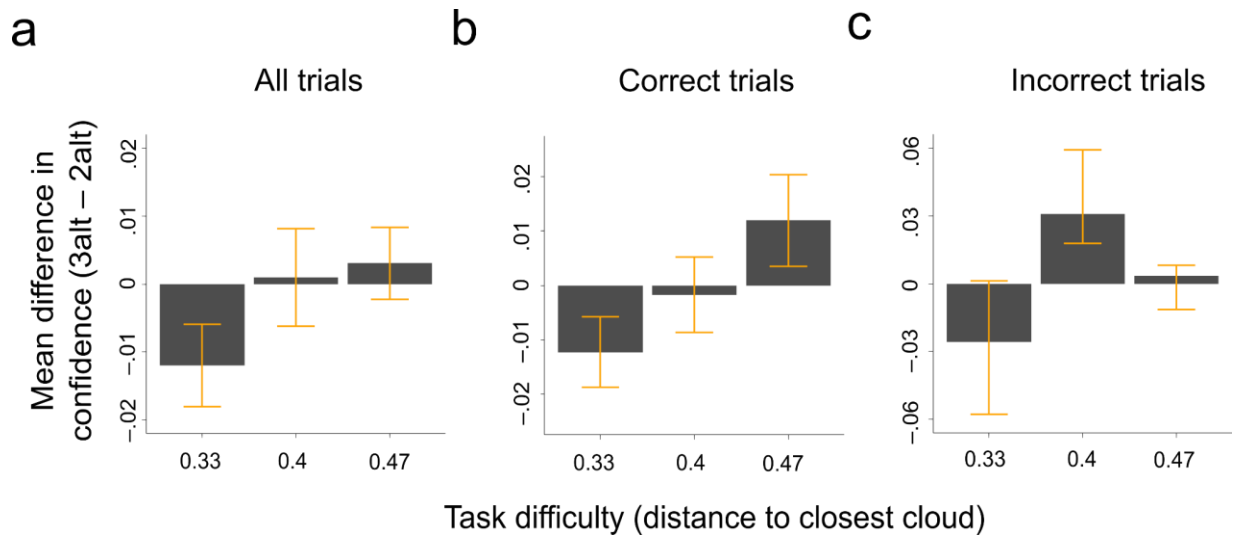
Confidence, as expected and in line with performance, decreased when the task got more difficult ( $F_{2, 102} = 97.59$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.66$ ) (Fig. 11a). In contrast with the results from Experiments 1 and 2, we did not find evidence for higher confidence in the 3-

alternative condition ( $F_{1, 51} = 0.485$ ,  $p = 0.49$ ,  $\eta_p^2 = 0.009$ ) (Fig. 11b) and there was not an interaction between the number of alternatives and task difficulty ( $F_{2, 102} = 1.84$ ,  $p < 0.16$ ,  $\eta_p^2 = 0.035$ ).



**Fig. 11.** Effect of number of alternatives on confidence. (a) Confidence diminished with task difficulty and is not affected by the presence of an irrelevant alternative. (b) Confidence difference between 3 and 2 alternative conditions, per participant.

We explored the impact of the presence of the third alternative on confidence level separately for correct and incorrect responses, as in Experiment 1 (Fig. 12). For correct trials only, confidence was not affected by the number of alternatives ( $F_{1, 51} = 0.03$ ,  $p = 0.86$ ,  $\eta_p^2 = 0.0006$ ) and we did not find an interaction between task difficulty and the number of alternatives ( $F_{2, 102} = 2.61$ ,  $p = 0.078$ ,  $\eta_p^2 = 0.05$ ). For incorrect trials, we did not find an effect of the amount of alternatives ( $F_{1, 25} = 0.045$ ,  $p = 0.83$ ,  $\eta_p^2 = 0.002$ ) or an interaction between task difficulty and the number of alternatives ( $F_{2, 50} = 1.40$ ,  $p = 0.26$ ,  $\eta_p^2 = 0.05$ ) (Fig. 12c).



**Fig. 12.** The impact of the third alternative on confidence dissociated by correct and incorrect responses. (a) Considering all trials, the third alternative did not increase confidence at any level of difficulty. Moreover, the third alternative did not have an effect on confidence neither when considering (b) correct trials nor (c) incorrect trials.

### 5.3 Discussion

The target categorization task of Experiment 3 does not show a dud-alternative effect: confidence remained the same despite the addition of a third, clearly incorrect alternative. The inclusion of the dud-alternative did not affect performance or confidence, but made response times longer. This could be one of the reasons that this experiment bears no dud-alternative effect, since longer response times are usually associated with more difficult tasks and with lower confidence levels (Kiani et al., 2014). Another possible reason underlying the lack of the dud-alternative effect is the different presentation times of the stimuli: up to 1 second in experiments 1 and 2, and untimed in Experiment 3. In fact, the computations underlying confidence in purely perceptual tasks with brief stimuli presentations could be different because confidence has to rely more on the internal representation of the stimuli (Rahnev, 2020; Yeon & Rahnev, 2020). Consequently, we decided to test in Experiment 4 and 5 whether the dud-alternative effect is present both in the size discrimination task with unlimited presentation time of the stimuli (as in Experiment 3) and in the target categorization task with the stimuli presentation time restricted to one second (as in Experiments 1 and 2).

## 6. Experiment 4

To investigate whether stimuli presentation time is driving the dud alternative effect, we conducted two more experiments: Experiment 4 consisted of the same size discrimination task as in Experiment 1 but stimuli were present up to the time of the decision as in

Experiment 3; Experiment 5 consisted of the same target categorization task as in Experiment 3 with stimuli being on screen for 1 second as in Experiments 1 and 2.

## 6.1 Materials & methods

As in the previous experiments, Experiment 4 was conducted online on JATOS (Lange et al., 2015) and programmed in JavaScript using the library jQuery.

### 6.1.1 Participants & experimental design

34 participants took part in this experiment (73.5% females; mean age = 25.5, sd = 6.38). One subject was excluded due to slow response times (see 6.1.2 Data analysis), so the final sample consisted of 33 participants.

The design was similar to the design of Experiment 1, with the difference that the stimuli remained on screen up to the time that the participant made the decision. To inform their choice, participants clicked directly on the geometrical figures.

### 6.1.2 Data analysis

We excluded trials with RT lower than 200 ms for both [decisions](#) and [confidence reports](#). We also excluded trials with RT greater than 20 s (both in [decisions](#) 1 and [confidence reports](#)) as in Experiment 3. With this filter one subject was completely excluded because of larger response times. [The reported results do not change if we include this data](#). We conducted repeated measures ANOVAs and Tukey HSD post hoc tests (both with the Statistica software) to estimate the impact of the difficulty of the task and the dud alternatives in RT, performance and confidence. Our predefined p-value for statistical significance was 0.05. The ANOVA for incorrect trials was done with the highest levels of difficulty (0.9, 0.93, 0.95) because there were not enough incorrect trials in easier conditions (0.7 and 0.8).

## 6.2 Results

### 6.2.1 Response times

Task difficulty had a significant effect on [decisions](#) RT ( $F_{4, 128} = 27.49, p < 0.000001, \eta_p^2 = 0.46$ ) (Fig. 13a). The inclusion of a third alternative did not affect [decisions](#) RT ( $F_{1, 32} = 0.39, p = 0.54, \eta_p^2 = 0.02$ ). No interaction was found between the number of alternatives and task difficulty ( $F_{4, 128} = 1.12, p = 0.35, \eta_p^2 = 0.03$ ). Task difficulty affected [confidence reports](#) RT ( $F_{4, 128} = 5.79, p = 0.0003, \eta_p^2 = 0.15$ ). The number of alternatives did not impact [confidence reports](#) RT ( $F_{1, 32} = 0.49, p = 0.49, \eta_p^2 = 0.015$ ). An interaction was found between task difficulty and the number of alternatives regarding [confidence reports](#) RT ( $F_{4, 128} = 2.84, p = 0.03, \eta_p^2 = 0.08$ ).

### 6.2.2 Performance

Performance, as expected, decreased as the task became more difficult ( $F_{4, 128} = 92.64$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.74$ ). The presence of a third alternative did not have an effect on performance ( $F_{1, 32} = 2.80$ ,  $p = 0.10$ ,  $\eta_p^2 = 0.08$ ). We did not find an interaction between task difficulty and the number of alternatives ( $F_{4, 128} = 1.45$ ,  $p = 0.22$ ,  $\eta_p^2 = 0.04$ ).

We again analyzed whether the shape of the third alternative had an effect on the shape that the participant picked (“square” vs “circle” choices). Comparing the 2-alternative condition and the 3-alternative condition when the dud-alternative was a square shows no effect regarding “square” choices ( $F_{1, 32} = 0.05$ ,  $p = 0.82$ ,  $\eta_p^2 = 0.002$ ). The presence of a third alternative that was a circle did not affect the proportion of “circle” choices either ( $F_{1, 32} = 1.11$ ,  $p = 0.3$ ,  $\eta_p^2 = 0.025$ ).

### 6.2.3 Confidence

Confidence, as expected and in line with performance, decreased with task difficulty ( $F_{4, 128} = 49.02$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.61$ ) (Fig. 13a). We replicated the dud-alternative effect found in Experiments 1 and 2 since confidence increased in the 3-alternative condition ( $F_{1, 32} = 20.28$ ,  $p = 0.00008$ ,  $\eta_p^2 = 0.39$ ) (Fig. 13a). Also, there was an interaction between the number of alternatives and task difficulty ( $F_{4, 128} = 3.03$ ,  $p = 0.02$ ,  $\eta_p^2 = 0.09$ ) (Fig. 13a). The effect was found for both correct ( $F_{1, 32} = 16.79$ ,  $p = 0.0003$ ,  $\eta_p^2 = 0.34$ ) and incorrect ( $F_{1, 22} = 7.87$ ,  $p = 0.01$ ,  $\eta_p^2 = 0.26$ ) trials. Comparing the confidence increment between correct and incorrect trials (on the 3 highest levels of difficulty) no differences were found ( $F_{1, 22} = 0.88$ ,  $p = 0.36$ ,  $\eta_p^2 = 0.04$ ).

Regarding the size of the third alternative, we found a significant effect ( $F_{6, 186} = 2.67$ ,  $p = 0.02$ ,  $\eta_p^2 = 0.08$ ). A Tukey HSD post-hoc test shows that the differences are between the 2-alternative condition and the conditions where the third alternative adopted the 0.07 ( $p = 0.04$ ) and the 0.28 ( $p = 0.008$ ) of the area of the stimulus 1.

As in Experiment 1, we did not find an effect of the shape of the third alternative on confidence: when considering if the dud alternative was a circle or a square only on the 3-alternative condition, no difference was found in confidence neither for “circle” choices ( $F_{1, 21} = 0.73$ ,  $p = 0.4$ ,  $\eta_p^2 = 0.03$ ) nor for “square” choices ( $F_{1, 27} = 0.43$ ,  $p = 0.52$ ,  $\eta_p^2 = 0.016$ ).

## 7. Experiment 5

As mentioned previously, to evaluate if presentation time of the stimuli is the main factor driving the dud-alternative effect we also conducted the target categorization task of Experiment 3 but with restricted presentation time: stimuli were present on screen up to 1 second as in Experiments 1 and 2.

## 7.1 Materials & methods

### 7.1.1 Participants & experimental design

31 participants took part in this experiment (83.9% females; mean age = 27.42, sd = 7.64). Participants should read and accept an informed consent prior to the realization of the experiment. All participants reported no psychiatric, illegal drug consumption or neurological history. The tasks' instructions were written on screen prior to the experiment. All participants completed the experiment on a computer.

The design was the same as Experiment 3, with the difference that the stimuli remained on screen up to 1 second.

### 7.1.2 Data analysis

We excluded trials with RT lower than 200 ms for both [decisions](#) and [confidence reports](#). We also excluded trials with RT greater than 10 s (both in [decisions](#) and [confidence reports](#)) as in Experiments 1 and 2. [Including the discarded data does not modify the results](#). We conducted repeated measures ANOVAs and Tukey HSD post hoc tests (both with the Statistica software) to estimate the impact of the difficulty of the task and the dud alternatives in RT, performance and confidence. Our predefined p-value for statistical significance was 0.05.

## 7.2 Results

### 7.2.1 Response times

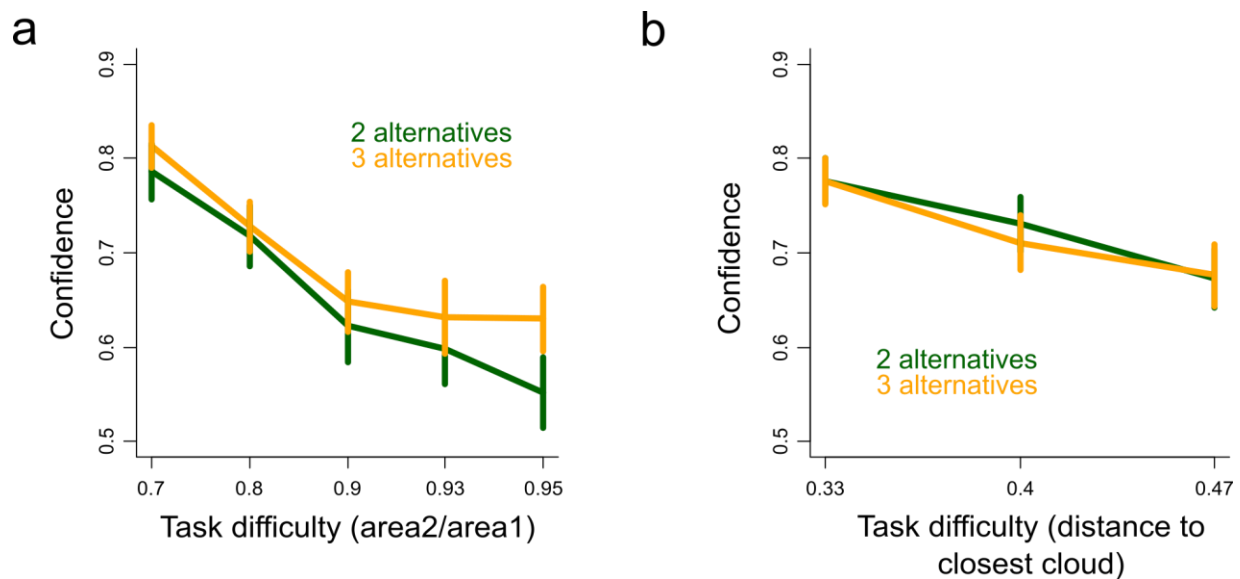
Task difficulty had a significant effect on [decisions](#) RT ( $F_{2, 60} = 13.73$ ,  $p = 0.00001$ ,  $\eta_p^2 = 0.31$ ). The inclusion of a third alternative made [decisions](#) RT larger ( $F_{1, 30} = 4.84$ ,  $p = 0.04$ ,  $\eta_p^2 = 0.14$ ). No interaction was found between the number of alternatives and task difficulty for [decisions](#) RT ( $F_{2, 60} = 1.52$ ,  $p = 0.23$ ,  $\eta_p^2 = 0.05$ ). Task difficulty did not affect [confidence reports](#) RT ( $F_{2, 60} = 1.66$ ,  $p = 0.20$ ,  $\eta_p^2 = 0.05$ ). The number of alternatives did not impact [confidence reports](#) RT ( $F_{1, 30} = 0.67$ ,  $p = 0.42$ ,  $\eta_p^2 = 0.02$ ). No interaction was found between task difficulty and the number of alternatives regarding [confidence reports](#) RT ( $F_{2, 60} = 0.44$ ,  $p = 0.65$ ,  $\eta_p^2 = 0.01$ ).

### 7.2.2 Performance

Performance decreased with task difficulty ( $F_{2, 60} = 155.77$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.84$ ). The presence of a third alternative did not have an effect on performance ( $F_{1, 30} = 0.035$ ,  $p = 0.85$ ,  $\eta_p^2 = 0.001$ ). We did not find an interaction between task difficulty and the number of alternatives ( $F_{2, 60} = 0.52$ ,  $p = 0.6$ ,  $\eta_p^2 = 0.02$ ).

### 7.2.3 Confidence

Confidence decreased with increasing levels of task difficulty ( $F_{2, 60} = 31.47, p < 0.000001, \eta_p^2 = 0.51$ ) (Fig. 13b). As in Experiment 3, confidence was not affected by the presence of a dud-alternative ( $F_{1, 30} = 1.15, p = 0.29, \eta_p^2 = 0.04$ ) (Fig. 13b). There was not an interaction between the number of alternatives and task difficulty ( $F_{2, 60} = 1.69, p = 0.19, \eta_p^2 = 0.05$ ) (Fig. 13b).



**Fig. 13.** Both experiments show converging evidence that the dud-alternative effect is independent of the presentation time of the stimuli. a) The dud-alternative effect was found for the size discrimination task even if stimuli remained on screen up to the participants' response. b) Despite restricting stimuli presentation time up to 1s in the target categorization task, no dud-alternative effect was found.

## 7.3 Discussion

Both Experiments 4 and 5 show converging evidence that the dud-alternative effect is not dependent on the presentation time of the stimuli, as the effect was replicated in Experiment 4 and, again, not found in the target categorization task of Experiment 5.

The dud alternatives did not affect performance nor RT in the size discrimination task, adding more evidence to the previous claims of Experiment 1 and 2 that the dud-alternatives did not make the task harder. Regarding RTs for the target categorization task, we found again that they were longer in the 3-alternative condition (as in Experiment 3). This could reflect that people were in fact more uncertain when the third alternative was present, thus canceling out a possible dud-alternative effect because of a decision process inherently more difficult.

Experiment 4 shows no “attraction effect”: people were equally likely to choose a square when the third alternative was a square when compared to the 2-alternative condition, and the same holds for “circle” choices. Moreover, this experiment replicates the findings of Experiment 1 in the sense that the shape of the dud-alternative did not affect confidence reports. In consequence, both experiments suggest that the dud-alternative effect is independent of the attraction effect.

## **8. General discussion**

In the present study, we investigated whether irrelevant alternatives increase confidence in a perceptual decision. The underlying motivation was that this kind of effect was reported in likelihood judgements (Windschitl & Chambers, 2004), line-up identifications (Charman et al., 2011) and associative memory (Hanczakowski et al., 2014) but never tested in perceptual confidence contexts. Furthermore, most accepted computational models of confidence in perceptual decisions (H.-H. Li & Ma, 2020; Meyniel et al., 2015; Sanders et al., 2016) state that the presence of irrelevant alternatives should not modify it or, in any case, should decrease it. Contrary, our main finding is that these alternatives can increase confidence in perceptual decisions, a result that seems at odds with normative models of confidence.

These weak alternatives, however, do not impact RTs (Experiments 1 and 2) or performance. These null effects are important because they discard that changes in performance or overconfidence usually present in difficult tasks (Baranski & Petrusic, 1994; Gigerenzer et al., 1991) are raising confidence.

Our results from Experiment 1 and 2 cannot be explained by current views of the field proposing that confidence arises directly from the probability of being correct (Meyniel et al., 2015; Sanders et al., 2016) or direct comparisons between the more probable stimulus and the second one (H.-H. Li & Ma, 2020). This depicts why considering the effect of irrelevant alternatives (Charman et al., 2011; Hanczakowski et al., 2014; Windschitl & Chambers, 2004) in models of confidence is needed. To account for the effect in non-perceptual tasks, Charman et al. (2011), Windschitl & Chambers (2004) and Hanczakowski et al. (2014) proposed various theoretical explanations. Interestingly, the preferred one was the Contrast model, that we computationally implemented: confidence level is obtained by a series of pairwise comparisons between the chosen option and the rest. Nevertheless, our computational modeling results suggest that, although the Contrast model captures the effect of increased confidence levels when a dud-alternative is present, only the Average-residual model replicates the pattern of our data. Specifically, the Average-residual model states that people construct their confidence by first judging the support offered by the evidence for chosen option and the support offered by the



average of the rest of the alternatives and then taking the difference between them. In this model having dud alternatives decreases the value of the competing options, inflating confidence.

The Contrast model faces many issues when extending its predictions to other decision contexts. First, the model predicts a constant increment in confidence when adding more than one dud-alternative (for example, a decision context with 2, 3 or more dud-alternatives), as illustrated in Supplementary Fig. 3b. This is not reasonable in extreme cases such as when an observer has to decide between a lot of alternatives (for example, adding a dud-alternative when there are already 15 dud-alternatives is not expected to raise confidence by the same amount as when there are not any dud-alternatives). The Average-residual model, conversely, predicts that increment in confidence should progressively decrease with the number of dud-alternatives, since the average of the residual alternatives will progressively change less with more dud-alternatives. Therefore, the Average-residual model is in a better position to account for the results reported in Experiment 2.

Second, when varying the size of a third alternative –ranging from a dud-alternative to a truly competitive alternative– the Contrast model still predicts that confidence should be higher in the 3-alternative condition. This is a counterintuitive prediction since it is expected that confidence will be lower in the case where 3 alternatives are equally likely to be the right decision when compared to only 2 equally likely alternatives. On the other hand, the Average-residual model predicts that confidence should be lower in that case, as expected (Supplementary Fig. 3a). This is because these models imply normalization, so a high value of a third alternative implies that the posterior probability for the chosen option also decreases, leading to a decrease in confidence. However, this decrease is not large enough to compensate for the increase in confidence by the presence of a dud-alternative in the Contrast model.

Finally, the Contrast model predicts that confidence should always increase with the presence of a dud-alternative, even if the task at hand is very easy. This is, again, a counterintuitive prediction since if a task is really easy one should reach a maximum confidence level. Therefore, the addition of a dud-alternative is not expected to have a large effect. The Average-residual model, on the other hand, predicts that the increase in confidence should be lower on easy tasks (and no increment is predicted if the two non-chosen options are equal, i.e. the both options are dud-alternatives). Indeed, according to the Average-residual mechanism, we found a null or reduced increase in confidence on easy trials on Experiment 1, 2 and 4. Taking into account all of these predictions, the Average-residual model not only is the best explanation for the dud-alternative effect, but

also seems a plausible blueprint for a general mechanism for computing confidence in multi-alternative tasks in general.

Windschitl & Chambers (2004) discuss a version of the Contrast model that includes a weight in the comparison between the chosen option and the dud-alternative, thus making the increment in confidence due to this contrast flexible. With this modification, the model could improve its performance regarding the fit to our data. However, this modified Contrast model will still predict a constant, difficulty independent increment in confidence, so it is likely that the model will not be better than the Average-residual model as it is (and, consequently, will definitely not be better than an Average-residual model including a weight, to match the number of free parameters). Moreover, the modification implies that the model should have an extra free parameter for controlling the weight of the contrast, making the model more complex unnecessarily since there is already a model that provides a better fit without the need of an extra free parameter.

Prior research suggests that maintaining mental representations for all alternatives is costly (Maniscalco et al., 2016). In that scenario, confidence only relies on the evidence in favor of the chosen option, also known as “positive evidence bias” (Koizumi et al., 2015; Maniscalco et al., 2016; Peters et al., 2017; Zylberberg et al., 2012). However, unchosen options can affect confidence (H.-H. Li & Ma, 2020). Our results and model are in line with this posture, since even very weak alternatives are taken into account to make confidence judgments. Moreover, our findings also deviate from the notion that, in multi-alternative perceptual decisions, individuals making decisions only have access to the level of activity of the alternative with highest internal activity (Yeon & Rahnev, 2020). Indeed, the Average-residual model necessarily implies that the level of activity of all alternatives is accessible for the observer in order to compute confidence.

The picture, however, seems more complicated. Our results from Experiments 3 and 5 show that, in that particular task, the dud-alternative barely affects confidence. This constitutes a main challenge for the Average-residual model. Why does this experimental paradigm show no dud-alternative effect? First of all, the slower reaction times found in these experiments in the 3-alternative condition may indicate that observers were more uncertain and needed more time to make their decision; this could counteract the dud-alternative effect. Second, we tested if stimuli presentation time plays a role in the dud-alternative effect. The reason was that in perceptual tasks with brief stimuli presentations, confidence computations rely more on an internal representation (Rahnev, 2020). Thus, mechanisms acting in Experiments 1 and 2 may differ from the ones acting in Experiment 3. In fact, the dud alternative effect is more prominent in timed tasks (Windschitl & Chambers, 2004). In this line, an alternative explanation for our results might be that the dud alternative effect depends on a form of variance misperception (Zylberberg et al.,

2014), an overconfidence bias found in perceptual tasks when signal is low and perceptual noise is added (M. K. Li et al., 2018; Rahnev et al., 2011; Solovey et al., 2015). The presence of dud alternatives might add perceptual noise, causing the participants to have higher levels of confidence if they do not adjust their [confidence](#) criteria accordingly. That is, if participants fixate on the third alternative, the rest of the alternatives remain at an attentional periphery, where there are effects of variance misperception and overconfidence (Winter & Peters, 2021) due to noisier percepts caused by the poorer resolution of the peripheral visual field. Larger stimuli presentations would rule out possible variance misperception effects, due to a higher signal to noise ratio. However, decreasing the stimuli duration used in Experiment 3 (Experiment 5) does not induce a raise in confidence levels in 3-alternative trials; also, the effect does not disappear with unlimited presentation time in the size discrimination task (Experiment 4). Consequently, stimuli presentation time seems not to be a factor driving the dud-alternative effect. In third place, another possible explanation might be that the dud-alternative effect in the size discrimination task is driven by the “Ebbinghaus illusion” (Roberts et al., 2005): shapes are perceived larger when surrounded by small shapes. The irrelevant alternative(s) may induce such an illusion by making the chosen option appear larger to the observer as compared to when the dud-alternative is not present. Confidence therefore will be higher due to the “positive evidence bias” mentioned above: the observer has now more evidence for her choice, because her chosen option now seems larger than in the 2-alternative condition. Importantly, if this is the case, it may explain why there is not a dud-alternative effect in Experiment 3 and 5, as this illusion is not present with that stimuli. Despite appealing, the Ebbinghaus illusion explanation predicts that the increment in confidence should be more pronounced on easy trials because all of the incorrect options are small. However, we see the opposite pattern in our data: confidence level rises due to the dud-alternative presence specifically on difficult trials, consistent with the explanation proposed by the Average-residual model. Moreover, according to the Ebbinghaus illusion account, the increment in confidence should be higher with lower size values of the third alternative. However, no effect was found regarding the size of irrelevant alternatives within the 3-alternative condition: confidence increased equally irrespective of the third alternative size. This is again consistent with the Average-residual account as the model predicts a relatively constant increase in confidence as long as the alternatives are irrelevant, as in our case (Supplementary Fig. 3).

Having ruled out those possible explanations, we must note that the dud-alternative effect is already reported in a range of different tasks (Charman et al., 2011; Hanczakowski et al., 2014; Windschitl & Chambers, 2004). This implies that different mechanisms take place on the target categorization task of Experiments 3 and 5. We identify three major characteristics of this experimental paradigm that are likely causing the lack of effect. First, this task requires a probabilistic response, i.e. the target could belong to either cloud

with a certain probability. This kind of probabilistic alternatives is different from the size discrimination task and also from the previous dud-alternative effect literature, where there were definite correct alternatives. This may induce a more probabilistic –and therefore, normative– use of the confidence scale, that could explain the absence of the rise in confidence levels in presence of the third cloud. Indeed, the dud-alternative effect is not present in tasks that induce concerns regarding the complementary rule (Windschitl & Chambers, 2004). Second, this task implies a direct distance judgment (between the target and the clouds) between two probable alternatives, thus making it reasonable that confidence reflects the difference between the probabilities of the best-two competing alternatives, as stated by the Diff model. Finally, there is the possibility that the third alternative was not even taken into account by the subjects for being highly irrelevant. Under this possibility, the increased response times on both target categorization experiments in the 3-alternative condition may reflect extra-time for searching for the target instead of increased uncertainty. As the distance between the third alternative and the target was not manipulated, we cannot rule out this possibility. Further research could vary this distance to evaluate whether this is a plausible explanation.

Previous research including irrelevant alternatives has shown a wide range of context effects in our decision making. The size discrimination task used here allow for the possibility of testing one particular context effect: the attraction effect (Huber et al., 1982), already reported in perceptual decision making (Trueblood et al., 2013). This effect implies that decision makers will more likely choose a specific alternative A when comparing to another alternative B when a third option simultaneously similar but inferior to A is added in the decision context. In Experiment 1, we found an attraction effect for “square” choices restricted to the highest level of difficulty (that is, participants were more likely to choose a square if the third alternative was also a square), but no clear pattern was found regarding the “circle” choices. Importantly, this effect does not interact with the increase in confidence. In Experiment 4 we did not find any attraction effect, neither in choices nor in confidence. These results suggest that the dud-alternative effect is independent of the attraction effect.

In conclusion, our results imply that —at least in some contexts— confidence in multi-alternative decisions deviates from the traditional Bayesian confidence hypothesis and from the Difference model, recently developed for decisions with multiple alternatives. Moreover, our findings suggest that unchosen options affect confidence in a way that is explained by the Average-residual model. This particular model not only gives the best explanation for the dud-alternative effect but also points out a possible mechanism for computing confidence in general multi-alternative contexts. Future computational models should consider this effect and the predictions of the Average-residual model to more accurately explain human confidence levels in perceptual decision-making.

## **CRedit authorship contribution statement**

**Nicolás A. Comay:** Conceptualization, Methodology, Software, Validation, Formal analysis, Investigation, Data curation, Writing – Original Draft, Writing – Review & Editing, Visualization. **Gabriel Della Bella:** Software. **Pedro Lamberti:** Software. **Mariano Sigman:** Conceptualization, Methodology, Writing – Original Draft, Writing – Review & Editing, Supervision. **Guillermo Solovey:** Conceptualization, Methodology, Software, Writing – Original Draft, Writing – Review & Editing, Supervision, Funding acquisition, Project administration. **Pablo Barttfeld:** Conceptualization, Methodology, Software, Writing – Original Draft, Writing – Review & Editing, Supervision, Funding acquisition, Project administration.

## **Acknowledgements**

This research was supported by a grant from Agencia Nacional de Promoción Científica y Tecnológica (Argentina) PICT (Grant #2018-03614). Nicolás A. Comay and Gabriel Della Bella have a scholarship from the National Scientific and Technical Research Council (CONICET - Argentina).

## **Supplementary material**

All data and materials are stored in [https://github.com/nicolascomay/confidence\\_dud](https://github.com/nicolascomay/confidence_dud). This includes the source code of the 5 experiments, the .jzip archives for uploading the experiments to JATOS and R code for model fitting and replication of main figures.

## **Declaration of interest**

None.

## **References**

- Ais, J., Zylberberg, A., Barttfeld, P., & Sigman, M. (2016). Individual consistency in the accuracy and distribution of confidence judgments. *Cognition*, 146, 377-386.  
<https://doi.org/10.1016/j.cognition.2015.10.006>
- Ariely, D., & Wallsten, T. S. (1995). Seeking Subjective Dominance in Multidimensional

Space: An Explanation of the Asymmetric Dominance Effect. *Organizational Behavior and Human Decision Processes*, 63(3), 223-232.

<https://doi.org/10.1006/obhd.1995.1075>

Baranski, J. V., & Petrusic, W. M. (1994). The calibration and resolution of confidence in perceptual judgments. *Perception & Psychophysics*, 55(4), 412-428.

<https://doi.org/10.3758/BF03205299>

Charman, S. D., Wells, G. L., & Joy, S. W. (2011). The dud effect: Adding highly dissimilar fillers increases confidence in lineup identifications. *Law and Human Behavior*, 35(6), 479-500. <https://doi.org/10.1007/s10979-010-9261-1>

Drugowitsch, J., Moreno-Bote, R., & Pouget, A. (2014). Relation between Belief and Performance in Perceptual Decision Making. *PLOS ONE*, 9(5), e96511.

<https://doi.org/10.1371/journal.pone.0096511>

Fleming, S. M., & Lau, H. C. (2014). How to measure metacognition. *Frontiers in Human Neuroscience*, 8. <https://doi.org/10.3389/fnhum.2014.00443>

Galvin, S. J., Podd, J. V., Drga, V., & Whitmore, J. (2003). Type 2 tasks in the theory of signal detectability: Discrimination between correct and incorrect decisions.

*Psychonomic Bulletin & Review*, 10(4), 843-876.

<https://doi.org/10.3758/BF03196546>

Gigerenzer, G., Hoffrage, U., & Kleinbölting, H. (1991). Probabilistic mental models: A Brunswikian theory of confidence. *Psychological Review*, 98(4), 506-528.

<https://doi.org/10.1037/0033-295X.98.4.506>

Grimaldi, P., Lau, H., & Basso, M. A. (2015). There are things that we know that we know, and there are things that we do not know we do not know: Confidence in

decision-making. *Neuroscience & Biobehavioral Reviews*, 55, 88-97.

<https://doi.org/10.1016/j.neubiorev.2015.04.006>

Hanczakowski, M., Zawadzka, K., & Higham, P. A. (2014). The dud-alternative effect in memory for associations: Putting confidence into local context. *Psychonomic Bulletin & Review*, 21(2), 543-548. <https://doi.org/10.3758/s13423-013-0497-x>

Huber, J., Payne, J. W., & Puto, C. (1982). Adding Asymmetrically Dominated Alternatives: Violations of Regularity and the Similarity Hypothesis. *Journal of Consumer Research*, 9(1), 90. <https://doi.org/10.1086/208899>

Kepecs, A., & Mainen, Z. F. (2012). A computational framework for the study of confidence in humans and animals. *Philosophical Transactions of the Royal Society B: Biological Sciences*, 367(1594), 1322-1337.

<https://doi.org/10.1098/rstb.2012.0037>

Kiani, R., Corthell, L., & Shadlen, M. N. (2014). Choice Certainty Is Informed by Both Evidence and Decision Time. *Neuron*, 84(6), 1329-1342.

<https://doi.org/10.1016/j.neuron.2014.12.015>

Koizumi, A., Maniscalco, B., & Lau, H. (2015). Does perceptual confidence facilitate cognitive control? *Attention, Perception, & Psychophysics*, 77(4), 1295-1306.

<https://doi.org/10.3758/s13414-015-0843-3>

Lange, K., Kühn, S., & Filevich, E. (2015). "Just Another Tool for Online Studies" (JATOS): An Easy Solution for Setup and Management of Web Servers Supporting Online Studies. *PLOS ONE*, 10(6), e0130834.

<https://doi.org/10.1371/journal.pone.0130834>

Li, H.-H., & Ma, W. J. (2020). Confidence reports in decision-making with multiple

- alternatives violate the Bayesian confidence hypothesis. *Nature Communications*, 11(1), 2004. <https://doi.org/10.1038/s41467-020-15581-6>
- Li, M. K., Lau, H., & Odegaard, B. (2018). An investigation of detection biases in the unattended periphery during simulated driving. *Attention, Perception, & Psychophysics*, 80(6), 1325-1332. <https://doi.org/10.3758/s13414-018-1554-3>
- Louie, K., Khaw, M. W., & Glimcher, P. W. (2013). Normalization is a general neural mechanism for context-dependent decision making. *Proceedings of the National Academy of Sciences*, 110(15), 6139-6144. <https://doi.org/10.1073/pnas.1217854110>
- Luce, R. D. (1979). *Individual choice behavior: A theoretical analysis*. Greenwood Press.
- Ma, W. J. (2019). Bayesian Decision Models: A Primer. *Neuron*, 104(1), 164-175. <https://doi.org/10.1016/j.neuron.2019.09.037>
- Mamassian, P. (2016). Visual Confidence. *Annual Review of Vision Science*, 2(1), 459-481. <https://doi.org/10.1146/annurev-vision-111815-114630>
- Maniscalco, B., & Lau, H. (2012). A signal detection theoretic approach for estimating metacognitive sensitivity from confidence ratings. *Consciousness and Cognition*, 21(1), 422-430. <https://doi.org/10.1016/j.concog.2011.09.021>
- Maniscalco, B., Peters, M. A. K., & Lau, H. (2016). Heuristic use of perceptual evidence leads to dissociation between performance and metacognitive sensitivity. *Attention, Perception, & Psychophysics*, 78(3), 923-937. <https://doi.org/10.3758/s13414-016-1059-x>
- Meyniel, F., Sigman, M., & Mainen, Z. F. (2015). Confidence as Bayesian Probability:



From Neural Origins to Behavior. *Neuron*, 88(1), 78-92.

<https://doi.org/10.1016/j.neuron.2015.09.039>

Niwa, M., & Ditterich, J. (2008). Perceptual Decisions between Multiple Directions of Visual Motion. *Journal of Neuroscience*, 28(17), 4435-4445.

<https://doi.org/10.1523/JNEUROSCI.5564-07.2008>

Northoff, G., & Mushiake, H. (2020). Why context matters? Divisive normalization and canonical microcircuits in psychiatric disorders. *Neuroscience Research*, 156, 130-140. <https://doi.org/10.1016/j.neures.2019.10.002>

Peters, M. A. K., Thesen, T., Ko, Y. D., Maniscalco, B., Carlson, C., Davidson, M., Doyle, W., Kuzniecky, R., Devinsky, O., Halgren, E., & Lau, H. (2017).

Perceptual confidence neglects decision-incongruent evidence in the brain.

*Nature Human Behaviour*, 1(7), 0139. <https://doi.org/10.1038/s41562-017-0139>

Pleskac, T. J., & Busemeyer, J. R. (2010). Two-stage dynamic signal detection: A theory of choice, decision time, and confidence. *Psychological Review*, 117(3), 864-901. <https://doi.org/10.1037/a0019737>

Pouget, A., Drugowitsch, J., & Kepecs, A. (2016). Confidence and certainty: Distinct probabilistic quantities for different goals. *Nature Neuroscience*, 19(3), 366-374.

<https://doi.org/10.1038/nn.4240>

Rahnev, D. (2020). Confidence in the Real World. *Trends in Cognitive Sciences*, 24(8), 590-591. <https://doi.org/10.1016/j.tics.2020.05.005>

Rahnev, D., & Denison, R. N. (2018). Suboptimality in perceptual decision making. *Behavioral and Brain Sciences*, 41, e223.

<https://doi.org/10.1017/S0140525X18000936>

- Rahnev, D., Maniscalco, B., Graves, T., Huang, E., de Lange, F. P., & Lau, H. (2011). Attention induces conservative subjective biases in visual perception. *Nature Neuroscience*, *14*(12), 1513-1515. <https://doi.org/10.1038/nn.2948>
- Ratcliff, R., Smith, P. L., Brown, S. D., & McKoon, G. (2016). Diffusion Decision Model: Current Issues and History. *Trends in Cognitive Sciences*, *20*(4), 260-281. <https://doi.org/10.1016/j.tics.2016.01.007>
- Ratcliff, R., & Starns, J. J. (2013). Modeling confidence judgments, response times, and multiple choices in decision making: Recognition memory and motion discrimination. *Psychological Review*, *120*(3), 697-719. <https://doi.org/10.1037/a0033152>
- Roberts, B., Harris, M. G., & Yates, T. A. (2005). The Roles of Inducer Size and Distance in the Ebbinghaus Illusion (Titchener Circles). *Perception*, *34*(7), 847-856. <https://doi.org/10.1068/p5273>
- Sanders, J. I., Hangya, B., & Kepecs, A. (2016). Signatures of a Statistical Computation in the Human Sense of Confidence. *Neuron*, *90*(3), 499-506. <https://doi.org/10.1016/j.neuron.2016.03.025>
- Solovey, G., Graney, G. G., & Lau, H. (2015). A decisional account of subjective inflation of visual perception at the periphery. *Attention, Perception, & Psychophysics*, *77*(1), 258-271. <https://doi.org/10.3758/s13414-014-0769-1>
- Trueblood, J. S., Brown, S. D., Heathcote, A., & Busemeyer, J. R. (2013). Not Just for Consumers: Context Effects Are Fundamental to Decision Making. *Psychological Science*, *24*(6), 901-908. <https://doi.org/10.1177/0956797612464241>
- Windschitl, P. D., & Chambers, J. R. (2004). The Dud-Alternative Effect in Likelihood

Judgment. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, 30(1), 198-215. <https://doi.org/10.1037/0278-7393.30.1.198>

Winter, C. J., & Peters, M. A. K. (2021). *Variance misperception under skewed empirical noise statistics explains overconfidence in the visual periphery* [Preprint].

Neuroscience. <https://doi.org/10.1101/2021.01.08.425966>

Yeon, J., & Rahnev, D. (2020). The suboptimality of perceptual decision making with multiple alternatives. *Nature Communications*, 11(1), Art. 1.

<https://doi.org/10.1038/s41467-020-17661-z>

Zylberberg, A., Barttfeld, P., & Sigman, M. (2012). The construction of confidence in a perceptual decision. *Frontiers in Integrative Neuroscience*, 6.

<https://doi.org/10.3389/fnint.2012.00079>

Zylberberg, A., Roelfsema, P. R., & Sigman, M. (2014). Variance misperception explains illusions of confidence in simple perceptual decisions. *Consciousness and Cognition*, 27, 246-253. <https://doi.org/10.1016/j.concog.2014.05.012>

## Editor:

Dear Mr. Nicolás Comay,

Reviewers' comments on your work have now been received. They are attached below. You will see that while Reviewers 1 and 3 now recommend publications "as is", Reviewer 2 has some residual concerns that you should probably address. Given the generally positive response to your revised manuscript, I would suggest that while you address all remaining issues regarding the clarity, for some other issues I would be happy for you to indicate why you disagree with Reviewer 2. I look forward to seeing your final revised manuscript.

Please bear in mind the following standard caveat if and when you revise the paper: Inviting resubmission does not entail that the next version, or any subsequent version, will be accepted for publication. It is our policy to avoid a protracted editorial process that may in any case end, eventually, in rejection. Moreover, the clarifications that result from the revision may reveal new issues, hitherto unnoticed, that preclude publication. I am not pre-judging this particular case; this is something I warn all authors of prior to inviting resubmission.

## Reviewer #1:

The authors had addressed my previous comments/suggestions.

**Response 1.0:** We thank the reviewer for his/her comments and suggestions that greatly improved our manuscript.

## Reviewer #2:

This revision contains a number of substantial changes that improve the paper. First, the authors included two new studies that together serve to rule out a presentation timing hypothesis. Second, the models are specified in greater detail. Third, the discussion of the models in the Discussion section better illuminates the contribution of the paper relative to its last version. Although the paper still doesn't provide strong direct evidence for why the dual-alternative effect was not found in the categorization task whereas it was found in the perceptual decision-making task, I appreciate that the two new experiments do bring us one step closer to understanding the differences in those paradigms, by ruling out one of the possible candidates. I also thought the speculation about the differences is stronger in the General Discussion than it used to be. Therefore, I am leaning more favorably towards publishing this paper. With that said, there are a number of issues or loose ends that should get attention.

**Response 2.0:** We thank the reviewer for his/her suggestions that improved the quality of our study. We considered all remaining concerns and made changes accordingly. We believe this new and improved version of the manuscript addresses those issues. We remain open if further changes are needed.

--In my last review, I suggested that the averaged residual account predicted that a dud alternative effect would occur even with the addition of alternatives that have posterior probabilities that are just slightly weaker than the already existing alternatives. In the authors' response, they explained that the model produces a probability distribution in which the responses for all alternatives would need to sum to 1, and that this implies that the "addition of a third alternative that is highly competitive but slightly weaker than the other two alternatives will also lower the probabilities of these last ones." Okay, but then are the descriptions of the averaged-residual account in 3.1.1 sufficiently informative? It seems like a reader is left to realize that the reason why the averaged-residual account makes that prediction is not because of what is described in 3.1.1 but more because of what is described in the model fitting paragraph 3.1.2.

**Response 2.1:** We thank the reviewer for this comment. As section 3.1.1 is a general introduction of the model, we did not include a discussion of this particular prediction. However, to clarify this issue, there is a paragraph dedicated to this point on Section "3.3 Discussion" and, additionally, the Supplementary Material provides more details.

--I am not sure what to make of the authors' discussion of how the average residual model predicts that confidence would increase monotonically with the number of duds. First, it's not clear what should be considered statistically significant support for this prediction. The authors claim that the data from Experiment 2 support this prediction (e.g., see 4.2.3 and see the third and fourth paragraphs of the General Discussion). However, in the results for Study 2, I see an inferential test of the difference in confidence between cases in which there are two versus five alternatives. This is essentially comparing cases when a dud is absent versus a dud is present. In that same paragraph, the authors test a case in which there are two alternatives versus three and two alternatives versus four. I don't see inferential tests that compare cases in which there are a total of 3 versus 4 alternatives or 4 versus 5 alternatives. (BTW, that paragraph is awfully hard to interpret.) So, I don't really think there's significant evidence showing that confidence does increase with the addition of more duds.

**Response 2.2:** We agree with the reviewer that there is not significant evidence of this increase, as an ANOVA (now reported) does not show a significant increasing effect on confidence between 1, 2 & 3 dud-alternatives. We changed the text accordingly. We now don't state that the pattern in the data is statistically significant. We thank the reviewer for pointing this out.

--Related to this issue, the fourth paragraph of the General Discussion gets very confusing when it starts to discuss how the contrast model makes the same prediction but that this prediction gets unrealistic in the case of where there are many alternatives. I think with a few adjustments, these issues could be clarified. The rest of that paragraph contains a number of interesting points.

**Response 2.3:** We thank the reviewer for this comment. We adjusted the beginning of the paragraph and referred the reader to the Supplementary Fig. 3b for more clarity on the subject.

--In Study 1, I like it that the authors manipulated the size of the added alternative. However, the description of these results in section 2.2.3 is a little confusing, and there aren't any figures

giving readers an easily interpretable glimpse at the impact of this manipulation. Would be great if this could be addressed.

**Response 2.4:** We thank the reviewer for pointing this out. We improved section 2.2.3 and, for clarity, we included a figure (current Fig. 3b) on the effect of the size of the irrelevant alternative on confidence and reworded that paragraph.

--Related to the above point, it's a little disappointing that there isn't a parallel manipulation in the categorization task (e.g., manipulate the distance between the third cloud and the other two clouds; not always a distance of 2.5r). Without it, there remains a question of whether the added dud was just so highly implausible that it didn't even serve as even a minor contender. The authors may point to some response time data as a way of suggesting that the added alternative wasn't perceived as entirely irrelevant. However, this isn't quite the same as doing what they did in Study 1. Moreover, perhaps the extended response time had something to do with people just finding the yellow dot and orienting to the problem, more so than how long they took to formulate a response. It would be useful if the authors could discuss some of this in the paper--even if it's mentioned as a limitation.

**Response 2.5:** We thank the reviewer for pointing this out. We now discuss this possibility in the General Discussion section of the manuscript (paragraph number 10).

--In their response to my review, the authors mentioned that they didn't pre-register any studies. They also identified what was and wasn't planned a priori, and they mentioned the (non)implications of dropping some data points. I was glad to see this additional information, but I think it should also go into the paper so readers can have the same benefit of knowing this information.

**Response 2.6:** We agree with the reviewer and we look forward to pre-register our future experiments. We included two sentences on Section 2.1.3 & Section 5.1.3 clarifying that exclusion criteria weren't pre-specified. In all data analysis sections we included a sentence mentioning that the discarded data do not modify the results.

--I don't understand why the last two studies weren't preregistered. This is a limitation of the paper.

**Response 2.7:** We agree with the reviewer that pre-registration should have been done. We apologize for not pre-registering our studies.

--The authors clarified the confidence questions in their response to the reviewers, but they did not include this clarification inside the document itself. I recommend that the document contain better information about exactly how confidence was queried.

**Response 2.8:** We added a paragraph on sections 2.1.2 & 5.1.2 explaining in detail how we asked for confidence in both the instructions and in the experiment.

--It would seem just as easy to label the two parts of the task as decision and confidence rather than referring to them in various locations as type 1 and type 2.

**Response 2.9:** We thank the reviewer for the suggestion. We replaced “type 1” and “type 2” for “decision” and “confidence reports”, respectively.

--In section 2.2.2 the newly added description of results is very hard to follow. It needs rewording.

**Response 2.10:** We agree that Section 2.2.2 was difficult to follow. We modified it and hope it is clearer now.

--Even more important is the wording in section 2.2.3. It seems like there should be a new paragraph starting at the sentence that begins with "Regarding the size of the third alternative..." What follows that sentence was very hard to interpret. This needs recasting.

**Response 2.11:** We agree with the reviewer and modified this paragraph to make it easier to follow. Moreover, we added a figure (Fig. 3b) showing the absence of effect of the third alternative size on confidence that we hope will make more clear the results described in this particular paragraph (as mentioned in Response 2.4).

--Under the contrast model in supplementary figure 3B, the axis labels for confidence go from 0.5 to over 3 in the bottom panel. The authors should fix or explain what's going on here. Looks like the model predictions aren't transferred or constrained to a 0-1 scale.

**Response 2.12:** We thank the reviewer for pointing out this. To map confidence to the 0-1 scale, we included the free parameters  $\beta_0$  and  $\beta_1$ . In the simulations of the Supplementary figures we did not include these parameters to illustrate the behavior of the model without their influence, and that is the reason underlying that scale. We replaced that figure with a simulation with values of  $\beta_0$  and  $\beta_1$  that constrain confidence to a 0-1 scale. We also added a sentence in the legend of the Supplementary Fig. 3b explaining this for clarity.

We thank the reviewer again for his/her comments that improved our work. We hope that we addressed his/her concerns, and remain open for further modifications if needed.

## Reviewer #3:

The authors have addressed my remaining concerns - congratulations for a very interesting and thought-provoking study.

**Response 3.0:** We thank the reviewer for her/his comments and suggestions that greatly improved our manuscript.

## The presence of irrelevant alternatives paradoxically increases confidence in perceptual decisions

Nicolás A. Comay<sup>a+</sup>, Gabriel Della Bella<sup>a</sup>, Pedro Lamberti<sup>b</sup>, Mariano Sigman<sup>c,d</sup>,  
Guillermo Solovey<sup>e\*</sup>, Pablo Barttfeld<sup>a\*</sup>

a- Cognitive Science Group. Instituto de Investigaciones Psicológicas (IIPsi), CONICET-UNC, Facultad de Psicología, Universidad Nacional de Córdoba, Boulevard de la Reforma esquina Enfermera Gordillo, CP 5000. Córdoba, Argentina  
[nicocomay@gmail.com](mailto:nicocomay@gmail.com)

b- Facultad de Matemática, Astronomía, Física y Computación, Universidad Nacional de Córdoba, Córdoba, Argentina.

c- Laboratorio de Neurociencia, Universidad Torcuato Di Tella, Buenos Aires, Argentina.

d- Facultad de Lenguas y Educación, Universidad Nebrija, Madrid, Spain.

e- Instituto de Cálculo, Facultad de Ciencias Exactas y Naturales, UBA-CONICET, Buenos Aires, Argentina

+ *corresponding author*

\* *last authors*



## Abstract

Confidence in perceptual decisions is thought to reflect the probability of being correct. According to this view, confidence should be unaffected or minimally reduced by the presence of irrelevant alternatives. To test this prediction, we designed five experiments. In Experiment 1, participants had to identify the largest geometrical shape among two or three alternatives. In the three-alternative condition, one of the shapes was much smaller than the other two, being a clearly incorrect option. Counter-intuitively, confidence was higher when the irrelevant alternative was present, evidencing that confidence construction is more complex than previously thought. Four computational models were tested, only one of them accounting for the results. This model predicts that confidence increases monotonically with the number of irrelevant alternatives, a prediction we tested in Experiment 2. In Experiment 3, we evaluated whether this effect replicated in a categorical task, but we did not find supporting evidence. Experiments 4 and 5 allowed us to discard stimuli presentation time as a factor driving the effect. Our findings suggest that confidence models cannot ignore the effect of multiple, possibly irrelevant alternatives to build a thorough understanding of confidence.

*Keywords: confidence, perceptual decision making, multiple alternatives, bayesian confidence hypothesis, computational modeling, open data*

## 1. Introduction

We constantly make decisions under uncertainty, accompanied by a feeling of confidence—a belief or a subjective feeling that our own thoughts, knowledge, performance, percepts or decisions are correct (Grimaldi et al., 2015; Mamassian, 2016; Meyniel et al., 2015). To be useful in our everyday activities, confidence has to reflect the true likelihood of being correct (Ais et al., 2016). However, this correspondence is not perfect, and several biases have been described in the literature (Rahnev & Denison, 2018), including overconfidence in difficult tasks and underconfidence in easy tasks (Baranski & Petrusic, 1994; Gigerenzer et al., 1991), a mismatch between confidence and accuracy on individual trials (Maniscalco & Lau, 2012), and overconfidence due to misperception of stimulus variability (Zylberberg et al., 2014). However, despite these findings, the dominant view of the field is that confidence reflects the probability that the decision is correct. This definition is known as the Bayesian confidence hypothesis (BCH) (H.-H. Li & Ma, 2020; Meyniel et al., 2015; Sanders et al., 2016) and is inline with the classical assumption—known as independence of irrelevant alternatives (Luce, 1979)—that the subjective value of a stimulus is only dependent on the stimulus properties.

The Bayesian confidence hypothesis is based mostly on 2-alternative forced choice tasks (2AFC), because they allow for a relatively easy and straightforward computational modeling of confidence (Rahnev, 2020) using diverse approaches, such as signal detection theory (Fleming & Lau, 2014), accumulation of evidence (Pleskac & Busemeyer, 2010; Ratcliff & Starns, 2013) and Bayesian modeling (Drugowitsch et al., 2014; Galvin et al., 2003; Kepecs & Mainen, 2012; Mamassian, 2016; Pouget et al., 2016). However, while methodologically useful, 2AFC tasks are a large oversimplification of the decision-making process, often implying more than two (or an undefined number of) options (H.-H. Li & Ma, 2020; Niwa & Ditterich, 2008; Rahnev, 2020). Including a larger number of alternatives may not only reveal that the methodological tools developed for 2AFC tasks are insufficient, but also that the proposed mechanisms are wrong (H.-H. Li & Ma, 2020). Specifically, the context in which we make decisions might alter our subjective interpretation of the facts (Ariely & Wallsten, 1995; Northoff & Mushiake, 2020). One example is the attraction effect (Huber et al., 1982): when deciding between two alternatives (the focal options), the addition of a third one—similar to one of the focal alternatives regarding one attribute but inferior in another attribute—may increase the probability for choosing that focal option. Critically, this kind of context phenomena has been shown to play a role both in conceptual and perceptual processes (Trueblood et al., 2013), so they are thought to be a fundamental part in our decision processes. Moreover, it has recently been proposed that the allocation of attention—modulated by the stimuli location (Winter & Peters, 2021)—might also give rise to context influence on decision-

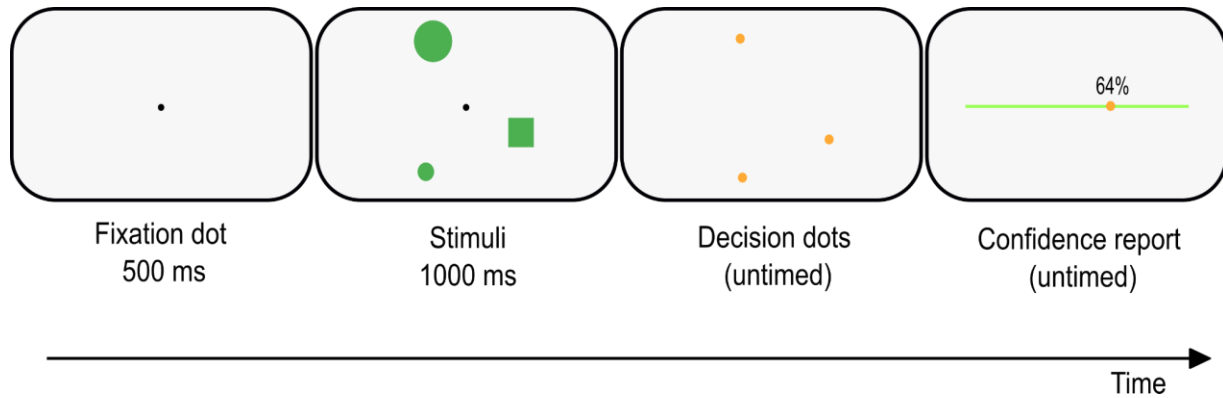
making. Nevertheless, partly due to the prevalence of 2AFC tasks paradigms, the impact of these effects on confidence remains unknown.

Building on these ideas we explored whether a phenomenon already described in the literature for likelihood judgments (Windschitl & Chambers, 2004), line-up identifications (Charman et al., 2011) and associative memory (Hanczakowski et al., 2014) takes place in multi-alternative perceptual decision-making. This effect is defined as “*the tendency to become more confident that a chosen response option is correct if it is surrounded by implausible response options*” (Charman et al., 2011, p. 479) and it is called the “dud-alternative effect”. Bayesian models of confidence predict that confidence should remain virtually invariant when adding irrelevant alternatives, because these hardly affect the probability of being correct. Moreover, they practically do not affect the difference between the posterior probabilities that the two best options are correct, a recently proposed computation for confidence in multi-alternative tasks (H.-H. Li & Ma, 2020). On the other hand, the dud-alternative effect found in non-perceptual tasks predicts that confidence should paradoxically increase.

We investigated the influence of irrelevant alternatives on confidence in three perceptual decision making tasks. In contrast to other decision making processes, perceptual decision making tasks are mainly based on incoming sensory information. In Experiment 1 we studied the effect of a third, irrelevant stimulus on confidence and contrasted our data with predictions from four computational models. In Experiment 2 we replicated the results from Experiment 1 and, based on the models’ simulations, extended them up to three irrelevant stimuli. In Experiment 3 we explored how stimuli-dependent our results are, using a task recently introduced to study confidence in a three alternative decision making context (H.-H. Li & Ma, 2020). In Experiments 4 and 5, we tested whether the differences found in the two previous paradigms are due to differences in the stimuli exposure duration.

## **2. Experiment 1**

We designed a size discrimination task to evaluate the effect of the presence of a third, weak alternative (i.e. dud alternative) in confidence (Fig. 1). This task allowed us to manipulate the subjective value of the alternatives, making them more or less eligible only by varying their relative size.



**Fig. 1.** Size discrimination task. Participants had to decide which was the largest shape. The size of the stimuli varied in every trial, and the relative size of the two largest shapes controlled the difficulty (established in 5 levels). Half of the trials had 2 alternatives and the other half had 3 alternatives, making up a total of 120 trials. The third alternative was very small when present, and varied in size (see Methods). After choosing the largest shape, participants had to report how confident they felt about their decision on a scale from 0% (not confident at all) to 100% (completely confident).

## 2.1 Materials & methods

The task was programmed in JavaScript using the library jQuery. It ran on a JATOS (Lange et al., 2015) server. The experiment could be run on mobile devices or desktop computers.

### 2.1.1 Participants

101 participants took part in Experiment 1 (63% females; mean age = 29.46, sd = 8.83). The study was approved by the ethical committee of the Institute of Psychological Research (IIPsi - CONICET - Córdoba, Argentina). Participants should read and accept an informed consent prior to the experiment. All participants reported no psychiatric, illegal drug consumption or neurological history. Instructions were written on screen prior to the experiment. Thirty four % of the sample performed the experiment on a mobile device, whereas the rest performed it on a computer.

### 2.1.2 Experimental design

The experiment consisted of a decision making task where participants had to decide which of two or three geometric shapes was the largest. It had 120 trials, 60 with two alternatives and 60 with three alternatives. The shapes were circles and squares, and the two largest shapes were always a circle and a square (to make the comparison harder). On half of the trials a circle was the correct option, and on the other half a square. The third alternative, when present, was randomly a square or a circle, and it was much smaller than the other 2 shapes in order to make it easily discarded (in fact, it was only chosen on 7 out of 11751 trials). The size of the largest shape was sampled from a normal

distribution with a mean value that depended on screen size (7500px<sup>2</sup> for a screen with a width size  $\geq 600$ px; 6500px<sup>2</sup> for a screen with a width size  $< 600$ px and  $\geq 400$ ; 5500px<sup>2</sup> for a screen with a width size  $< 400$ px) and a standard deviation of one fourth of the mean value. The second largest shape area was set to the 0.7, 0.8, 0.9, 0.93 or 0.95 of the area of the stimulus 1, and the third alternative' area (if present), was set to the 0.1, 0.2, 0.3, 0.4, 0.5 or 0.6 of the area of the stimulus 2. Consequently, there were 60 trials with 2 alternatives (of which there were 12 trials per each size of the second largest alternative) and 60 trials with 3 alternatives (of which there were 2 trials for each combination of size of the third and second largest alternative) (Table 1). Stimuli were randomly displayed in 3 equispaced positions (120 degrees) located in a circular array of a radius that varied with the screen size. The stimuli-array was randomly rotated so the positions changed across trials. Shapes were shown for 1 s, and the participants could respond by clicking the chosen shape or, once disappeared, by clicking a small circular dot marking the position. After that, participants had to report their confidence level on the decision on a scale from 0% (not confident at all) to 100% (completely confident). Participants had to move a dot that was initially hidden (until they moved the cursor) and appeared in the cursor's position. Specifically, in the confidence instructions we stated (in spanish in the actual experiment): "Once you have picked the shape that you think is the largest you will have to report your degree of confidence in that choice, that is, how sure you are that you picked the correct option" [...] "the scale goes from 0% (COMPLETELY UNSURE, that implies that you don't have confidence at all in your decision of which was the largest shape) to 100% (COMPLETELY SURE, that implies that you are fully confident about your decision of which was the largest shape). YOU CAN USE INTERMEDIATE VALUES, the idea is that you report your confidence in your choice in the most precise way possible". On the first 3 trials we included, on the top of the screen, the question "How sure are you?".

Table 1. Task structure.

Third alternative size (area3/area2)	Second alternative size (area2/area1)				
	0.7	0.8	0.9	0.93	0.95
Absent	12 trials	12 trials	12 trials	12 trials	12 trials
0.1	2 trials	2 trials	2 trials	2 trials	2 trials
0.2	2 trials	2 trials	2 trials	2 trials	2 trials
0.3	2 trials	2 trials	2 trials	2 trials	2 trials
0.4	2 trials	2 trials	2 trials	2 trials	2 trials
0.5	2 trials	2 trials	2 trials	2 trials	2 trials

0.6	2 trials	2 trials	2 trials	2 trials	2 trials
-----	----------	----------	----------	----------	----------

### 2.1.3 Data analysis

We excluded 2 participants from subsequent analysis due to low overall performance (8 and 66% overall accuracy; the median performance for the sample was 85% with an interquartile range (Q3-Q1) of 6.7%). The definitive sample consisted of 99 participants. Our sample size was based on a pilot study with 20 participants in which we observed our main findings. We excluded trials with response times (RT) shorter than 200 ms and larger than 10 s. These exclusion criteria were not pre-registered, but including the discarded data does not modify the results. We conducted repeated measures ANOVAs and Tukey HSD post hoc tests (both with the software Statistica). Our predefined p-value for statistical significance was 0.05. We defined task difficulty as the ratio between the area of the two largest shapes. The ANOVA for incorrect trials was done with the highest levels of difficulty (0.9, 0.93, 0.95) because there were not enough incorrect trials in easier conditions (0.7 and 0.8).

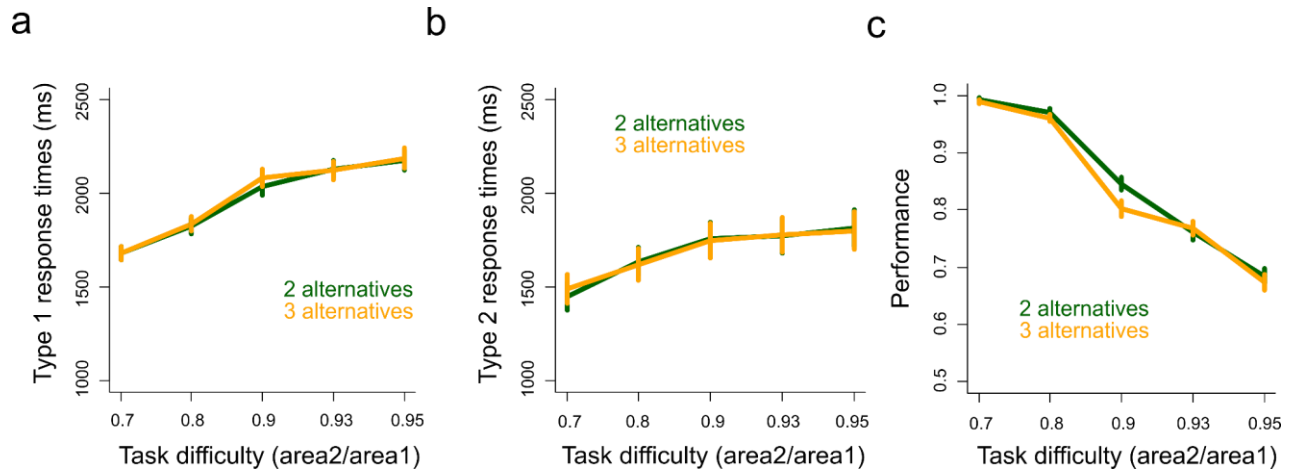
## 2.2 Results

### 2.2.1 Response times

Task difficulty had a significant impact on the response times of both the decisions and the confidence reports. Higher difficulty was associated with larger RT ( $F_{4, 392} = 130.95$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.57$  - decisions - Fig. 2a;  $F_{4, 392} = 19.36$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.16$  - confidence reports - Fig. 2b). The presence of a dud alternative in half of the trials did not affect RT in none of the tasks ( $F_{1, 98} = 0.79$ ,  $p = 0.37$ ,  $\eta_p^2 = 0.008$  - decisions - Fig. 2a;  $F_{1, 98} = 0.002$ ,  $p = 0.96$ ,  $\eta_p^2 = 0.00002$  - confidence reports - Fig. 2b).

### 2.2.2 Performance

Participants' performance, as expected, decreased as task difficulty increased irrespective of the number of alternatives ( $F_{4, 392} = 374.31$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.79$ ) (Fig. 2c). We found a marginally significant effect of the inclusion of the third alternative on performance, restricted to the middle difficulty ( $F_{1, 98} = 4.04$ ,  $p = 0.047$ ,  $\eta_p^2 = 0.03$ ) (Fig. 2c). We didn't find a significant interaction between the number of alternatives and the task difficulty ( $F_{4, 392} = 1.79$ ,  $p = 0.12$ ,  $\eta_p^2 = 0.017$ ) (Fig. 2c).

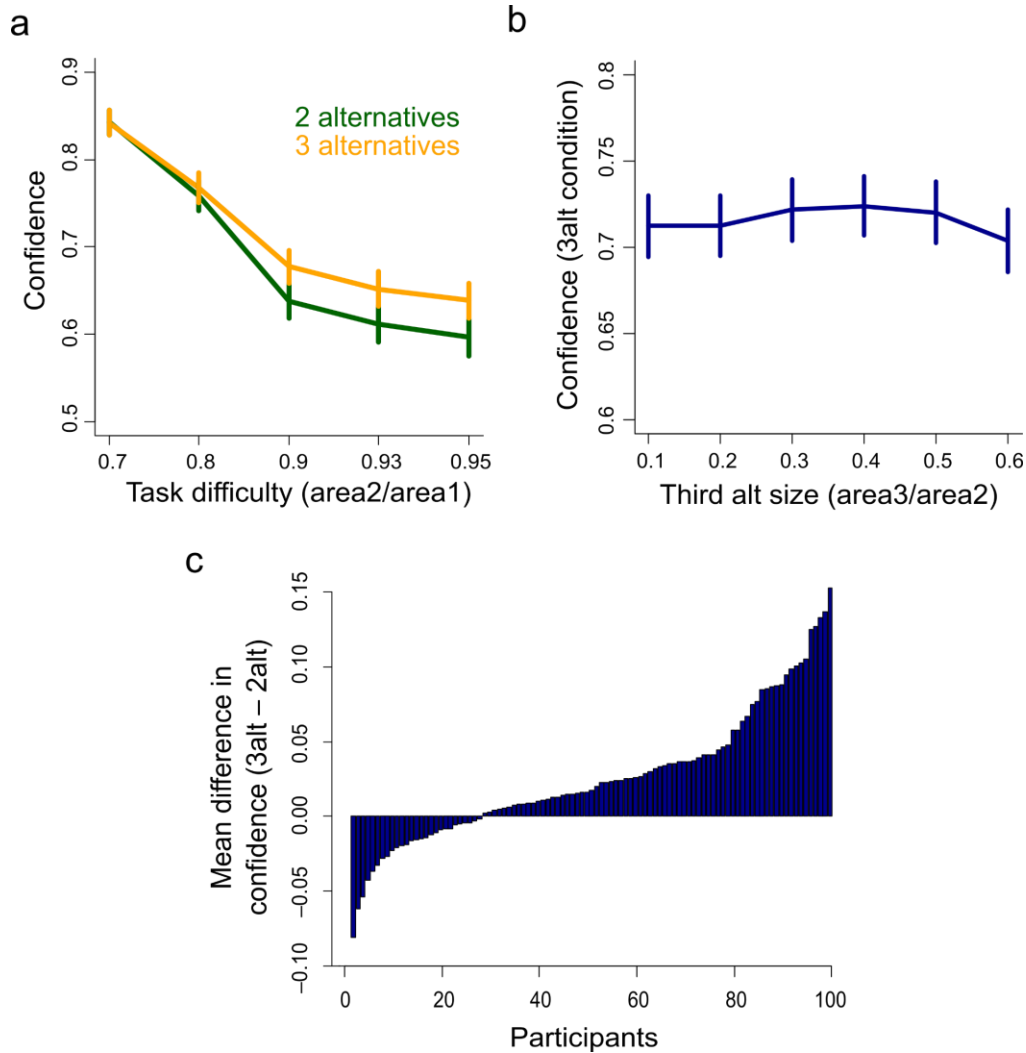


**Fig. 2.** The dud alternative did not have an effect on response times neither in (a) the decision task nor in (b) the confidence report. (c) The dud alternative only decreased task performance in difficulty 0.9. In all figures vertical bars refer to s.e.m. and “area2” and “area1” refer to the area of the second largest shape and the largest shape, respectively.

We also analyzed whether the shape of the third alternative had any effect on the decisions (i.e, a context effect regarding “square” and “circle” choices). In other words, we tested whether a squared (circled) third alternative made subjects more likely to choose a square (circle) as the largest figure. For trials where the chosen shape was a square, we found an interaction between the 2-alternative condition and the presence of the squared third alternative ( $F_{4, 392} = 3.66, p = 0.006, \eta_p^2 = 0.04$ ). When comparing between 2 or 3-alternative conditions on the same level of difficulty, a Tukey HSD post-hoc test showed a significant difference only on the highest level of difficulty ( $p = 0.02$ ). This means that participants were more likely to choose a square when the dud-alternative was also a square on that particular difficulty level. With respect to trials where the chosen shape was a circle, we again found an interaction between the 2-alternative condition and the presence of a circular third alternative ( $F_{4, 392} = 2.72, p = 0.03, \eta_p^2 = 0.03$ ). However, a Tukey HSD post-hoc test showed no significant difference between the same difficulty conditions (i.e. participants were not more likely to choose a circle if the third alternative was a circle).

### 2.2.3 Confidence

Confidence, just like performance and as expected, decreased with increasing levels of task difficulty ( $F_{4, 392} = 233.47, p < 0.000001, \eta_p^2 = 0.7$ ) (Fig. 3a). Importantly, we found a significant increment of confidence in the three-alternative condition ( $F_{1, 98} = 33.25, p < 0.000001, \eta_p^2 = 0.25$ ) (Fig. 3a and 3b). Overall, 72 out of the 99 participants had an increased confidence in the three-alternative condition (Fig. 3c) as compared with the two-alternative condition. We also found a significant interaction between the difficulty of the task and the presence of a weak alternative ( $F_{4, 392} = 6.85, p = 0.00002, \eta_p^2 = 0.06$ ) (Fig. 3a).

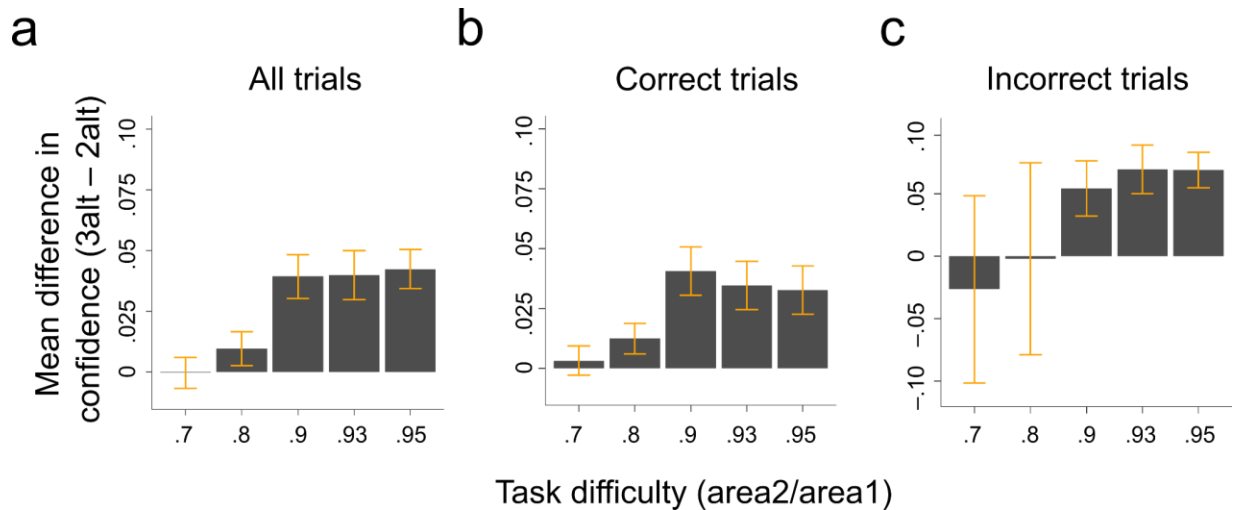


**Fig. 3.** (a) Confidence diminishes as a function of task difficulty but decreases less when a dud alternative is present (specifically at high levels of difficulty). (b) No effect was found regarding the size of the irrelevant alternative on confidence (i.e., confidence increased equally irrespectively of the third stimuli size). (c) Difference in confidence (2 vs 3 alternatives) per participant. Each line in (b) represents the change in confidence for each participant (considering all difficulty levels for each condition). A positive value means that confidence was higher when the dud alternative was present, whereas a negative value means that, conversely, confidence decreased in that condition.

The effect of increased confidence is present both in correct and incorrect trials ( $F_{1, 98} = 26.65$ ,  $p = 0.000001$ ,  $\eta_p^2 = 0.21$  - correct trials;  $F_{1, 61} = 22.2$ ,  $p = 0.00001$ ,  $\eta_p^2 = 0.27$  - incorrect trials) (Fig. 4). Comparing the confidence increment between correct and incorrect trials (on the 3 highest levels of difficulty) no differences were found ( $F_{1, 61} = 3.82$ ,  $p < 0.055$ ,  $\eta_p^2 = 0.06$ ). Regarding the size of the third alternative, we found a significant effect ( $F_{6, 582} = 4.73$ ,  $p = 0.0001$ ,  $\eta_p^2 = 0.05$ ). A Tukey HSD post hoc test showed that the significant differences were between the 2 alternative condition and the conditions where the size of the dud alternative was 0.07 ( $p = 0.048$ ), 0.21 ( $p = 0.0007$ ), 0.28 ( $p = 0.005$ ) and 0.35 ( $p = 0.001$ ) of the area of the largest stimulus. This means that no



differences were found across the third stimulus sizes (all differences are with respect to the 2 alternative condition). In other words, confidence increased irrespectively of the size of the dud-alternative (Fig. 3b).



**Fig. 4.** Confidence increases when the third alternative is present. All panels depict the confidence difference between 3-alternative and 2-alternative conditions. The figure shows confidence difference for (a) all trials, (b) correct trials and (c) incorrect trials. Large s.e.m. in (c) at low difficulties (difficulties 0.7 and 0.8) are due to low numbers of incorrect responses.

We did not find an effect of the shape of the third alternative on confidence. That is, when considering if the dud alternative was a circle or a square only on the 3-alternative condition, no difference was found in confidence neither for trials where the chosen shape was a circle ( $F_{1, 63} = 0.16, p = 0.69, \eta_p^2 = 0.003$ ) nor for trials where the chosen shape was a square ( $F_{1, 83} = 1.69, p = 0.2, \eta_p^2 = 0.02$ ).

## 2.3 Discussion

The results of Experiment 1 extend the “dud-alternative” effect to a perceptual decision making task: confidence level increased with the addition of a small, clearly incorrect alternative. This effect is remarkably important because it implies that confidence does not directly reflect the probability of being correct, as stated by classical views (Meyniel et al., 2015; Sanders et al., 2016), and even deviates from recent models such as the difference of the probabilities of being correct of the two best options (H.-H. Li & Ma, 2020). According to these models, the addition of irrelevant alternatives should not affect confidence (because they hardly affect the probabilities of the rest of the alternatives), and, in any case, it should decrease it. However, the opposite pattern is observed in Experiment 1.

The dud-alternative had a small effect on performance. The effect is only restricted to a middle-level difficulty, where participants’ performance only decreased minimally. So it is

likely that the task was not more difficult with the addition of the third alternative. The lack of effect in response times is consistent with this explanation, as more difficult tasks are expected to generate larger response times (Ratcliff et al., 2016). In consequence, the effect of the inclusion of the irrelevant alternative is mainly restricted to confidence.

The design of Experiment 1 allows for the possibility of testing a specific kind of “decoy effect”: the probability of choosing a geometrical shape as the largest one increases when the third alternative is of the same shape (Huber et al., 1982; Trueblood et al., 2013). However, we only found this effect for square choices, restricted to the highest level of difficulty. Moreover, this effect did not interact with the dud-alternative effect, suggesting that both are independent contextual effects.

Studies focused on the dud-alternative effect propose two main accounts for this phenomenon (Charman et al., 2011; Hanczakowski et al., 2014; Windschitl & Chambers, 2004). The first one is the “Average-residual” account: confidence reflects the difference between the evidence supporting the chosen option and the average of the evidence supporting the unchosen options (Eq. 3, see below). According to this idea, confidence increases with the addition of a dud alternative because its presence decreases the average of the evidence in favor of the unchosen options. The second proposed explanation for the dud effect is the “Contrast” account: confidence is obtained by a series of pairwise comparisons, where observers take the differences between the evidence supporting the chosen alternative and the evidence supporting each of the rest of the alternatives and sum them up (Eq. 4, see below). Confidence therefore increases with the presence of an irrelevant alternative, since there is another favorable comparison for the chosen option. We decided to formalize and test these verbal explanations in two computational models: the “Average-residual” model and the “Contrast” model. We compared these two models with the “Max” model –that states that confidence reflects the probability of being correct (Eq. 2, see below)– (H.-H. Li & Ma, 2020; Meyniel et al., 2015; Sanders et al., 2016) and the Difference model –that states that confidence reflects the difference between the probabilities of being correct of the two best alternatives (Eq. 1, see below)– (H.-H. Li & Ma, 2020).

### **3. Computational models**

In order to evaluate whether the predictions of different models of confidence could fit our empirical results of Experiment 1 —and to propose some venues for future models— we carried out simulations for 4 models: the Difference model (H.-H. Li & Ma, 2020), the Max model (H.-H. Li & Ma, 2020; Meyniel et al., 2015; Sanders et al., 2016), the Contrast model (Charman et al., 2011; Hanczakowski et al., 2014; Windschitl & Chambers, 2004)

and the Average-residual model (Charman et al., 2011; Hanczakowski et al., 2014; Windschitl & Chambers, 2004).

### 3.1 Materials & methods

#### 3.1.1 Computational modeling.

All models were developed under a Bayesian modeling approach (Ma, 2019). To set the generative model, we defined stimuli sizes as in Exp. 1. We simulated the internal responses on each trial. We assumed that observers make a noisy measurement  $x_i$  of each stimulus  $S_i$ . This measurement was modeled using a Gaussian distribution with mean on the actual value of the stimuli and standard deviation  $\sigma$ . Ideal observers compute the posterior probability that each stimuli is the largest, formally:  $p_i = p(S_i = \max(S_1, S_2, S_3) | (x_1, x_2, x_3, s))$ . As some variability in behavior is due to a “late noise” at the level of the decision variable (H.-H. Li & Ma, 2020), we assumed that observers do not maintain the exact posterior probability but a noisy version of it,  $q_i$ , modeled as a random sample of a Dirichlet distribution centered on the true posterior probabilities with a spread controlled by a parameter  $\alpha$  (H.-H. Li & Ma, 2020). We assumed participants choose the stimulus with the highest  $q(S_i | x_1, x_2, x_3, s)$ . For readability, from now on we will refer to these noisy posterior probabilities as simply the posterior probabilities.

We simulated confidence levels according to four different models (Fig. 5a). For the Difference model (Diff), confidence level is the result of the difference between the two highest posterior probabilities. In the Max model confidence level is the larger posterior probability. This model corresponds to the Bayesian Confidence hypothesis, stating that confidence reflects the probability that the decision is correct. The Contrast model and the Average-residual model are computational implementations of the two mechanisms proposed in the dud alternative literature to account for the effect (Charman et al., 2011; Windschitl & Chambers, 2004). The Contrast model states that confidence is obtained by a series of pairwise comparisons between the chosen option and the remaining. Following this, we modeled confidence by the sum of the differences between the largest posterior probability and all other posterior probabilities. The Average-residual model proposes that confidence reflects the evidence favoring the chosen option minus the average evidence of the remaining options. Therefore, we modeled confidence as the difference between the alternative with the highest posterior probability and the mean of the remaining posterior probabilities. Formally:

$$\text{Diff model: } \textit{confidence} = q_1 - q_2 \quad (\text{Eq. 1})$$

$$\text{Max model: } \textit{confidence} = q_1 \quad (\text{Eq. 2})$$

$$\text{Average-residual model: } \textit{confidence} = q_1 - \frac{(q_2 + q_3)}{2} \quad (\text{Eq. 3})$$

$$\text{Contrast Model: } \textit{confidence} = (q_1 - q_2) + (q_1 - q_3) \quad (\text{Eq. 4})$$

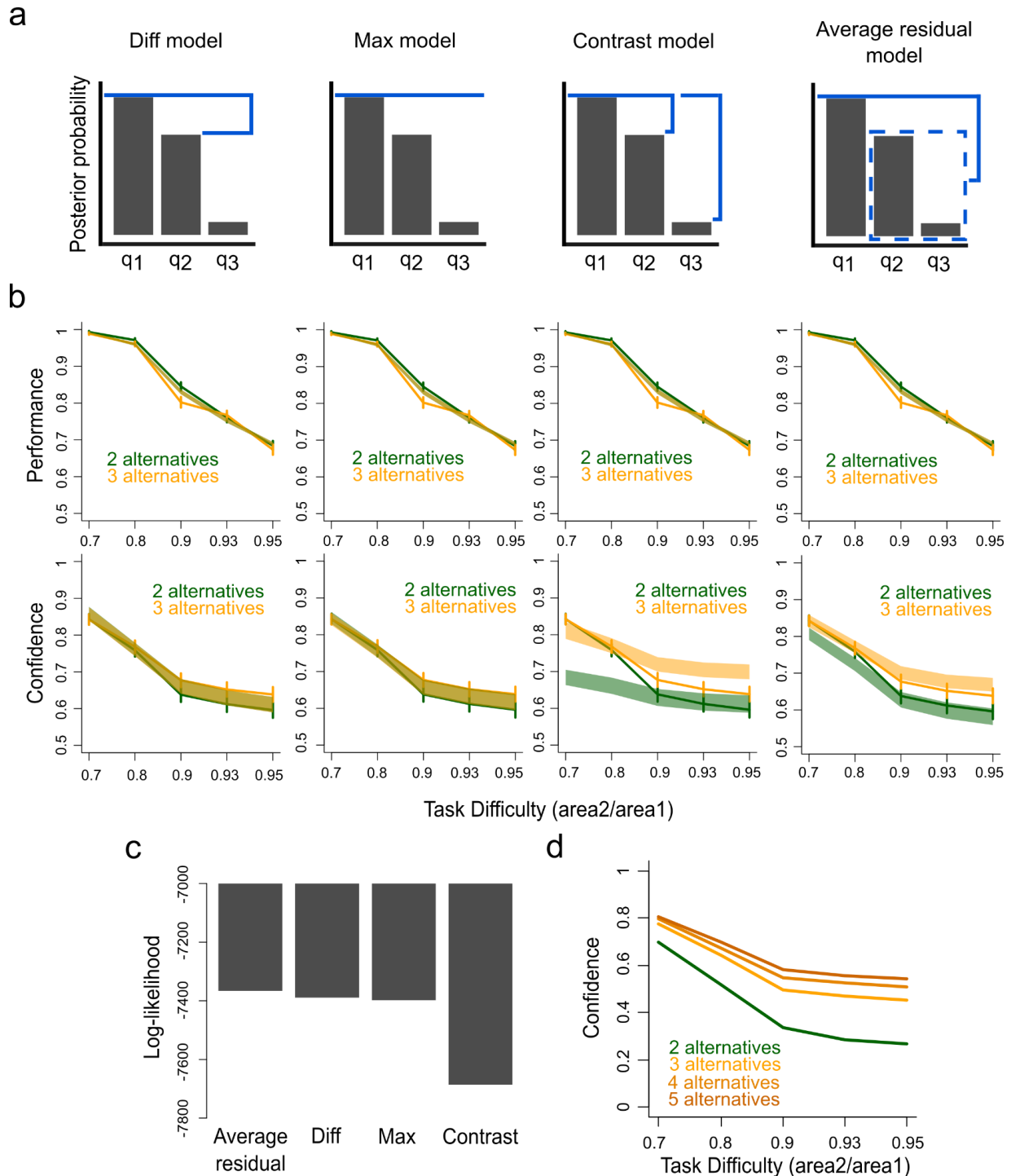
### 3.1.2 Model fitting

We fitted the models' free parameters separately for each participant's data (decisions and confidence) by maximizing the likelihood of the parameters. Formally, we maximized  $L(\theta|data) = \log p(data | \theta)$ , where  $L(\theta|data)$  is the log-likelihood of the parameters given the data,  $data$  is the decisions and the mean confidence level on each condition, and  $\theta$  the parameters ( $\sigma, \alpha, \beta_0$  and  $\beta_1$ ). The free parameters were sensory noise ( $\sigma$ ), decision noise ( $\alpha$ ) and two parameters controlling the intercept ( $\beta_0$ ) and slope ( $\beta_1$ ) of the linear transformation that maps the confidence output of the model to the confidence data of the subject (using alternative mappings does not change the computational modeling results, see Supplementary material). We first fitted  $\sigma$  and  $\alpha$  using the participant's decisions and then used these two parameters as fixed to fit confidence levels. For that, we simulated 10000 trials and calculated the proportion of trials where the model decision is equal to the decision of the participant. These numbers (one per trial) are an approximation of the data probability given the parameter values. We summed the log of these numbers, thus computing the log-likelihood of the parameters given the observed data. To find the best fitting parameter values we used the R function *optim* with the simulated annealing method to minimize the negative log-likelihood of the parameters' values given the observed data (which is equivalent to maximizing the likelihood of the parameters' values given the observed data). We then used the best  $\sigma$  and  $\alpha$  values as fixed values for fitting  $\beta_0$  and  $\beta_1$ . We simulated 100000 trials per model taking the mean confidence by 1000 trials. Confidence data was divided by 100 to transform it to the scale of 0 to 1 and then rounded to 1 decimal. We fitted the model to the mean confidence level on each condition for each participant (fitting the whole trial distribution instead of the mean level did not qualitatively change our results, see Supplementary material). To fit confidence, we ran three optimization realizations with different starting points of the parameters, and kept the best estimation. Using the resulting parameters values we simulated 100000 trials according to each model taking the mean confidence by 1000 trials and calculated their mean performance and confidence to compare these models' predictions to the participants' behavior. As all the models have the same number of free parameters we directly compared them using the summed log-likelihood across participants.

To evaluate the ability of our method to detect the true parameters for each subject, we performed parameter recovery by simulating, with the Average-residual model, the same amount of data that we had by participant (120 trials; 12 per condition) using values of  $\sigma, \alpha, \beta_0$  and  $\beta_1$  sampled from our data and then fitting models to this simulated data with the mentioned procedure. The Pearson correlation between the true parameters and the estimated parameters was 0.83 for  $\sigma$  ( $p < 0.0001$ ), 0.58 for  $\alpha$  ( $p < 0.0001$ ), 0.99 for  $\beta_0$  ( $p < 0.0001$ ) and 0.99 for  $\beta_1$  ( $p < 0.0001$ ). This suggests that our method successfully recovers the true parameters underlying each participant data.

### 3.2 Results

For both the Max model (summed log-likelihood = -7398.2) and the Diff model (summed log-likelihood = -7389) the presence of a third irrelevant option does not affect confidence (Fig. 5b). In contrast, for both the Contrast model (summed log-likelihood = -7686.03) and the Average-residual model (summed log-likelihood = -7365.97) confidence increases with the presence of an irrelevant option (Fig. 5b). However, the Contrast model shows a constant (difficulty-independent) confidence increase, whereas the Average-residual model accounts for the pattern shown in our data: the difference in confidence between three and two alternatives increases with the difficulty. Furthermore, if we extend simulations to a context with more dud alternatives, the Average-residual model predicts that confidence should increase monotonically with the number of dud alternatives (Fig. 5d).



**Fig. 5.** (a) Sketches of confidence computation for each model. In the Average residual Model, confidence is obtained by the difference between the highest posterior probability and the mean of the remaining posterior probabilities. Confidence reflects the probability of being correct in the Max Model. The Difference Model states that confidence reflects the difference between the two best posterior probabilities. Finally, in the Contrast Model confidence is the result of the sum of the differences between the highest posterior probability and each of the remaining posterior probabilities. (b) Model fits for performance (first row) and confidence (second row). Both the max model and the Diff model show that

confidence should remain invariant when a dud-alternative is added to the decision context. Conversely, the Average-residual model and the Contrast model show that confidence should be higher. However, only the Average-residual model replicates the pattern found in our experiment. Shaded regions are the standard error of the mean of model fits. (c) The log-likelihood of each model. The Average-residual model is the best fitting model regarding our data. (d) The Average-residual model predicts that confidence should increase with the number of dud alternatives, as these alternatives reduce even more the average of the remaining options.

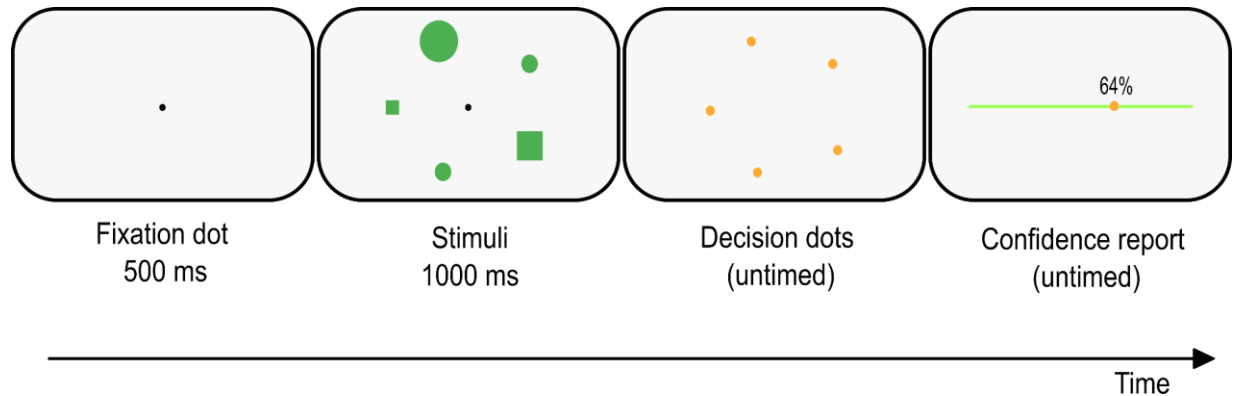
### **3.3 Discussion**

Among all tested models, both the Average-residual model and the Contrast model can recover the increment in confidence in the 3-alternative condition. However, only the Average-residual predicts a lower effect on easier trials. Contrary, both the Max model and the Diff model predict the opposite pattern: confidence remains the same when more alternatives are added into the decision context.

The Average-residual model predicts that confidence should be higher with more alternatives only when these alternatives are dud-alternatives, i.e. when the probability of these alternatives of being correct is close to zero (according to the model, if the extra alternatives are not dud-alternatives they will decrease the probability of being correct of the chosen option and then confidence will be lower than in 2-alternative case, see Supplementary Fig. 3a). This is because, with the addition of irrelevant alternatives, the probabilities of being correct of the competitive options remain the same while the average of the remaining options is lower. As a consequence, the model predicts that confidence increases monotonically with the number of dud-alternatives, since these alternatives progressively lower the average of the probabilities of being correct of the unchosen options (Supplementary Fig. 3b). We tested for this possibility in the next experiment.

## **4. Experiment 2**

The Average-residual model predicts that confidence should increase monotonically with the number of dud-alternatives, because the presence of more irrelevant alternatives decreases the average of posterior probabilities of non-chosen alternatives with a minimal effect on the posterior probabilities of the competing alternatives (Fig. 5d). In this second experiment we not only aimed to replicate the results of Experiment 1 but to see whether confidence increases with the number of dud alternatives (Fig. 6).



**Fig. 6.** Size discrimination task. Participants had to decide which one of the shapes was the largest. Stimuli size varied in every trial, and the relative sizes of the two largest shapes controlled the difficulty (established in 5 levels). There were 4 conditions: 2, 3, 4 and 5 alternatives, each one with 120 trials. After that decision, participants had to report their confidence level on a scale from 0% (not confident at all) to 100% (completely confident). Only two alternatives competed for the correct answer, the others (when present) were relatively small and easily discarded.

## 4.1 Materials & methods

As in Experiment 1, the task was programmed in JavaScript using the library jQuery and conducted online on a JATOS (Lange et al., 2015) server. Experiment 2 involved more experimental conditions and, thus, more trials. To guarantee participants' attention during the task, the experimenter made a video call and remained available for the duration of the experiment.

### 4.1.1 Participants

18 participants took part in this experiment (62% females; mean age = 27.17, sd = 4.77). The study was approved by the ethical committee of the Institute of Psychological Research (IIPsi - CONICET - Córdoba, Argentina). Participants should read and accept an informed consent prior to the realization of the experiment. All participants reported no psychiatric, illegal drug consumption or neurological history. The tasks' instructions were written on screen prior to the experiments. All participants performed the task on a computer. Each participant received a payment of roughly 4 US dollars.

### 4.1.2 Experimental design

The design of Experiment 2 was similar to that of Experiment 1 but involving a larger number of conditions: 480 trials including 120 trials of 2, 3, 4 or 5 alternatives. As in Experiment 1, only two alternatives were large enough to compete for the correct answer; the others were much smaller in order to make them easily discarded (irrelevant alternatives). In trials where the irrelevant alternatives were present, they all had the same size, and each one was randomly a square or a circle. These dud alternatives also varied



in size (as in Experiment 1). Participants had to report their confidence level in the decision in the same way as in Experiment 1.

#### 4.1.3 Data analysis

No subject was excluded from the analysis. We followed a similar analysis strategy than in Exp 1 (including the excluded trials does not modify the results). We excluded the easiest level of the task from the performance analysis because one category (the one with 5 alternatives) had perfect performance. The dissociation between correct and incorrect trials carried out in Experiment 1 was not possible because there were not enough incorrect trials.

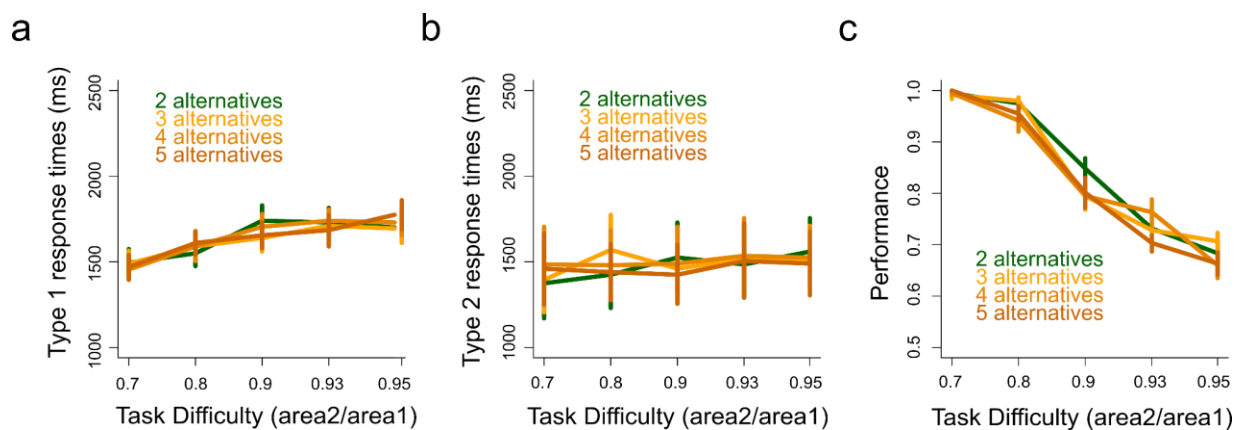
## 4.2 Results

### 4.2.1 Response times

Decisions RT increased with difficulty ( $F_{4, 68} = 23.47, p < 0.000001, \eta_p^2 = 0.58$ ) (Fig. 7a). This effect was not found in confidence reports RT ( $F_{4, 68} = 1.59, p = 0.18, \eta_p^2 = 0.08$ ) (Fig. 7b). The weak alternatives did not impact the RT on either of the tasks ( $F_{3, 51} = 0.26, p = 0.84, \eta_p^2 = 0.01$  - decisions - Fig. 7a;  $F_{3, 51} = 0.57, p = 0.63, \eta_p^2 = 0.03$  - confidence report - Fig. 7b).

### 4.2.2 Performance

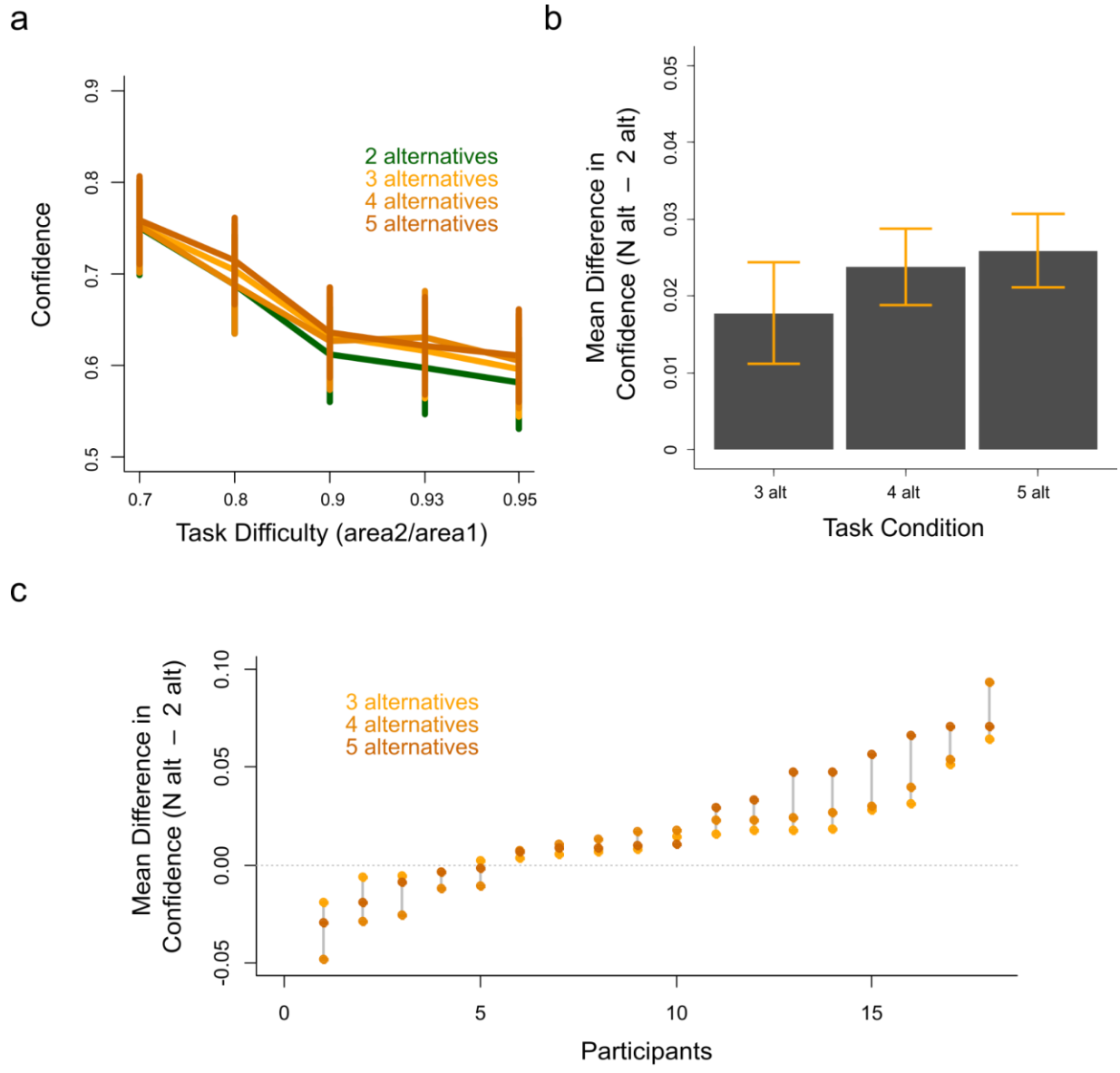
Regarding task performance, participants' accuracy decreased as the difficulty increased ( $F_{3, 51} = 90.45, p < 0.000001, \eta_p^2 = 0.84$ ) (Fig. 7c). Contrary, the dud alternatives did not affect participants' performance ( $F_{3, 51} = 2.62, p = 0.06, \eta_p^2 = 0.13$ ) (Fig. 7c).



**Fig. 7.** As in Experiment 1, dud alternatives did not have an effect in RT, neither in (a) decisions or in (b) confidence reports. (c) Performance did not vary with the addition of dud alternatives.

### 4.2.3 Confidence

Confidence level decreased with task difficulty ( $F_{4, 68} = 54.63, p < 0.000001, \eta_p^2 = 0.76$ ) (Fig. 8a). Replicating the main finding in Experiment 1 confidence increased with the presence of irrelevant alternatives ( $F_{3, 51} = 3.81, p = 0.01, \eta_p^2 = 0.18$ ) (Fig. 8a). We conducted a Tukey HSD post hoc analysis, showing that there was a significant difference between confidence with 2 and 5 alternatives ( $p = 0.008$ ). To further explore this result, we conducted ANOVAs separately for each remaining conditions (3 and 4 alternatives vs 2 alternatives). We found a significant effect on confidence for the 3-alternative condition ( $F_{1, 17} = 9.06, p = 0.007, \eta_p^2 = 0.34$ ) not detected by the post hoc test. No interaction was found on this condition ( $F_{4, 68} = 0.5, p = 0.72, \eta_p^2 = 0.03$ ). For the condition with 4 alternatives we found a marginally significant effect ( $F_{1, 17} = 3.58, p = 0.075, \eta_p^2 = 0.17$ ) and a significant interaction between the amount of alternatives and the task difficulty ( $F_{4, 68} = 2.61, p = 0.04, \eta_p^2 = 0.13$ ). We did not replicate the interaction between difficulty and the irrelevant alternatives found in Experiment 1 ( $F_{12, 204} = 1.13, p = 0.33, \eta_p^2 = 0.06$ ) (Fig. 8a). Confidence was not affected by the number of dud-alternatives ( $F_{2, 34} = 0.95, p = 0.39, \eta_p^2 = 0.05$ ) (Fig. 8a and Fig. 8b). Thirteen out of eighteen participants showed the effect of increased confidence in the dud alternative conditions (Fig. 8c). There was a significant effect of the dud alternative size on confidence ( $F_{6, 102} = 2.49, p = 0.03, \eta_p^2 = 0.13$ ).



**Fig. 8.** (a) As in Experiment 1, confidence decreased with task difficulty but increased when weak alternatives were present. (b) Confidence difference between the 3, 4 and 5 alternative conditions and 2-alternative condition considering the highest levels of difficulty (0.9, 0.93 and 0.95). (c) Average difference in confidence by condition and participant.

### 4.3 Discussion

In Experiment 2 we replicated the dud-alternative effect found in Experiment 1. However, we did not find evidence that adding more dud-alternatives influences confidence. Although this constitutes a challenge for the Average-residual model, one should keep in mind that the prediction of the model is that the increase in confidence becomes smaller with the addition of each dud alternative (because the average of the probabilities of the non-chosen options start to decrease less with each added alternative), making this

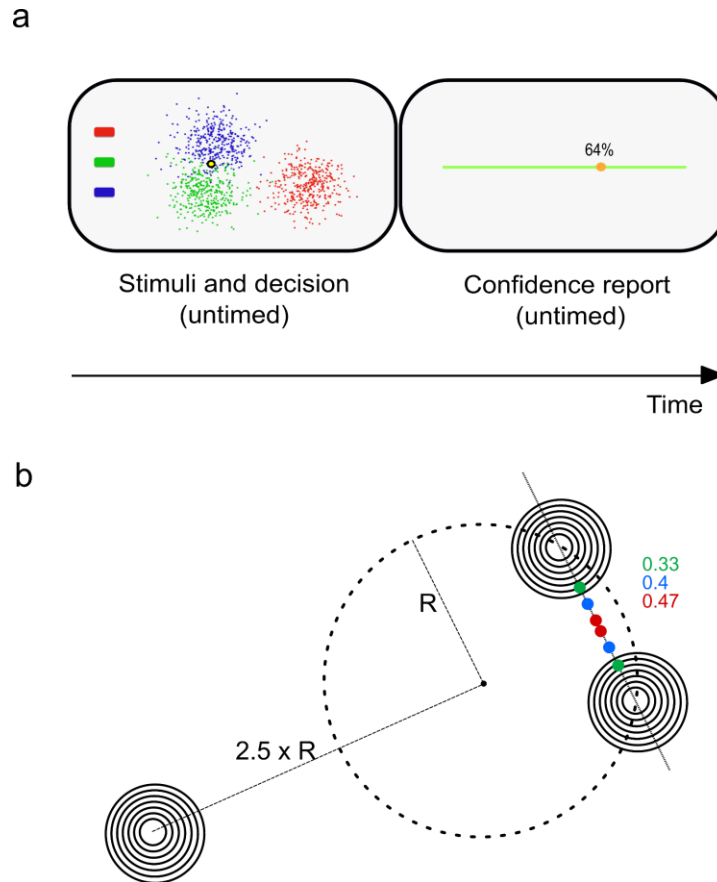
effect, if it exists, much difficult to detect. Moreover, with higher levels of sensory or decision noise the model predicts no difference between conditions. Further research is needed to evaluate if the monotonic increase in confidence actually exists and if the Average-residual model can account for its presence or absence by fitting it to participants' behavior.

Interestingly, performance was not affected by the inclusion of the dud-alternatives. This confirms the notion that these alternatives are not making the task harder (despite the small but significant effect on performance found in Experiment 1).

We extended the dud-alternative effect to a perceptual decision making task in Experiments 1 and 2. However, we wanted to test if this effect was present in a different task, the one where the Diff model was developed (H.-H. Li & Ma, 2020), to evaluate whether the predictions of the Average-residual model hold even in the context where the Diff model was the best model. Therefore, we run Experiment 3.

## **5. Experiment 3**

To evaluate whether the dud-alternative effect replicates in a different multi-alternative task, we adapted the target categorization task from Li & Ma (2020) (Fig. 9).



**Fig. 9.** Target categorization task. (a) Participants decided which cloud of dots the yellow target dot belonged to. Half of the trials had three alternatives and half two. When present, the third cloud was far from the target in order to make it ineligible, following the logic of the previous two studies (red cloud in the figure). After the decision, participants reported their confidence level on a continuous bar. (b) The underlying structure of the task (see Materials & methods).

## 5.1 Materials & methods

As the two previous experiments, the third experiment was conducted online on JATOS (Lange et al., 2015) and programmed in JavaScript using the library jQuery.

### 5.1.1 Participants

63 participants took part in this experiment (62.5% females; mean age = 30.16, sd = 12.32). The study was approved by the ethical committee of the Institute of Psychological Research (IIPsi - CONICET - Córdoba, Argentina). Participants should read and accept an informed consent prior to the realization of the experiment. All participants reported no psychiatric, illegal drug consumption or neurological history. The tasks' instructions were written on screen prior to the experiment. All participants completed the experiment on a computer.

### 5.1.2 Experimental design

The experiment consisted of a decision making task where participants had to decide which cloud of dots a target dot belonged to. It had 120 trials, 60 with two alternatives and 60 with three alternatives (i.e., two or three clouds). Dots were normally distributed in space. The mean of the distributions were set in space such that the two main clouds were closer together. More specifically, the mean of these distributions were located in a circle of radius  $R$  centered at a fixation point and separated by an angle of 120 degrees. In trials where the third cloud was present, its mean was located at a distance  $2.5 \times R$  from the fixation point and at an angle of 120 degrees from each of the mean locations of the other two clouds. Each dot cloud had 375 dots. Dot size and standard deviation of the distribution was responsively set, according to the presentation screen. The target dot was yellow with a black border. The target was located in a segment that begins and ends at the mean values of the 2 competing clouds distributions. The position of the target was parameterized by a “task difficulty” variable  $d$  that takes values from 0 to 0.5, where 0 represents one of the extremes and 0.5 represents the middle, equidistant from the mean values of the distributions. We used  $d = \{0.33, 0.4, 0.47\}$  where 0.33 is the easiest and 0.47 the most difficult condition. See Fig. 9b for a graphical reference of the task. Stimuli remained on the screen until the participant made a decision, clicking on color coded screen buttons. Participants reported their confidence level on the decision on a continuous scale, as in Experiments 1 and 2. Similar to Experiments 1 and 2, the confidence instructions stated (spanish in the actual experiment): “your second task consists in reporting your degree of confidence in your choice, that is, how sure you are to have picked the correct option” [...] “the scale ranges from 0% (COMPLETELY UNSURE, that implies that you don’t have confidence at all in your decision to which cloud of dots did the yellow dot belonged to) to 100% (COMPLETELY SURE, that implies that you are fully confident about your decision to which cloud of dots did the yellow dot belonged to). YOU CAN USE INTERMEDIATE VALUES, the idea is that you report your confidence in your choice in the most precise way possible”. On the first 3 trials we included, on the top of the screen, the question “How sure are you?”.

### 5.1.3 Data analysis

We excluded 7 participants from the analysis (3 due to low performance -our accuracy cutoff point was an accuracy of 0.6-, and 4 due to lack of variability in the confidence report (confidence level at 100% in > 90% of the trials). The final sample consisted of 52 participants (including all participants does not modify the results). We excluded trials with RT lower than 200ms both for decisions and confidence reports. We excluded trials with a response time greater than 20 s instead of 10 s as in our previous tasks since RTs are larger in this task. These exclusion criteria were not pre-registered, but including the discarded data does not modify the results. We conducted repeated measures ANOVAs and Tukey HSD post hoc tests (both with the Statistica software) to estimate the impact

of the difficulty of the task and the dud alternatives in RT, performance and confidence. Our predefined p-value for statistical significance was 0.05.

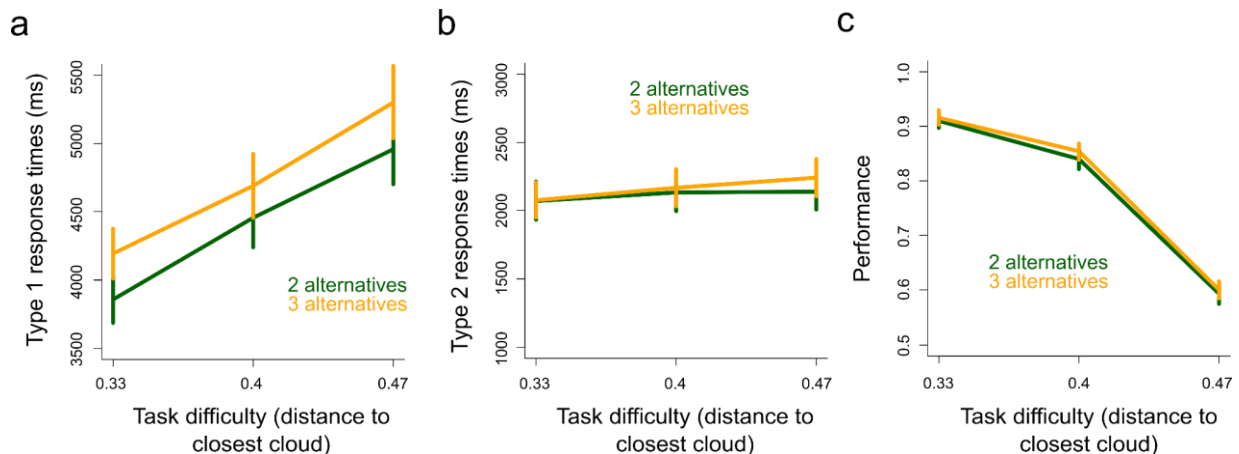
## 5.2 Results

### 5.2.1 Response times

Task difficulty had a significant effect on decisions RT ( $F_{2, 102} = 34.40$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.40$ ) (Fig. 11a). RT were also larger for the 3-alternative condition ( $F_{1, 51} = 14.38$ ,  $p = 0.0004$ ,  $\eta_p^2 = 0.22$ ) (Fig. 10a). No interaction was found between the number of alternatives and task difficulty ( $F_{2, 102} = 0.26$ ,  $p = 0.77$ ,  $\eta_p^2 = 0.005$ ) (Fig. 10a). Task difficulty affected confidence reports RT ( $F_{2, 102} = 3.63$ ,  $p = 0.03$ ,  $\eta_p^2 = 0.07$ ). The number of alternatives did not impact confidence reports RT ( $F_{1, 51} = 3.20$ ,  $p = 0.08$ ,  $\eta_p^2 = 0.059$ ). No interaction was found between task difficulty and the number of alternatives ( $F_{2, 102} = 1.01$ ,  $p = 0.37$ ,  $\eta_p^2 = 0.02$ ).

### 5.2.2 Performance

Performance, as expected, decreased as the task became more difficult ( $F_{2, 102} = 418.85$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.89$ ) (Fig. 10c). The presence of a third alternative did not have an effect on performance ( $F_{1, 51} = 0.78$ ,  $p = 0.38$ ,  $\eta_p^2 = 0.015$ ) (Fig. 10c).

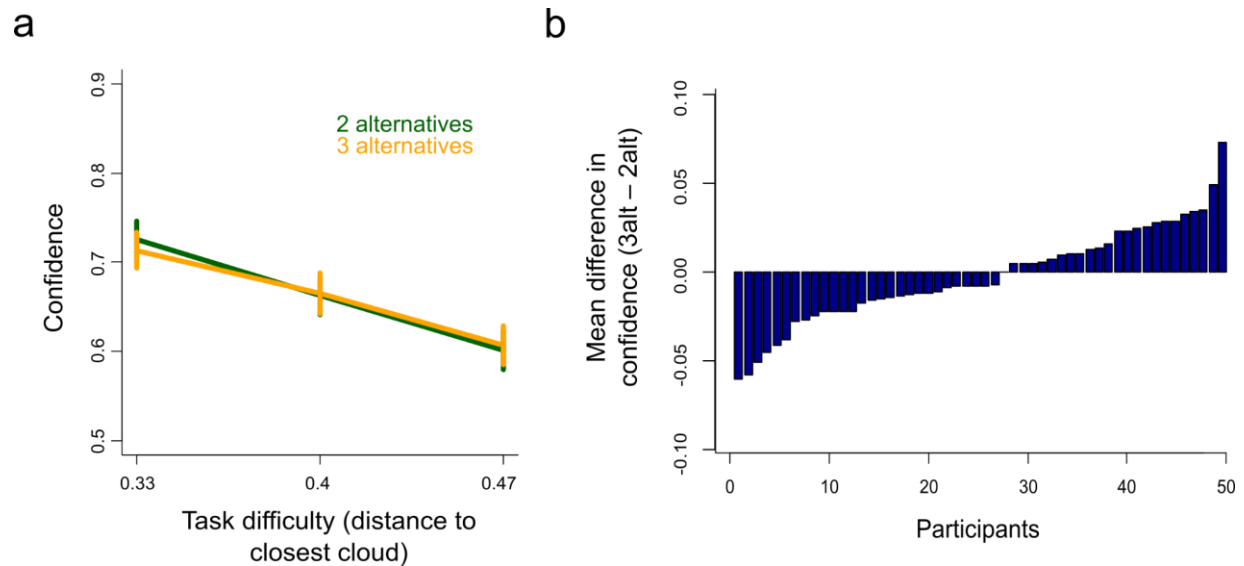


**Fig. 10.** (a) Both task difficulty and the presence of the dud alternative increased response times in the decisions. (b) Contrary to decisions, response times for the confidence report were not affected neither by task difficulty nor the amount of alternatives. (c) Performance decreased as the task difficulty increased, whereas the dud alternative did not affect it.

### 5.2.3 Confidence

Confidence, as expected and in line with performance, decreased when the task got more difficult ( $F_{2, 102} = 97.59$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.66$ ) (Fig. 11a). In contrast with the results from Experiments 1 and 2, we did not find evidence for higher confidence in the 3-

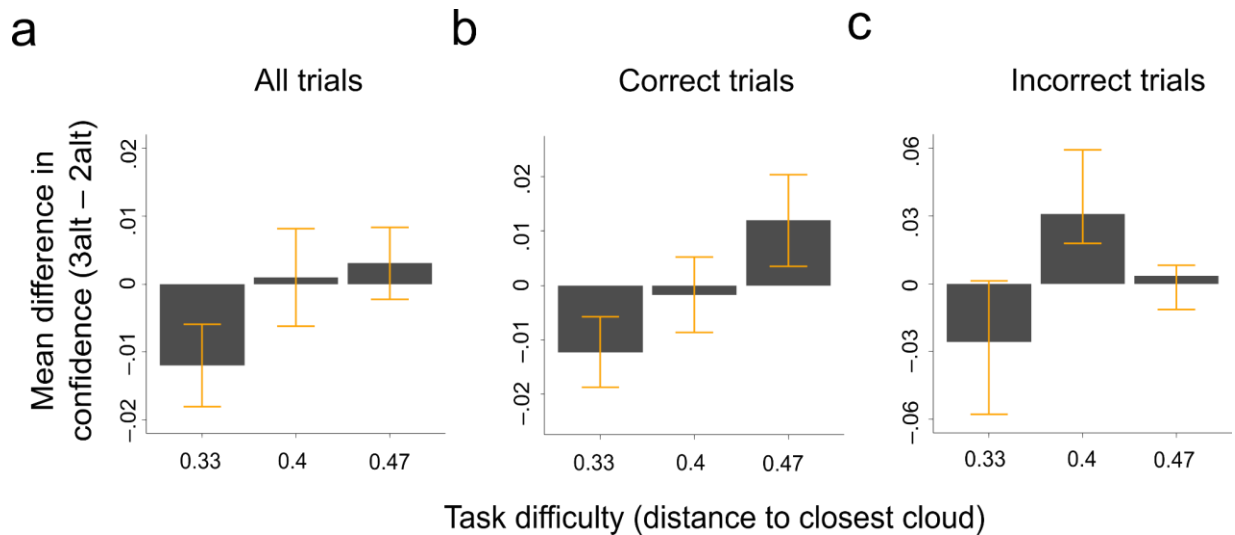
alternative condition ( $F_{1, 51} = 0.485, p = 0.49, \eta_p^2 = 0.009$ ) (Fig. 11b) and there was not an interaction between the number of alternatives and task difficulty ( $F_{2, 102} = 1.84, p < 0.16, \eta_p^2 = 0.035$ ).



**Fig. 11.** Effect of number of alternatives on confidence. (a) Confidence diminished with task difficulty and is not affected by the presence of an irrelevant alternative. (b) Confidence difference between 3 and 2 alternative conditions, per participant.

We explored the impact of the presence of the third alternative on confidence level separately for correct and incorrect responses, as in Experiment 1 (Fig. 12). For correct trials only, confidence was not affected by the number of alternatives ( $F_{1, 51} = 0.03, p = 0.86, \eta_p^2 = 0.0006$ ) and we did not find an interaction between task difficulty and the number of alternatives ( $F_{2, 102} = 2.61, p = 0.078, \eta_p^2 = 0.05$ ). For incorrect trials, we did not find an effect of the amount of alternatives ( $F_{1, 25} = 0.045, p = 0.83, \eta_p^2 = 0.002$ ) or an interaction between task difficulty and the number of alternatives ( $F_{2, 50} = 1.40, p = 0.26, \eta_p^2 = 0.05$ ) (Fig. 12c).





**Fig. 12.** The impact of the third alternative on confidence dissociated by correct and incorrect responses. (a) Considering all trials, the third alternative did not increase confidence at any level of difficulty. Moreover, the third alternative did not have an effect on confidence neither when considering (b) correct trials nor (c) incorrect trials.

### 5.3 Discussion

The target categorization task of Experiment 3 does not show a dud-alternative effect: confidence remained the same despite the addition of a third, clearly incorrect alternative. The inclusion of the dud-alternative did not affect performance or confidence, but made response times longer. This could be one of the reasons that this experiment bears no dud-alternative effect, since longer response times are usually associated with more difficult tasks and with lower confidence levels (Kiani et al., 2014). Another possible reason underlying the lack of the dud-alternative effect is the different presentation times of the stimuli: up to 1 second in experiments 1 and 2, and untimed in Experiment 3. In fact, the computations underlying confidence in purely perceptual tasks with brief stimuli presentations could be different because confidence has to rely more on the internal representation of the stimuli (Rahnev, 2020; Yeon & Rahnev, 2020). Consequently, we decided to test in Experiment 4 and 5 whether the dud-alternative effect is present both in the size discrimination task with unlimited presentation time of the stimuli (as in Experiment 3) and in the target categorization task with the stimuli presentation time restricted to one second (as in Experiments 1 and 2).

## 6. Experiment 4

To investigate whether stimuli presentation time is driving the dud alternative effect, we conducted two more experiments: Experiment 4 consisted of the same size discrimination task as in Experiment 1 but stimuli were present up to the time of the decision as in

Experiment 3; Experiment 5 consisted of the same target categorization task as in Experiment 3 with stimuli being on screen for 1 second as in Experiments 1 and 2.

## 6.1 Materials & methods

As in the previous experiments, Experiment 4 was conducted online on JATOS (Lange et al., 2015) and programmed in JavaScript using the library jQuery.

### 6.1.1 Participants & experimental design

34 participants took part in this experiment (73.5% females; mean age = 25.5, sd = 6.38). One subject was excluded due to slow response times (see 6.1.2 Data analysis), so the final sample consisted of 33 participants.

The design was similar to the design of Experiment 1, with the difference that the stimuli remained on screen up to the time that the participant made the decision. To inform their choice, participants clicked directly on the geometrical figures.

### 6.1.2 Data analysis

We excluded trials with RT lower than 200 ms for both decisions and confidence reports. We also excluded trials with RT greater than 20 s (both in decisions 1 and confidence reports) as in Experiment 3. With this filter one subject was completely excluded because of larger response times. The reported results do not change if we include this data. We conducted repeated measures ANOVAs and Tukey HSD post hoc tests (both with the Statistica software) to estimate the impact of the difficulty of the task and the dud alternatives in RT, performance and confidence. Our predefined p-value for statistical significance was 0.05. The ANOVA for incorrect trials was done with the highest levels of difficulty (0.9, 0.93, 0.95) because there were not enough incorrect trials in easier conditions (0.7 and 0.8).

## 6.2 Results

### 6.2.1 Response times

Task difficulty had a significant effect on decisions RT ( $F_{4, 128} = 27.49$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.46$ ) (Fig. 13a). The inclusion of a third alternative did not affect decisions RT ( $F_{1, 32} = 0.39$ ,  $p = 0.54$ ,  $\eta_p^2 = 0.02$ ). No interaction was found between the number of alternatives and task difficulty ( $F_{4, 128} = 1.12$ ,  $p = 0.35$ ,  $\eta_p^2 = 0.03$ ). Task difficulty affected confidence reports RT ( $F_{4, 128} = 5.79$ ,  $p = 0.0003$ ,  $\eta_p^2 = 0.15$ ). The number of alternatives did not impact confidence reports RT ( $F_{1, 32} = 0.49$ ,  $p = 0.49$ ,  $\eta_p^2 = 0.015$ ). An interaction was found between task difficulty and the number of alternatives regarding confidence reports RT ( $F_{4, 128} = 2.84$ ,  $p = 0.03$ ,  $\eta_p^2 = 0.08$ ).

### 6.2.2 Performance

Performance, as expected, decreased as the task became more difficult ( $F_{4, 128} = 92.64$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.74$ ). The presence of a third alternative did not have an effect on performance ( $F_{1, 32} = 2.80$ ,  $p = 0.10$ ,  $\eta_p^2 = 0.08$ ). We did not find an interaction between task difficulty and the number of alternatives ( $F_{4, 128} = 1.45$ ,  $p = 0.22$ ,  $\eta_p^2 = 0.04$ ).

We again analyzed whether the shape of the third alternative had an effect on the shape that the participant picked (“square” vs “circle” choices). Comparing the 2-alternative condition and the 3-alternative condition when the dud-alternative was a square shows no effect regarding “square” choices ( $F_{1, 32} = 0.05$ ,  $p = 0.82$ ,  $\eta_p^2 = 0.002$ ). The presence of a third alternative that was a circle did not affect the proportion of “circle” choices either ( $F_{1, 32} = 1.11$ ,  $p = 0.3$ ,  $\eta_p^2 = 0.025$ ).

### 6.2.3 Confidence

Confidence, as expected and in line with performance, decreased with task difficulty ( $F_{4, 128} = 49.02$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.61$ ) (Fig. 13a). We replicated the dud-alternative effect found in Experiments 1 and 2 since confidence increased in the 3-alternative condition ( $F_{1, 32} = 20.28$ ,  $p = 0.00008$ ,  $\eta_p^2 = 0.39$ ) (Fig. 13a). Also, there was an interaction between the number of alternatives and task difficulty ( $F_{4, 128} = 3.03$ ,  $p = 0.02$ ,  $\eta_p^2 = 0.09$ ) (Fig. 13a). The effect was found for both correct ( $F_{1, 32} = 16.79$ ,  $p = 0.0003$ ,  $\eta_p^2 = 0.34$ ) and incorrect ( $F_{1, 22} = 7.87$ ,  $p = 0.01$ ,  $\eta_p^2 = 0.26$ ) trials. Comparing the confidence increment between correct and incorrect trials (on the 3 highest levels of difficulty) no differences were found ( $F_{1, 22} = 0.88$ ,  $p = 0.36$ ,  $\eta_p^2 = 0.04$ ).

Regarding the size of the third alternative, we found a significant effect ( $F_{6, 186} = 2.67$ ,  $p = 0.02$ ,  $\eta_p^2 = 0.08$ ). A Tukey HSD post-hoc test shows that the differences are between the 2-alternative condition and the conditions where the third alternative adopted the 0.07 ( $p = 0.04$ ) and the 0.28 ( $p = 0.008$ ) of the area of the stimulus 1.

As in Experiment 1, we did not find an effect of the shape of the third alternative on confidence: when considering if the dud alternative was a circle or a square only on the 3-alternative condition, no difference was found in confidence neither for “circle” choices ( $F_{1, 21} = 0.73$ ,  $p = 0.4$ ,  $\eta_p^2 = 0.03$ ) nor for “square” choices ( $F_{1, 27} = 0.43$ ,  $p = 0.52$ ,  $\eta_p^2 = 0.016$ ).

## 7. Experiment 5

As mentioned previously, to evaluate if presentation time of the stimuli is the main factor driving the dud-alternative effect we also conducted the target categorization task of Experiment 3 but with restricted presentation time: stimuli were present on screen up to 1 second as in Experiments 1 and 2.

## 7.1 Materials & methods

### 7.1.1 Participants & experimental design

31 participants took part in this experiment (83.9% females; mean age = 27.42, sd = 7.64). Participants should read and accept an informed consent prior to the realization of the experiment. All participants reported no psychiatric, illegal drug consumption or neurological history. The tasks' instructions were written on screen prior to the experiment. All participants completed the experiment on a computer.

The design was the same as Experiment 3, with the difference that the stimuli remained on screen up to 1 second.

### 7.1.2 Data analysis

We excluded trials with RT lower than 200 ms for both decisions and confidence reports. We also excluded trials with RT greater than 10 s (both in decisions and confidence reports) as in Experiments 1 and 2. Including the discarded data does not modify the results. We conducted repeated measures ANOVAs and Tukey HSD post hoc tests (both with the Statistica software) to estimate the impact of the difficulty of the task and the dud alternatives in RT, performance and confidence. Our predefined p-value for statistical significance was 0.05.

## 7.2 Results

### 7.2.1 Response times

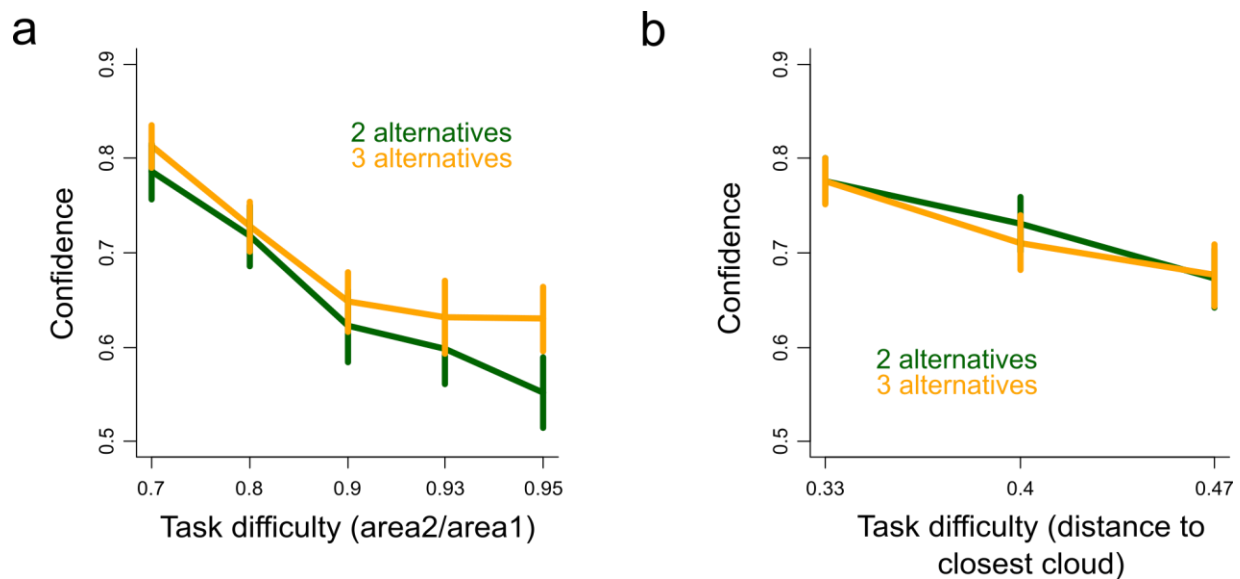
Task difficulty had a significant effect on decisions RT ( $F_{2, 60} = 13.73$ ,  $p = 0.00001$ ,  $\eta_p^2 = 0.31$ ). The inclusion of a third alternative made decisions RT larger ( $F_{1, 30} = 4.84$ ,  $p = 0.04$ ,  $\eta_p^2 = 0.14$ ). No interaction was found between the number of alternatives and task difficulty for decisions RT ( $F_{2, 60} = 1.52$ ,  $p = 0.23$ ,  $\eta_p^2 = 0.05$ ). Task difficulty did not affect confidence reports RT ( $F_{2, 60} = 1.66$ ,  $p = 0.20$ ,  $\eta_p^2 = 0.05$ ). The number of alternatives did not impact confidence reports RT ( $F_{1, 30} = 0.67$ ,  $p = 0.42$ ,  $\eta_p^2 = 0.02$ ). No interaction was found between task difficulty and the number of alternatives regarding confidence reports RT ( $F_{2, 60} = 0.44$ ,  $p = 0.65$ ,  $\eta_p^2 = 0.01$ ).

### 7.2.2 Performance

Performance decreased with task difficulty ( $F_{2, 60} = 155.77$ ,  $p < 0.000001$ ,  $\eta_p^2 = 0.84$ ). The presence of a third alternative did not have an effect on performance ( $F_{1, 30} = 0.035$ ,  $p = 0.85$ ,  $\eta_p^2 = 0.001$ ). We did not find an interaction between task difficulty and the number of alternatives ( $F_{2, 60} = 0.52$ ,  $p = 0.6$ ,  $\eta_p^2 = 0.02$ ).

### 7.2.3 Confidence

Confidence decreased with increasing levels of task difficulty ( $F_{2, 60} = 31.47, p < 0.000001, \eta_p^2 = 0.51$ ) (Fig. 13b). As in Experiment 3, confidence was not affected by the presence of a dud-alternative ( $F_{1, 30} = 1.15, p = 0.29, \eta_p^2 = 0.04$ ) (Fig. 13b). There was not an interaction between the number of alternatives and task difficulty ( $F_{2, 60} = 1.69, p = 0.19, \eta_p^2 = 0.05$ ) (Fig. 13b).



**Fig. 13.** Both experiments show converging evidence that the dud-alternative effect is independent of the presentation time of the stimuli. a) The dud-alternative effect was found for the size discrimination task even if stimuli remained on screen up to the participants' response. b) Despite restricting stimuli presentation time up to 1s in the target categorization task, no dud-alternative effect was found.

## 7.3 Discussion

Both Experiments 4 and 5 show converging evidence that the dud-alternative effect is not dependent on the presentation time of the stimuli, as the effect was replicated in Experiment 4 and, again, not found in the target categorization task of Experiment 5.

The dud alternatives did not affect performance nor RT in the size discrimination task, adding more evidence to the previous claims of Experiment 1 and 2 that the dud-alternatives did not make the task harder. Regarding RTs for the target categorization task, we found again that they were longer in the 3-alternative condition (as in Experiment 3). This could reflect that people were in fact more uncertain when the third alternative was present, thus canceling out a possible dud-alternative effect because of a decision process inherently more difficult.

Experiment 4 shows no “attraction effect”: people were equally likely to choose a square when the third alternative was a square when compared to the 2-alternative condition, and the same holds for “circle” choices. Moreover, this experiment replicates the findings of Experiment 1 in the sense that the shape of the dud-alternative did not affect confidence reports. In consequence, both experiments suggest that the dud-alternative effect is independent of the attraction effect.

## **8. General discussion**

In the present study, we investigated whether irrelevant alternatives increase confidence in a perceptual decision. The underlying motivation was that this kind of effect was reported in likelihood judgements (Windschitl & Chambers, 2004), line-up identifications (Charman et al., 2011) and associative memory (Hanczakowski et al., 2014) but never tested in perceptual confidence contexts. Furthermore, most accepted computational models of confidence in perceptual decisions (H.-H. Li & Ma, 2020; Meyniel et al., 2015; Sanders et al., 2016) state that the presence of irrelevant alternatives should not modify it or, in any case, should decrease it. Contrary, our main finding is that these alternatives can increase confidence in perceptual decisions, a result that seems at odds with normative models of confidence.

These weak alternatives, however, do not impact RTs (Experiments 1 and 2) or performance. These null effects are important because they discard that changes in performance or overconfidence usually present in difficult tasks (Baranski & Petrusic, 1994; Gigerenzer et al., 1991) are raising confidence.

Our results from Experiment 1 and 2 cannot be explained by current views of the field proposing that confidence arises directly from the probability of being correct (Meyniel et al., 2015; Sanders et al., 2016) or direct comparisons between the more probable stimulus and the second one (H.-H. Li & Ma, 2020). This depicts why considering the effect of irrelevant alternatives (Charman et al., 2011; Hanczakowski et al., 2014; Windschitl & Chambers, 2004) in models of confidence is needed. To account for the effect in non-perceptual tasks, Charman et al. (2011), Windschitl & Chambers (2004) and Hanczakowski et al. (2014) proposed various theoretical explanations. Interestingly, the preferred one was the Contrast model, that we computationally implemented: confidence level is obtained by a series of pairwise comparisons between the chosen option and the rest. Nevertheless, our computational modeling results suggest that, although the Contrast model captures the effect of increased confidence levels when a dud-alternative is present, only the Average-residual model replicates the pattern of our data. Specifically, the Average-residual model states that people construct their confidence by first judging the support offered by the evidence for chosen option and the support offered by the

average of the rest of the alternatives and then taking the difference between them. In this model having dud alternatives decreases the value of the competing options, inflating confidence.

The Contrast model faces many issues when extending its predictions to other decision contexts. First, the model predicts a constant increment in confidence when adding more than one dud-alternative (for example, a decision context with 2, 3 or more dud-alternatives), as illustrated in Supplementary Fig. 3b. This is not reasonable in extreme cases such as when an observer has to decide between a lot of alternatives (for example, adding a dud-alternative when there are already 15 dud-alternatives is not expected to raise confidence by the same amount as when there are not any dud-alternatives). The Average-residual model, conversely, predicts that increment in confidence should progressively decrease with the number of dud-alternatives, since the average of the residual alternatives will progressively change less with more dud-alternatives. Therefore, the Average-residual model is in a better position to account for the results reported in Experiment 2.

Second, when varying the size of a third alternative –ranging from a dud-alternative to a truly competitive alternative– the Contrast model still predicts that confidence should be higher in the 3-alternative condition. This is a counterintuitive prediction since it is expected that confidence will be lower in the case where 3 alternatives are equally likely to be the right decision when compared to only 2 equally likely alternatives. On the other hand, the Average-residual model predicts that confidence should be lower in that case, as expected (Supplementary Fig. 3a). This is because these models imply normalization, so a high value of a third alternative implies that the posterior probability for the chosen option also decreases, leading to a decrease in confidence. However, this decrease is not large enough to compensate for the increase in confidence by the presence of a dud-alternative in the Contrast model.

Finally, the Contrast model predicts that confidence should always increase with the presence of a dud-alternative, even if the task at hand is very easy. This is, again, a counterintuitive prediction since if a task is really easy one should reach a maximum confidence level. Therefore, the addition of a dud-alternative is not expected to have a large effect. The Average-residual model, on the other hand, predicts that the increase in confidence should be lower on easy tasks (and no increment is predicted if the two non-chosen options are equal, i.e. the both options are dud-alternatives). Indeed, according to the Average-residual mechanism, we found a null or reduced increase in confidence on easy trials on Experiment 1, 2 and 4. Taking into account all of these predictions, the Average-residual model not only is the best explanation for the dud-alternative effect, but

also seems a plausible blueprint for a general mechanism for computing confidence in multi-alternative tasks in general.

Windschitl & Chambers (2004) discuss a version of the Contrast model that includes a weight in the comparison between the chosen option and the dud-alternative, thus making the increment in confidence due to this contrast flexible. With this modification, the model could improve its performance regarding the fit to our data. However, this modified Contrast model will still predict a constant, difficulty independent increment in confidence, so it is likely that the model will not be better than the Average-residual model as it is (and, consequently, will definitely not be better than an Average-residual model including a weight, to match the number of free parameters). Moreover, the modification implies that the model should have an extra free parameter for controlling the weight of the contrast, making the model more complex unnecessarily since there is already a model that provides a better fit without the need of an extra free parameter.

Prior research suggests that maintaining mental representations for all alternatives is costly (Maniscalco et al., 2016). In that scenario, confidence only relies on the evidence in favor of the chosen option, also known as “positive evidence bias” (Koizumi et al., 2015; Maniscalco et al., 2016; Peters et al., 2017; Zylberberg et al., 2012). However, unchosen options can affect confidence (H.-H. Li & Ma, 2020). Our results and model are in line with this posture, since even very weak alternatives are taken into account to make confidence judgments. Moreover, our findings also deviate from the notion that, in multi-alternative perceptual decisions, individuals making decisions only have access to the level of activity of the alternative with highest internal activity (Yeon & Rahnev, 2020). Indeed, the Average-residual model necessarily implies that the level of activity of all alternatives is accessible for the observer in order to compute confidence.

The picture, however, seems more complicated. Our results from Experiments 3 and 5 show that, in that particular task, the dud-alternative barely affects confidence. This constitutes a main challenge for the Average-residual model. Why does this experimental paradigm show no dud-alternative effect? First of all, the slower reaction times found in these experiments in the 3-alternative condition may indicate that observers were more uncertain and needed more time to make their decision; this could counteract the dud-alternative effect. Second, we tested if stimuli presentation time plays a role in the dud-alternative effect. The reason was that in perceptual tasks with brief stimuli presentations, confidence computations rely more on an internal representation (Rahnev, 2020). Thus, mechanisms acting in Experiments 1 and 2 may differ from the ones acting in Experiment 3. In fact, the dud alternative effect is more prominent in timed tasks (Windschitl & Chambers, 2004). In this line, an alternative explanation for our results might be that the dud alternative effect depends on a form of variance misperception (Zylberberg et al.,



2014), an overconfidence bias found in perceptual tasks when signal is low and perceptual noise is added (M. K. Li et al., 2018; Rahnev et al., 2011; Solovey et al., 2015). The presence of dud alternatives might add perceptual noise, causing the participants to have higher levels of confidence if they do not adjust their confidence criteria accordingly. That is, if participants fixate on the third alternative, the rest of the alternatives remain at an attentional periphery, where there are effects of variance misperception and overconfidence (Winter & Peters, 2021) due to noisier percepts caused by the poorer resolution of the peripheral visual field. Larger stimuli presentations would rule out possible variance misperception effects, due to a higher signal to noise ratio. However, decreasing the stimuli duration used in Experiment 3 (Experiment 5) does not induce a raise in confidence levels in 3-alternative trials; also, the effect does not disappear with unlimited presentation time in the size discrimination task (Experiment 4). Consequently, stimuli presentation time seems not to be a factor driving the dud-alternative effect. In third place, another possible explanation might be that the dud-alternative effect in the size discrimination task is driven by the “Ebbinghaus illusion” (Roberts et al., 2005): shapes are perceived larger when surrounded by small shapes. The irrelevant alternative(s) may induce such an illusion by making the chosen option appear larger to the observer as compared to when the dud-alternative is not present. Confidence therefore will be higher due to the “positive evidence bias” mentioned above: the observer has now more evidence for her choice, because her chosen option now seems larger than in the 2-alternative condition. Importantly, if this is the case, it may explain why there is not a dud-alternative effect in Experiment 3 and 5, as this illusion is not present with that stimuli. Despite appealing, the Ebbinghaus illusion explanation predicts that the increment in confidence should be more pronounced on easy trials because all of the incorrect options are small. However, we see the opposite pattern in our data: confidence level rises due to the dud-alternative presence specifically on difficult trials, consistent with the explanation proposed by the Average-residual model. Moreover, according to the Ebbinghaus illusion account, the increment in confidence should be higher with lower size values of the third alternative. However, no effect was found regarding the size of irrelevant alternatives within the 3-alternative condition: confidence increased equally irrespective of the third alternative size. This is again consistent with the Average-residual account as the model predicts a relatively constant increase in confidence as long as the alternatives are irrelevant, as in our case (Supplementary Fig. 3).

Having ruled out those possible explanations, we must note that the dud-alternative effect is already reported in a range of different tasks (Charman et al., 2011; Hanczakowski et al., 2014; Windschitl & Chambers, 2004). This implies that different mechanisms take place on the target categorization task of Experiments 3 and 5. We identify three major characteristics of this experimental paradigm that are likely causing the lack of effect. First, this task requires a probabilistic response, i.e. the target could belong to either cloud

with a certain probability. This kind of probabilistic alternatives is different from the size discrimination task and also from the previous dud-alternative effect literature, where there were definite correct alternatives. This may induce a more probabilistic –and therefore, normative– use of the confidence scale, that could explain the absence of the rise in confidence levels in presence of the third cloud. Indeed, the dud-alternative effect is not present in tasks that induce concerns regarding the complementary rule (Windschitl & Chambers, 2004). Second, this task implies a direct distance judgment (between the target and the clouds) between two probable alternatives, thus making it reasonable that confidence reflects the difference between the probabilities of the best-two competing alternatives, as stated by the Diff model. Finally, there is the possibility that the third alternative was not even taken into account by the subjects for being highly irrelevant. Under this possibility, the increased response times on both target categorization experiments in the 3-alternative condition may reflect extra-time for searching for the target instead of increased uncertainty. As the distance between the third alternative and the target was not manipulated, we cannot rule out this possibility. Further research could vary this distance to evaluate whether this is a plausible explanation.

Previous research including irrelevant alternatives has shown a wide range of context effects in our decision making. The size discrimination task used here allow for the possibility of testing one particular context effect: the attraction effect (Huber et al., 1982), already reported in perceptual decision making (Trueblood et al., 2013). This effect implies that decision makers will more likely choose a specific alternative A when comparing to another alternative B when a third option simultaneously similar but inferior to A is added in the decision context. In Experiment 1, we found an attraction effect for “square” choices restricted to the highest level of difficulty (that is, participants were more likely to choose a square if the third alternative was also a square), but no clear pattern was found regarding the “circle” choices. Importantly, this effect does not interact with the increase in confidence. In Experiment 4 we did not find any attraction effect, neither in choices nor in confidence. These results suggest that the dud-alternative effect is independent of the attraction effect.

In conclusion, our results imply that —at least in some contexts— confidence in multi-alternative decisions deviates from the traditional Bayesian confidence hypothesis and from the Difference model, recently developed for decisions with multiple alternatives. Moreover, our findings suggest that unchosen options affect confidence in a way that is explained by the Average-residual model. This particular model not only gives the best explanation for the dud-alternative effect but also points out a possible mechanism for computing confidence in general multi-alternative contexts. Future computational models should consider this effect and the predictions of the Average-residual model to more accurately explain human confidence levels in perceptual decision-making.

## **CRedit authorship contribution statement**

**Nicolás A. Comay:** Conceptualization, Methodology, Software, Validation, Formal analysis, Investigation, Data curation, Writing – Original Draft, Writing – Review & Editing, Visualization. **Gabriel Della Bella:** Software. **Pedro Lamberti:** Software. **Mariano Sigman:** Conceptualization, Methodology, Writing – Original Draft, Writing – Review & Editing, Supervision. **Guillermo Solovey:** Conceptualization, Methodology, Software, Writing – Original Draft, Writing – Review & Editing, Supervision, Funding acquisition, Project administration. **Pablo Barttfeld:** Conceptualization, Methodology, Software, Writing – Original Draft, Writing – Review & Editing, Supervision, Funding acquisition, Project administration.

## **Acknowledgements**

This research was supported by a grant from Agencia Nacional de Promoción Científica y Tecnológica (Argentina) PICT (Grant #2018-03614). Nicolás A. Comay and Gabriel Della Bella have a scholarship from the National Scientific and Technical Research Council (CONICET - Argentina).

## **Supplementary material**

All data and materials are stored in [https://github.com/nicolascomay/confidence\\_dud](https://github.com/nicolascomay/confidence_dud). This includes the source code of the 5 experiments, the .jzip archives for uploading the experiments to JATOS and R code for model fitting and replication of main figures.

## **Declaration of interest**

None.

## **References**

- Ais, J., Zylberberg, A., Barttfeld, P., & Sigman, M. (2016). Individual consistency in the accuracy and distribution of confidence judgments. *Cognition*, *146*, 377-386.  
<https://doi.org/10.1016/j.cognition.2015.10.006>
- Ariely, D., & Wallsten, T. S. (1995). Seeking Subjective Dominance in Multidimensional

Space: An Explanation of the Asymmetric Dominance Effect. *Organizational Behavior and Human Decision Processes*, 63(3), 223-232.

<https://doi.org/10.1006/obhd.1995.1075>

Baranski, J. V., & Petrusic, W. M. (1994). The calibration and resolution of confidence in perceptual judgments. *Perception & Psychophysics*, 55(4), 412-428.

<https://doi.org/10.3758/BF03205299>

Charman, S. D., Wells, G. L., & Joy, S. W. (2011). The dud effect: Adding highly dissimilar fillers increases confidence in lineup identifications. *Law and Human Behavior*, 35(6), 479-500. <https://doi.org/10.1007/s10979-010-9261-1>

Drugowitsch, J., Moreno-Bote, R., & Pouget, A. (2014). Relation between Belief and Performance in Perceptual Decision Making. *PLOS ONE*, 9(5), e96511.

<https://doi.org/10.1371/journal.pone.0096511>

Fleming, S. M., & Lau, H. C. (2014). How to measure metacognition. *Frontiers in Human Neuroscience*, 8. <https://doi.org/10.3389/fnhum.2014.00443>

Galvin, S. J., Podd, J. V., Drga, V., & Whitmore, J. (2003). Type 2 tasks in the theory of signal detectability: Discrimination between correct and incorrect decisions.

*Psychonomic Bulletin & Review*, 10(4), 843-876.

<https://doi.org/10.3758/BF03196546>

Gigerenzer, G., Hoffrage, U., & Kleinbölting, H. (1991). Probabilistic mental models: A Brunswikian theory of confidence. *Psychological Review*, 98(4), 506-528.

<https://doi.org/10.1037/0033-295X.98.4.506>

Grimaldi, P., Lau, H., & Basso, M. A. (2015). There are things that we know that we know, and there are things that we do not know we do not know: Confidence in

decision-making. *Neuroscience & Biobehavioral Reviews*, 55, 88-97.

<https://doi.org/10.1016/j.neubiorev.2015.04.006>

Hanczakowski, M., Zawadzka, K., & Higham, P. A. (2014). The dud-alternative effect in memory for associations: Putting confidence into local context. *Psychonomic Bulletin & Review*, 21(2), 543-548. <https://doi.org/10.3758/s13423-013-0497-x>

Huber, J., Payne, J. W., & Puto, C. (1982). Adding Asymmetrically Dominated Alternatives: Violations of Regularity and the Similarity Hypothesis. *Journal of Consumer Research*, 9(1), 90. <https://doi.org/10.1086/208899>

Kepecs, A., & Mainen, Z. F. (2012). A computational framework for the study of confidence in humans and animals. *Philosophical Transactions of the Royal Society B: Biological Sciences*, 367(1594), 1322-1337.

<https://doi.org/10.1098/rstb.2012.0037>

Kiani, R., Corthell, L., & Shadlen, M. N. (2014). Choice Certainty Is Informed by Both Evidence and Decision Time. *Neuron*, 84(6), 1329-1342.

<https://doi.org/10.1016/j.neuron.2014.12.015>

Koizumi, A., Maniscalco, B., & Lau, H. (2015). Does perceptual confidence facilitate cognitive control? *Attention, Perception, & Psychophysics*, 77(4), 1295-1306.

<https://doi.org/10.3758/s13414-015-0843-3>

Lange, K., Kühn, S., & Filevich, E. (2015). "Just Another Tool for Online Studies" (JATOS): An Easy Solution for Setup and Management of Web Servers Supporting Online Studies. *PLOS ONE*, 10(6), e0130834.

<https://doi.org/10.1371/journal.pone.0130834>

Li, H.-H., & Ma, W. J. (2020). Confidence reports in decision-making with multiple

- alternatives violate the Bayesian confidence hypothesis. *Nature Communications*, 11(1), 2004. <https://doi.org/10.1038/s41467-020-15581-6>
- Li, M. K., Lau, H., & Odegaard, B. (2018). An investigation of detection biases in the unattended periphery during simulated driving. *Attention, Perception, & Psychophysics*, 80(6), 1325-1332. <https://doi.org/10.3758/s13414-018-1554-3>
- Louie, K., Khaw, M. W., & Glimcher, P. W. (2013). Normalization is a general neural mechanism for context-dependent decision making. *Proceedings of the National Academy of Sciences*, 110(15), 6139-6144. <https://doi.org/10.1073/pnas.1217854110>
- Luce, R. D. (1979). *Individual choice behavior: A theoretical analysis*. Greenwood Press.
- Ma, W. J. (2019). Bayesian Decision Models: A Primer. *Neuron*, 104(1), 164-175. <https://doi.org/10.1016/j.neuron.2019.09.037>
- Mamassian, P. (2016). Visual Confidence. *Annual Review of Vision Science*, 2(1), 459-481. <https://doi.org/10.1146/annurev-vision-111815-114630>
- Maniscalco, B., & Lau, H. (2012). A signal detection theoretic approach for estimating metacognitive sensitivity from confidence ratings. *Consciousness and Cognition*, 21(1), 422-430. <https://doi.org/10.1016/j.concog.2011.09.021>
- Maniscalco, B., Peters, M. A. K., & Lau, H. (2016). Heuristic use of perceptual evidence leads to dissociation between performance and metacognitive sensitivity. *Attention, Perception, & Psychophysics*, 78(3), 923-937. <https://doi.org/10.3758/s13414-016-1059-x>
- Meyniel, F., Sigman, M., & Mainen, Z. F. (2015). Confidence as Bayesian Probability:

From Neural Origins to Behavior. *Neuron*, 88(1), 78-92.

<https://doi.org/10.1016/j.neuron.2015.09.039>

Niwa, M., & Ditterich, J. (2008). Perceptual Decisions between Multiple Directions of Visual Motion. *Journal of Neuroscience*, 28(17), 4435-4445.

<https://doi.org/10.1523/JNEUROSCI.5564-07.2008>

Northoff, G., & Mushiake, H. (2020). Why context matters? Divisive normalization and canonical microcircuits in psychiatric disorders. *Neuroscience Research*, 156, 130-140. <https://doi.org/10.1016/j.neures.2019.10.002>

Peters, M. A. K., Thesen, T., Ko, Y. D., Maniscalco, B., Carlson, C., Davidson, M., Doyle, W., Kuzniecky, R., Devinsky, O., Halgren, E., & Lau, H. (2017).

Perceptual confidence neglects decision-incongruent evidence in the brain.

*Nature Human Behaviour*, 1(7), 0139. <https://doi.org/10.1038/s41562-017-0139>

Pleskac, T. J., & Busemeyer, J. R. (2010). Two-stage dynamic signal detection: A theory of choice, decision time, and confidence. *Psychological Review*, 117(3), 864-901. <https://doi.org/10.1037/a0019737>

Pouget, A., Drugowitsch, J., & Kepecs, A. (2016). Confidence and certainty: Distinct probabilistic quantities for different goals. *Nature Neuroscience*, 19(3), 366-374.

<https://doi.org/10.1038/nn.4240>

Rahnev, D. (2020). Confidence in the Real World. *Trends in Cognitive Sciences*, 24(8), 590-591. <https://doi.org/10.1016/j.tics.2020.05.005>

Rahnev, D., & Denison, R. N. (2018). Suboptimality in perceptual decision making.

*Behavioral and Brain Sciences*, 41, e223.

<https://doi.org/10.1017/S0140525X18000936>

- Rahnev, D., Maniscalco, B., Graves, T., Huang, E., de Lange, F. P., & Lau, H. (2011). Attention induces conservative subjective biases in visual perception. *Nature Neuroscience*, *14*(12), 1513-1515. <https://doi.org/10.1038/nn.2948>
- Ratcliff, R., Smith, P. L., Brown, S. D., & McKoon, G. (2016). Diffusion Decision Model: Current Issues and History. *Trends in Cognitive Sciences*, *20*(4), 260-281. <https://doi.org/10.1016/j.tics.2016.01.007>
- Ratcliff, R., & Starns, J. J. (2013). Modeling confidence judgments, response times, and multiple choices in decision making: Recognition memory and motion discrimination. *Psychological Review*, *120*(3), 697-719. <https://doi.org/10.1037/a0033152>
- Roberts, B., Harris, M. G., & Yates, T. A. (2005). The Roles of Inducer Size and Distance in the Ebbinghaus Illusion (Titchener Circles). *Perception*, *34*(7), 847-856. <https://doi.org/10.1068/p5273>
- Sanders, J. I., Hangya, B., & Kepecs, A. (2016). Signatures of a Statistical Computation in the Human Sense of Confidence. *Neuron*, *90*(3), 499-506. <https://doi.org/10.1016/j.neuron.2016.03.025>
- Solovey, G., Graney, G. G., & Lau, H. (2015). A decisional account of subjective inflation of visual perception at the periphery. *Attention, Perception, & Psychophysics*, *77*(1), 258-271. <https://doi.org/10.3758/s13414-014-0769-1>
- Trueblood, J. S., Brown, S. D., Heathcote, A., & Busemeyer, J. R. (2013). Not Just for Consumers: Context Effects Are Fundamental to Decision Making. *Psychological Science*, *24*(6), 901-908. <https://doi.org/10.1177/0956797612464241>
- Windschitl, P. D., & Chambers, J. R. (2004). The Dud-Alternative Effect in Likelihood



Judgment. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, 30(1), 198-215. <https://doi.org/10.1037/0278-7393.30.1.198>

Winter, C. J., & Peters, M. A. K. (2021). *Variance misperception under skewed empirical noise statistics explains overconfidence in the visual periphery* [Preprint].

Neuroscience. <https://doi.org/10.1101/2021.01.08.425966>

Yeon, J., & Rahnev, D. (2020). The suboptimality of perceptual decision making with multiple alternatives. *Nature Communications*, 11(1), Art. 1.

<https://doi.org/10.1038/s41467-020-17661-z>

Zylberberg, A., Barttfeld, P., & Sigman, M. (2012). The construction of confidence in a perceptual decision. *Frontiers in Integrative Neuroscience*, 6.

<https://doi.org/10.3389/fnint.2012.00079>

Zylberberg, A., Roelfsema, P. R., & Sigman, M. (2014). Variance misperception explains illusions of confidence in simple perceptual decisions. *Consciousness and Cognition*, 27, 246-253. <https://doi.org/10.1016/j.concog.2014.05.012>



Click here to access/download  
**Supplementary Item**  
supplementary material.pdf



Table 1. Task structure.

Third alternative size (area3/area2)	Second alternative size (area2/area1)				
	0.7	0.8	0.9	0.93	0.95
Absent	12 trials	12 trials	12 trials	12 trials	12 trials
0.1	2 trials	2 trials	2 trials	2 trials	2 trials
0.2	2 trials	2 trials	2 trials	2 trials	2 trials
0.3	2 trials	2 trials	2 trials	2 trials	2 trials
0.4	2 trials	2 trials	2 trials	2 trials	2 trials
0.5	2 trials	2 trials	2 trials	2 trials	2 trials
0.6	2 trials	2 trials	2 trials	2 trials	2 trials

## The presence of irrelevant alternatives paradoxically increases confidence in perceptual decisions

Nicolás A. Comay<sup>a+</sup>, Gabriel Della Bella<sup>a</sup>, Pedro Lamberti<sup>b</sup>, Mariano Sigman<sup>c,d</sup>,  
Guillermo Solovey<sup>e\*</sup>, Pablo Barttfeld<sup>a\*</sup>

a- Cognitive Science Group. Instituto de Investigaciones Psicológicas (IIPsi), CONICET-UNC, Facultad de Psicología, Universidad Nacional de Córdoba, Boulevard de la Reforma esquina Enfermera Gordillo, CP 5000. Córdoba, Argentina  
[nicocomay@gmail.com](mailto:nicocomay@gmail.com)

b- Facultad de Matemática, Astronomía, Física y Computación, Universidad Nacional de Córdoba, Córdoba, Argentina.

c- Laboratorio de Neurociencia, Universidad Torcuato Di Tella, Buenos Aires, Argentina.

d- Facultad de Lenguas y Educación, Universidad Nebrija, Madrid, Spain.

e- Instituto de Cálculo, Facultad de Ciencias Exactas y Naturales, UBA-CONICET, Buenos Aires, Argentina

+ *corresponding author*

\* *last authors*

## **CRedit authorship contribution statement**

**Nicolás A. Comay:** Conceptualization, Methodology, Software, Validation, Formal analysis, Investigation, Data curation, Writing – Original Draft, Writing – Review & Editing, Visualization. **Gabriel Della Bella:** Software. **Pedro Lamberti:** Software. **Mariano Sigman:** Conceptualization, Methodology, Writing – Original Draft, Writing – Review & Editing, Supervision. **Guillermo Solovey:** Conceptualization, Methodology, Software, Writing – Original Draft, Writing – Review & Editing, Supervision, Funding acquisition, Project administration. **Pablo Barttfeld:** Conceptualization, Methodology, Software, Writing – Original Draft, Writing – Review & Editing, Supervision, Funding acquisition, Project administration.